

This is a copy of the published version, or version of record, available on the publisher's website. This version does not track changes, errata, or withdrawals on the publisher's site.

Magnetic correlations in the triangular antiferromagnet FeGa₂S₄

K. Guratinder, M. Schmidt, H. C. Walker, R. Bewley, M. Wörle, D. Cabra, S. A. Osorio, M. Villalba, A. K. Madsen, L. Keller, A. Wildes, P. Puphal, A. Cervellino, Ch. Rüegg, and O. Zaharko

Published version information

Citation: K Guratinder et al. Magnetic correlations in the triangular antiferromagnet FeGa₂S₄. Phys Rev B 104, no. 6 (2021): 064412

DOI: [10.1103/PhysRevB.104.064412](https://doi.org/10.1103/PhysRevB.104.064412)

This version is made available in accordance with publisher policies. Please cite only the published version using the reference above. This is the citation assigned by the publisher at the time of issuing the APV. Please check the publisher's website for any updates.

This item was retrieved from **ePubs**, the Open Access archive of the Science and Technology Facilities Council, UK. Please contact epublications@stfc.ac.uk or go to <http://epubs.stfc.ac.uk/> for further information and policies.

Magnetic correlations in the triangular antiferromagnet FeGa₂S₄

K. Guratinder

*Laboratory for Neutron Scattering and Imaging, Paul Scherrer Institute, CH-5232 Villigen, Switzerland
and Department of Quantum Matter Physics, University of Geneva, CH-1211 Geneva, Switzerland*

M. Schmidt

*Max-Planck-Institut für Chemische Physik fester Stoffe, 01187 Dresden, Germany*H. C. Walker  and R. Bewley*Rutherford Appleton Laboratory, ISIS Facility, Chilton, Didcot, Oxon OX11 0QX, United Kingdom*M. Wörle *Laboratorium für Anorganische Chemie, ETH Zürich, CH-8093 Zürich, Switzerland*

D. Cabra, S. A. Osorio, and M. Villalba

*Departamento de Física, Facultad de Ciencias Exactas, Instituto de Física de Líquidos y Sistemas Biológicos, CCT La Plata, CONICET,
Universidad Nacional de La Plata, Casilla de Correo 67, 1900 La Plata, Argentina*A. K. Madsen *Quantum Criticality and Dynamics Group, Paul Scherrer Institute, CH-5232 Villigen, Switzerland*L. Keller *Laboratory for Neutron Scattering and Imaging, Paul Scherrer Institute, CH-5232 Villigen, Switzerland*A. Wildes *Institut Laue-Langevin, 156X, 38042 Grenoble Cédex, France*

P. Puphal

Laboratory for Multiscale Materials Experiments, Paul Scherrer Institute, CH-5232 Villigen, Switzerland

A. Cervellino

*Swiss Light Source, Paul Scherrer Institute, CH-5232 Villigen, Switzerland*Ch. Rüegg *Laboratory for Neutron Scattering and Imaging, Paul Scherrer Institute, CH-5232 Villigen, Switzerland
and Department of Quantum Matter Physics, University of Geneva, CH-1211 Geneva, Switzerland*O. Zaharko **Laboratory for Neutron Scattering and Imaging, Paul Scherrer Institute, CH-5232 Villigen, Switzerland*

(Received 28 April 2021; revised 10 June 2021; accepted 7 July 2021; published 6 August 2021)

The crystal structure and magnetic correlations in triangular antiferromagnet FeGa₂S₄ are studied by x-ray diffraction, magnetic susceptibility, neutron diffraction, and neutron inelastic scattering. We report significant mixing at the cation sites and disentangle magnetic properties dominated by major and minor magnetic sites. The magnetic short-range correlations at 0.77 Å⁻¹ correspond to the major sites and being static at base temperature they evolve into dynamic correlations around 30–50 K. The minor sites contribute to the magnetic peak at 0.6 Å⁻¹, which vanishes at 5.5 K. Our analytical studies of triangular lattice models with bilinear and biquadratic terms provide the ratios between exchanges for the proposed ordering vectors. The modeling of the inelastic neutron spectrum within linear spin-wave theory results in the set of exchange couplings $J_1 = 1.7$, $J_2 = 0.9$, $J_3 = 0.8$ meV for the bilinear Heisenberg Hamiltonian. However, not all features of the excitation spectrum are explained with this model.

DOI: [10.1103/PhysRevB.104.064412](https://doi.org/10.1103/PhysRevB.104.064412)

*oksana.zaharko@psi.ch

I. INTRODUCTION

The interest in the MT_2X_4 family of compounds ($M = \text{Ni, Fe}$; $T = \text{Ga, Al}$; $X = \text{S, Se}$) arises due to the quasi-two-dimensional (2D) triangular geometry of the magnetic M sublattice. This family, especially NiGa_2S_4 , are strong candidates as an experimental realization of the triangular lattice antiferromagnet (TLAFM), the extensively studied theoretical model in frustrated magnetism. For the spin $S = 1/2$ TLAFM case a resonating valence bond spin liquid ground state was proposed by Anderson [1], which was later shown instead to have a classical-like 120° planar ground state [2] despite the quantum fluctuations that only reduce the value of the order parameter. For Ising spins, on the other hand, it has been shown that the first nearest-neighbor (J_1) Ising TLAFM model stays disordered even down to zero temperature. Additional exchange interactions spanning over the second (J_2) and third (J_3) nearest neighbors could enhance frustration and for certain combinations of the exchange parameters exotic ground states are predicted. For example, for $J_1/J_3 = -\frac{1}{3}$ or $J_1/J_2 = -\frac{1}{4}$ a skyrmion crystal multi- k state should be realized [3]. Such swirling configurations with topological properties are of interest for the fast emerging field of spintronics. MGa_2S_4 compounds with $M = \text{Ni, Fe}$ crystallize in the trigonal space-group $P\bar{3}m1$ [4]. All atoms are located on triangular layers, which generally could be stacked in the $A, B,$ or C fashion [Fig. 1(a)]. In MGa_2S_4 the sulfur layers stack in the $BCBC$ sequence providing octahedral and tetrahedral voids. The octahedral voids are occupied by the smaller M cations, and the tetrahedral voids by Ga [Fig. 1(b)]. The unit cell of MGa_2S_4 is terminated by an empty void layer. Our x-ray diffraction study detected significant mixed occupancies (inversion) of the cation sites which we associate with highly nontrivial magnetic behavior of the MGa_2S_4 series. This feature is one of the important outcomes of our paper. The published bulk properties [5–7] suggest stronger exchange couplings for FeGa_2S_4 (Fe^{2+} , $S = 2$) compared to NiGa_2S_4 (Ni^{2+} , $S = 1$), but the main observations remain very similar. The Curie-Weiss temperature is $\theta_{CW} = 160$ K for FeGa_2S_4 ($\theta_{CW} = 80$ K for the Ni analog) and there is a bifurcation between field-cooled (FC) and zero-field-cooled (ZFC) dc magnetic susceptibilities at $T_f(\text{Fe}) = 16$ K [$T_f(\text{Ni}) = 8\text{--}9$ K]. No long-range order has been detected so far for both systems, but an inelastic neutron scattering (INS) study [8] for NiGa_2S_4 reported incommensurate (ICM) quasielastic short-range magnetic correlations in the vicinity of $Q = (0.155, 0.155, 0)$ and spin waves propagating from this Q point up to 3.5 meV. The dynamic muon relaxation rates [7,9] show an anomaly at $T^*(\text{Fe}) = 33$ K [$T^*(\text{Ni}) = 10$ K] approaching correlation times $\tau_c(\text{Fe}) = 10^{-6}$ s [$\tau_c(\text{Ni}) = 10^{-7}$ s]. These processes are much slower than the timescale of exchange interaction (10^{-12} s) and the corresponding states are interpreted as a slowly fluctuating “spin gel.” Surprisingly, no anomaly at T_f was observed by ^{57}Fe Mössbauer, μSR , and magnetic specific heat C_M , whereas the T^* anomaly is not present in magnetic bulk properties [5,6]. The magnetic component of the specific-heat $C_M(T)$ has a double-peak structure for both compounds with a first maximum at 10 K for both and a second maximum at 60 K (100 K) for FeGa_2S_4 [5] (NiGa_2S_4

[10]). $C_M(T)$ has a T^2 dependence at low temperatures, which indicates gapless and linearly dispersive modes in 2D, and it is insensitive to magnetic fields up to 7 T. Our samples show the same magnetic behavior, and we complement experimental information on the FeGa_2S_4 system by neutron experiments both diffraction and inelastic scattering.

From the theoretical side a number of extensions to the TLAFM model were proposed to explain the observed magnetic behavior of the Ni and Fe analogs. A strong dominant third-nearest-neighbor antiferromagnetic exchange interaction is supported by density functional theory calculations [11] and could explain the ICM magnetic propagation vector of NiGa_2S_4 [8]. Biquadratic interactions, which would yield spin-nematic quadrupolar correlations, account for the double-peak structure in specific heat [12–14]. The origin of the spin nematic could be the coupling of magnetic correlations to phonons observed by Raman scattering [15]. The Z_2 vortex model with binding-unbinding transition [16] could also explain the high-temperature anomalies in magnetic properties, whereas linearly dispersing Halperin-Saslow modes in the absence of long-range magnetic order could elucidate the anomalous low-temperature properties [17]. We scrutinize the TLAFM model with $J_1, J_2,$ and J_3 bilinear exchanges and show that it is not sufficient to model our INS data. We associate the unconventional magnetic properties with the nonideal structure of the MGa_2S_4 family.

II. CRYSTAL STRUCTURE OF FeGa_2S_4 and NiGa_2S_4

A. Study of structure imperfection by x-ray diffraction

First we check thoroughly the crystal structure of our polycrystalline FeGa_2S_4 sample [18] analyzing synchrotron x-ray-diffraction powder pattern collected at 300 K. These data were well refined within the crystal structure published by Simiri *et al.* [4]: The Ga and two S atoms located at the $2(d)$ sites and Fe atoms at the $1(b)$ site of the $P\bar{3}m1$ space-group ($R_{\text{Bragg}} = 3.64\%$, $R_f = 1.99\%$, $\chi^2 = 47.3$). The fits became even better ($R_{\text{Bragg}} = 2.98\%$, $R_f = 1.89\%$, $\chi^2 = 46.2$) when the inversion between the Fe and the Ga atoms was introduced with the total occupancy constrained to the stoichiometric composition FeGa_2S_4 . According to this refinement the $1(b)$ site is occupied 20% by gallium and 80% by iron, whereas the $2(d)$ site is occupied by 10% iron and 90% gallium, respectively. As the model with partial inversion is only nominally better and a small amount of Ga_2O_3 impurity phase was detected in the powder pattern, we verified this result by x-ray diffraction on single crystals.

For several studied crystals (even very small ones) the shape of reflections was not exceptionally good—they had “tails” typical for small arbitrary rotations of macroscopic domains around the $[001]$ axis as can be seen in the reciprocal $hk0$ -layer reconstruction presented in Fig. 2 (top). Nevertheless, the consequent data reduction lead to good data with $R_{\text{int}} = 3.69\%$ for 520 unique reflections for the Laue group $\bar{3}m1$. A refinement assuming the nondisordered FeGa_2S_4 structure with full occupancies converged at acceptable R values: $R_1 = 2.83\%$, $wR_2 = 8.21\%$, $\text{GooF} = 1.184$ for 514 $F_o > 4 \sigma F_o$. The difference

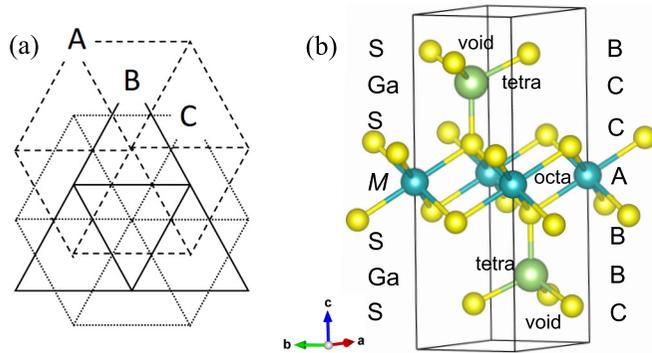


FIG. 1. (a) Projection of the A, B, C layers on the ab plane. (b) View on the $M\text{Ga}_2\text{S}_4$ unit cell with labeled (from left to right) sequence of S, Ga, and M atoms, coordination of the voids between the S layers and order of the A, B, C layers.

Fourier maps as in the case of the powder pattern contained relatively strong residual electron density peaks: positive at the $1(b)$ Fe site (corresponding to around $3 e/\text{\AA}^3$) and negative (corresponding to around $-1.7 e/\text{\AA}^3$) in the vicinity of the $2(d)$ Ga sites. Along with this no significant electron density occurred between the atomic positions of the ideal structure. The residual electron density could be accounted for by the partial inversion at the $1(b)$ and $2(d)$ sites. Refinement converged to 21.5(3)% Ga [and 78.4(3)% Fe] on the $1(b)$ Wyckoff position and 10.8(1)% Fe [and 89.2(1)% Ga] on the Wyckoff position $2(d)$ with improved figure of merit: $R_1 = 2.04\%$, $Rw_2 = 6.08\%$, $\text{GooF} = 1.367$.

We took the indication of partial inversion from x-ray diffraction with great caution. Bulk properties (magnetic susceptibility and specific heat) measured by us and by other groups are very similar suggesting that partial inver-

sion might improve the understanding of magnetic properties of the whole $M\text{Ga}_2\text{S}_4$ family. To clarify this, we synthesized and characterized isostructural NiGa_2S_4 . Refinement of NiGa_2S_4 single-crystal x-ray-diffraction data revealed the same degree of inversion as for FeGa_2S_4 . This complies with nuclear quadrupole resonance (NQR) studies of polycrystalline NiGa_2S_4 samples [19,20], which reported two Ga signals. Our results imply that these NQR signals could arise from gallium atoms located on two different crystallographic sites. We also considered whether other imperfections discussed in the literature could explain our diffraction data. For example, high-resolution electron microscopy detected the presence of the stacking faults along the $[001]$ direction [20]. Any significant fraction of stacking faults generated by a shift of the layers as realized, for example, in the case of the rhombohedral structure of MgAl_2S_4 or by introducing layers found in $\text{Fe}_2\text{Ga}_2\text{S}_5$ or in GaS with the hexagonal β -InSe structure, would lead to residual electron density off the atomic positions of the ideal structure. The same holds for the stacking faults along the slip planes $(11-20)$, $(10-11)$, and $(11-23)$, which sometimes occur in the hexagonal close-packing structures. Diffuse scattering should also be observed, but this is not the case in our diffraction patterns presented in Fig. 2, top. We also checked for twinning, finding no indication of twofold rotations around $[110]$, $[1-10]$, and $[001]$, the usual twin laws occurring in trigonal systems. Our scanning electron microscopy images clearly show that crystals consist of layers with a thickness on the micrometer scale, which are rotated against each other by small angles (Fig. 2, bottom). One more sample imperfection was reported by Nambu *et al.* [20] based on energy-dispersive x-ray spectroscopy (EDXS)—nonstoichiometry in the sulfur content. Our EDXS analysis shows no sulfur deficiency within the detection limit.

Thus, we conclude that polycrystalline and single-crystal $M\text{Ga}_2\text{S}_4$ samples have significant inversion on the cation sites. In the following text we correlate this partial inversion with magnetic bulk properties and neutron-scattering results, labeling the $1(b)$ site as the “major” site and the $2(d)$ site as the “minor” site since they are occupied by 80% and 10% with the magnetic ion, respectively.

B. Temperature evolution of the crystal structure

To identify possible changes to the crystal structure of FeGa_2S_4 we measured and refined synchrotron x-ray powder-diffraction patterns of a polycrystalline sample in the 5–300 K temperature range. The obtained temperature evolution of the lattice constants, atomic positions, and thermal parameters is presented in Fig. 3. No significant structural anomalies could be detected in these x-ray patterns. The lattice constants show a typical Debye thermal expansion, the slope of the ratio c/a changes below 50 K and near 10 K. The interatomic distances $d_{\text{FeS}2}$, $d_{\text{GaS}1}$ decrease, whereas $d_{\text{GaS}2}$ increases with lower temperature. The anisotropic thermal parameters of all atoms decrease very much alike, only the thermal parameters U_{11} and U_{33} of the $2(d)$ site decrease faster and slower, respectively.

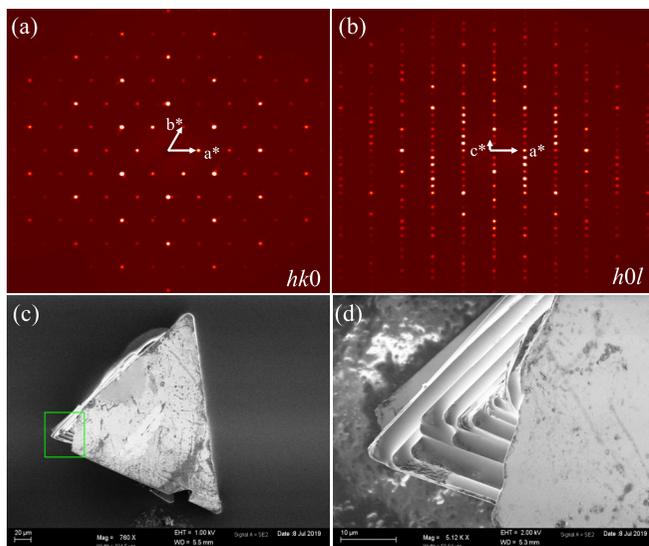


FIG. 2. Top: The $hk0$ (a) and $h0l$ (b) reciprocal layers reconstruction based on the x-ray single-crystal diffraction of FeGa_2S_4 . Bottom: (c) scanning electron microscopy image of a single crystal of FeGa_2S_4 and (d) zoom into its left marked corner.

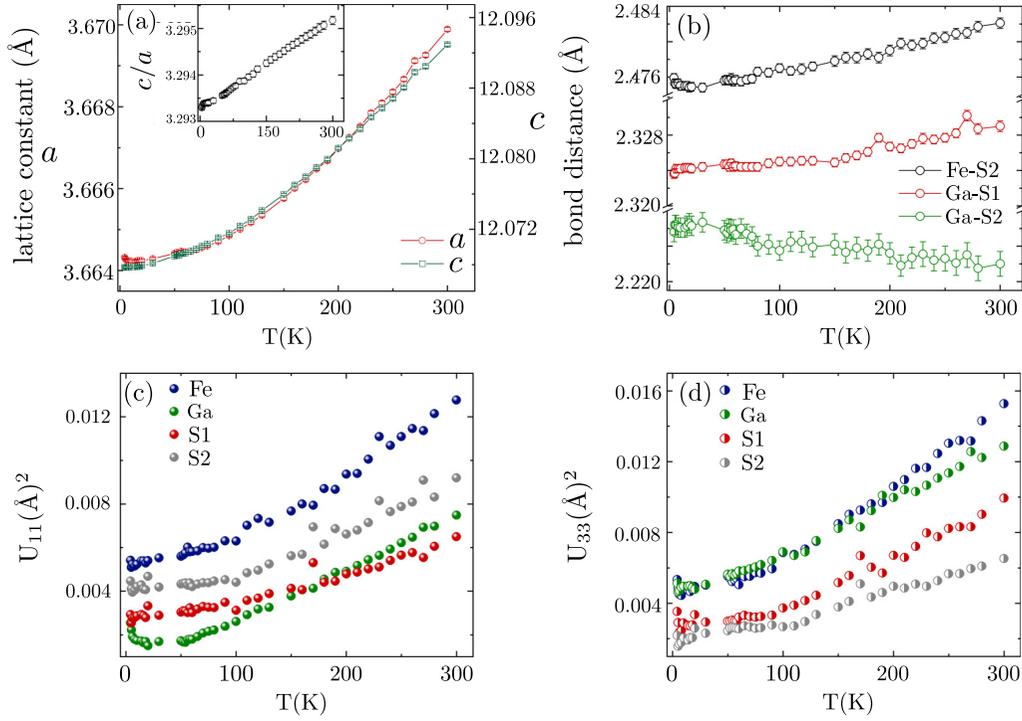


FIG. 3. Temperature evolution of the (a) lattice constants, (b) selected bond distances, and (c), (d) thermal parameters of FeGa_2S_4 from synchrotron x-ray powder diffraction.

These parameters of FeGa_2S_4 do not point to anomalies in vibrations of the sulfur atom S2 detected in the sister compound NiGa_2S_4 by Raman scattering [15].

change constant,

$$J/k_B = -\frac{3\Theta_{\text{CW}}}{zS(S+1)} \sim 13 \text{ K} \sim 1.1 \text{ meV},$$

III. MAGNETIC PROPERTIES

A. Magnetic bulk properties

We briefly report magnetic bulk properties of our FeGa_2S_4 samples. Figure 4 (left) presents the magnetic susceptibility of a FeGa_2S_4 single crystal measured at 0.1 T in the range of 1.8–350 K for the three principal orthogonal crystallographic directions: [001], [100], and $[-120]$. At high-temperatures (200–350 K) the curves almost overlap, and fits to the Curie-Weiss law yield antiferromagnetic Curie-Weiss temperatures $\Theta_{\text{CW}} = -165(11)$ K for the [001] direction and $-151(9)$ K for the [100] and $[-120]$ and effective magnetic moments $m_{\text{eff}} = 5.53\mu_B$ and $5.08\mu_B$, respectively. The susceptibility on the ab plane and along the c axis deviate below 200 K, and this anisotropy reaches 20% near 16 K. At $T_f = 16$ K the susceptibility has a kink and a bifurcation between the FC and the ZFC sample for all measured directions. The difference between the FC and the ZFC curves is tiny, $0.004 \mu_B/\text{Fe}$. Careful inspection of the derivative of χ (Fig. 4, right inset) reveals an additional change in the slope at 5.6 K. We associate it with long-range ordering of the minor Fe spins by powder neutron diffraction (PND) (see Sec. IV).

For our polycrystalline FeGa_2S_4 sample the Curie-Weiss temperature is $-158.0(9)$ K. This results in the effective ex-

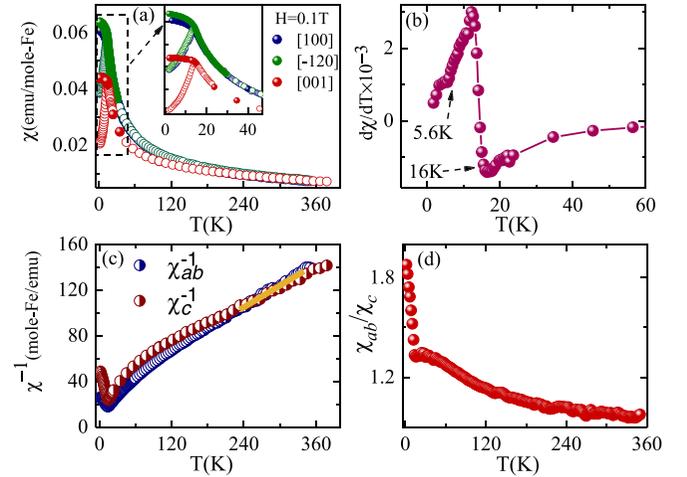


FIG. 4. (a) Magnetic susceptibility χ measured at 0.1 T on a single crystal of FeGa_2S_4 (mass $m = 2.87$ mg) along the three principal directions [100], $[-120]$, and [001]. ZFC and FC χ 's are plotted by empty and filled circles, respectively. The inset: zoom of the low-temperature region, (b) derivative of ZFC magnetic susceptibility highlighting deflection points. (c) Inverse susceptibility $1/\chi$ for $H \parallel [100]$ (blue) and $H \parallel [001]$ (red) and fit to the Curie-Weiss law in yellow. (d) The ratio of ZFC χ_{ab}/χ_c .

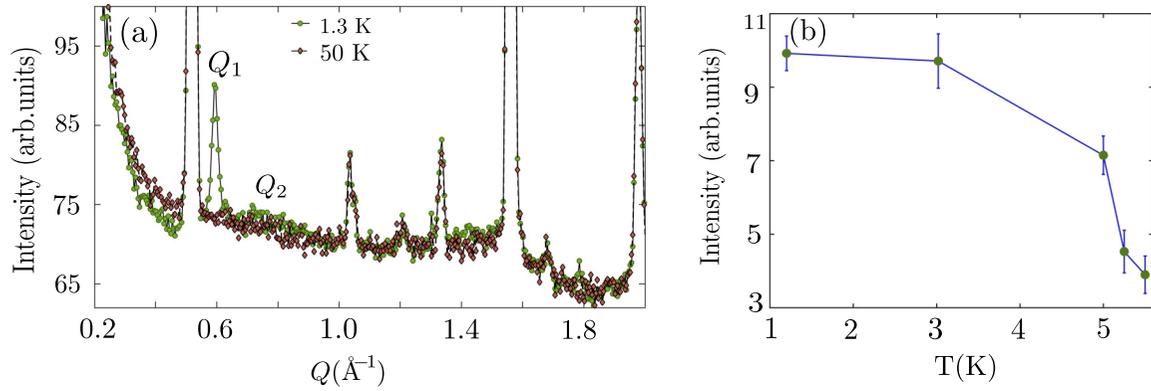


FIG. 5. Neutron-diffraction DMC patterns of FeGa_2S_4 at (a) 1.3 and 50 K. Temperature dependence of the magnetic peak at (b) $Q_1 = 0.6 \text{ \AA}^{-1}$.

here k_B is the Boltzmann constant, $z = 6$ is the coordination number, and $S = 2$ is the spin of the Fe^{2+} ions.

B. Magnetic static correlations from neutron diffraction

It is crucial to understand, if the magnetic properties of FeGa_2S_4 samples could be disentangled into major- and minor-site properties. First we address this question with PND.

In PND patterns collected on the cold neutron powder diffractometer (DMC) two different features of magnetic origin appear. Prominent in Fig. 5(a) is the peak at $Q_1 = 0.6 \text{ \AA}^{-1}$ below $T_N = 5.5 \text{ K}$. It could be indexed with the incommensurate propagation vector $\mathbf{k} = [0.1737(1), 0.1737(1)0]$ in analogy to $\mathbf{k} = (0.153, 0.1530)$ reported for NiGa_2S_4 . However, no long-range magnetic arrangement akin to only the major site reproduces the diffraction pattern. Models with Fe only on the 1(b) site require the second peak at $(0.1737, 0.1737, 1)$ with $Q = 0.79 \text{ \AA}^{-1}$ to have significant intensity. The single $(0.1737, 0.1737, 0)$ peak can be reproduced by a model with the Fe moments on the 2(d) site. The moments are sinusoidally modulated along the z axis. The moment amplitude $7.0(2)\mu_B/\text{Fe}$ (maximal value of the moment) would be, however, unreasonably large for the 10% occupied 2(d) site. So the M_z component on the minor 2(d) site is most probably significant but not the only “participant” in the magnetic ordering at $T_N = 5.5 \text{ K}$ and $Q_1 = 0.6 \text{ \AA}^{-1}$.

The second less evident feature in PND is diffuse magnetic scattering centered at $Q_2 = 0.77 \text{ \AA}^{-1}$ [Fig. 5(a)]. The XYZ-polarization analysis of powder neutron-diffraction patterns collected on D7 verifies that this is purely magnetic scattering (Fig. 6). In NiGa_2S_4 a similar diffuse bump was reported beneath the $\mathbf{k} = (0.153, 0.153, 0)$ magnetic peak (Fig. 4 in Ref. [10]), and it was interpreted in terms of two-dimensional (2D) correlations extending within $25(3) \text{ \AA}$. In the case of FeGa_2S_4 the diffuse feature is broader. To estimate the 2D correlation length we first used the Warren function [21] initially developed to describe scattered intensity from parallel equidistant layers randomly rotated along the normal direction. Modeling of the magnetic PND pattern presented in Fig. 6(a) suggests an in-plane correlation length of 10 \AA , which does not exceed the fourth nearest-neighbor Fe-Fe distance. As an alternative route, we used the RMC algorithm implemented in the SPINVERT program [22]. We fit the magnetic PND pattern to a

large array ($30 \times 30 \times 10$ unit cells) of spin vectors located on the major 1(b) sites [Fig. 6(b)]. The spin-pair correlation function in real space $\langle \mathbf{S}(0) \cdot \mathbf{S}(r) \rangle$ is calculated from the fitted spin configurations by the program SPINCORREL [22]. The negative sign of correlations for the in-plane distances $d_1^{1b} = 3.66$, $d_2^{1b} = 6.35$, $d_3^{1b} = 7.33 \text{ \AA}$ [three first points in the Fig. 6(b) inset] suggests antiparallel alignment of spins within a triangular layer. RMC runs with additional spins on the minor 2(d) sites did not improve the fit, so the minor spins are not decisive for the Q_2 feature.

We summarize our PND results as follows: long-range correlations resulting in the $Q_1 = 0.6 \text{ \AA}^{-1}$ peak arise mostly from the minor Fe spins, whereas the short-range correlations at $Q_2 = 0.77 \text{ \AA}^{-1}$ are magnetic in-plane correlations of the major Fe spins. To distinguish whether these are static or dynamic we turned to inelastic neutron scattering, presented below.

C. Magnetic dynamic correlations from inelastic neutron scattering

The excitation spectrum of polycrystalline FeGa_2S_4 was measured on the LET spectrometer [23]. Figure 7 displays the wide-ranging $S(Q, \omega)$ accessed with the $E_i = 24.3 \text{ meV}$ rep mode at 2 and 180 K. Two prominent INS features are evident. The first one is peaked at $Q_2 = 0.77 \text{ \AA}^{-1}$ and $E = 5 \text{ meV}$. It decreases towards the elastic line, suggesting that these might be gapped spin waves, but it is hard to identify the value of the anticipated gap and temperature of its softening even from the lower-energy $E_i = 7.7 \text{ meV}$ rep-mode spectrum [Fig. 7(d)]. The second, high-energy feature at 13 meV spans over the whole measured interval of $1 < Q < 6 \text{ \AA}^{-1}$. The low Q -part ($Q < 4.5 \text{ \AA}^{-1}$) reduces with temperature, thus, it has magnetic origin. The high- Q part ($Q > 4.5 \text{ \AA}^{-1}$) persists, so it has significant phonon contribution. These two features reside on a very broad background which remains even at 180 K, the highest temperature reached in the experiment.

The anticipated gap region for the first feature is magnified in the top panel of Fig. 8 where $S(Q, \omega)$ maps measured with the $E_i = 3.8 \text{ meV}$ rep mode at three representative temperatures 2, 38, and 60 K are presented. At 2 K the correlations are predominantly static. In Fig. 8(d) the counts summed within

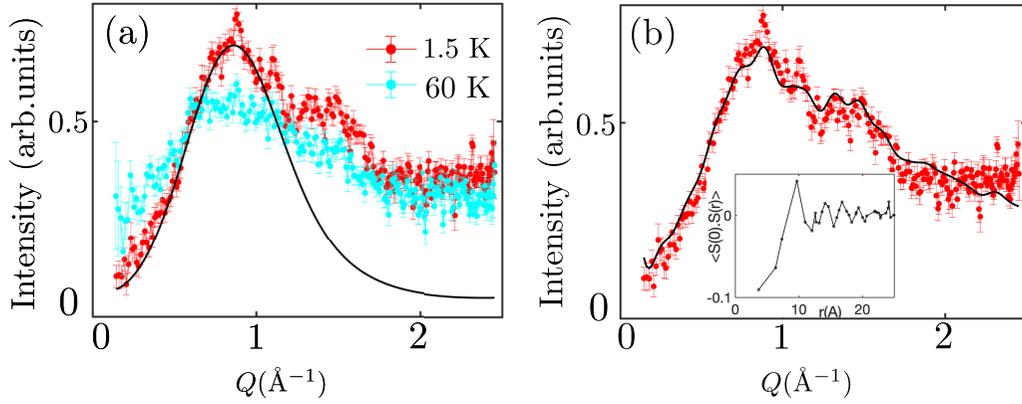


FIG. 6. Magnetic diffuse scattering measured at 1.5 K (red) and 60 K (cyan) on $D7$ ($E_i = 3.8$ meV) and fit to the Warren function (a) and calculated by the reverse Monte Carlo (RMC) method (b) with resulting radial spin-correlation function $\langle S(0) \cdot S(r) \rangle$ shown in the inset.

$0 < E_1 < 0.2$ meV are divided by a factor of 50 to match the scale of the intensity within the gap $0.2 < E_2 < 0.5$ meV and of the excitations above the gap $0.5 < E_2 < 3$ meV. Interestingly, at 2 K a weak dispersive feature starting from Q_1 could also be identified. At higher temperatures it is completely obscured by a continuum centered at $Q_2 = 0.77 \text{ \AA}^{-1}$. The continuum gains intensity in the 30–40 K region and is reduced with further increasing temperature.

It would be of interest to compare the temperature evolution of various static and dynamic correlations observed

on LET and in bulk magnetic measurements. Unfortunately the insufficient resolution does not allow to separate the Q_1 feature from the nearby nuclear peak Fig. 8(d). Therefore, we present the temperature dependence of the elastic intensity of the predominantly Q_2 feature summed within $0.6 < Q < 1 \text{ \AA}^{-1}$ in Fig. 8(e). It decreases sharply around 50 K. The two prominent INS signals centered at 5 and 13 meV, in contrast are maximal at 50 K. The 5 meV feature is integrated within the $E_i = 3.8$ meV setup, and this allows the documentation of the deflection point at 10 K (close to T_f).

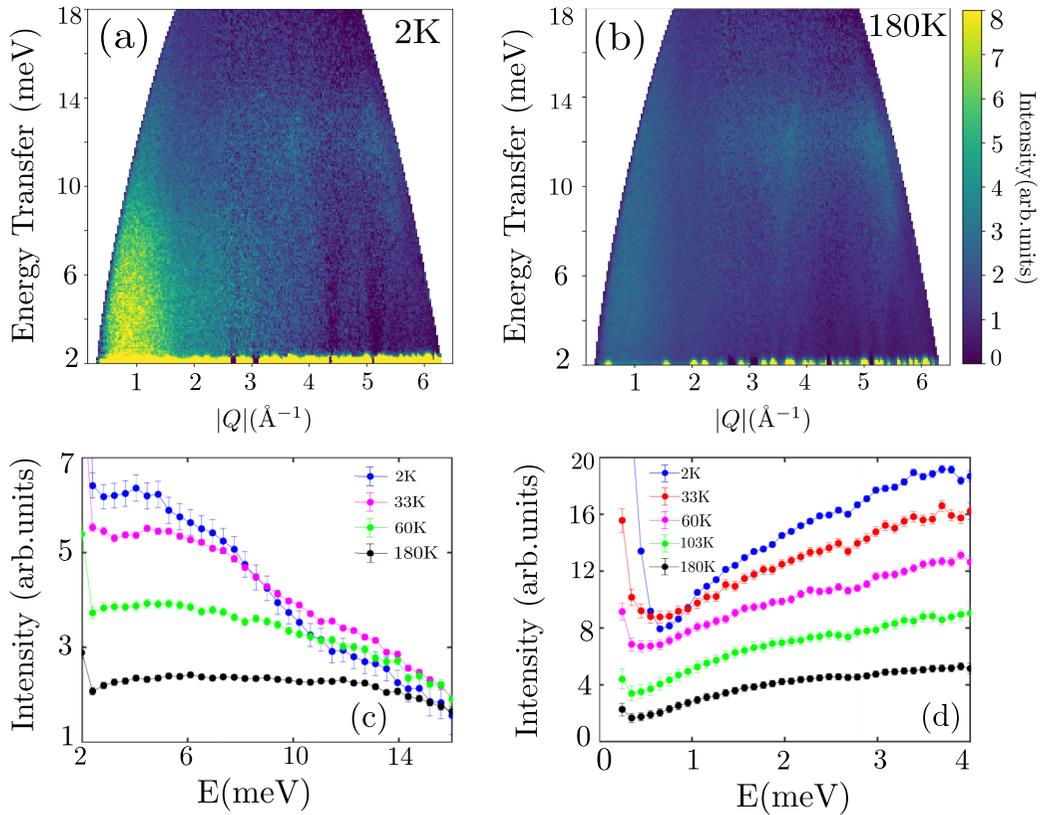


FIG. 7. Top: Excitation spectrum of FeGa_2S_4 measured on LET with $E_i = 24.3$ meV at the lowest (a) $T = 2$ K and the (b) highest 180 K temperatures. Bottom: Temperature evolution of the low- Q feature with the signal integrated over $Q = [0.3 \dots 1.5] \text{ \AA}^{-1}$ with the (c) $E_i = 24.3$ meV rep-mode ($\delta E_{0\text{meV}} = 1.15$ meV) and (d) over $Q = [0.4 \dots 0.8] \text{ \AA}^{-1}$, $E_i = 7.7$ meV ($\delta E_{0\text{meV}} = 0.22$ meV). The Al can was subtracted, and data were corrected for the Bose factor.

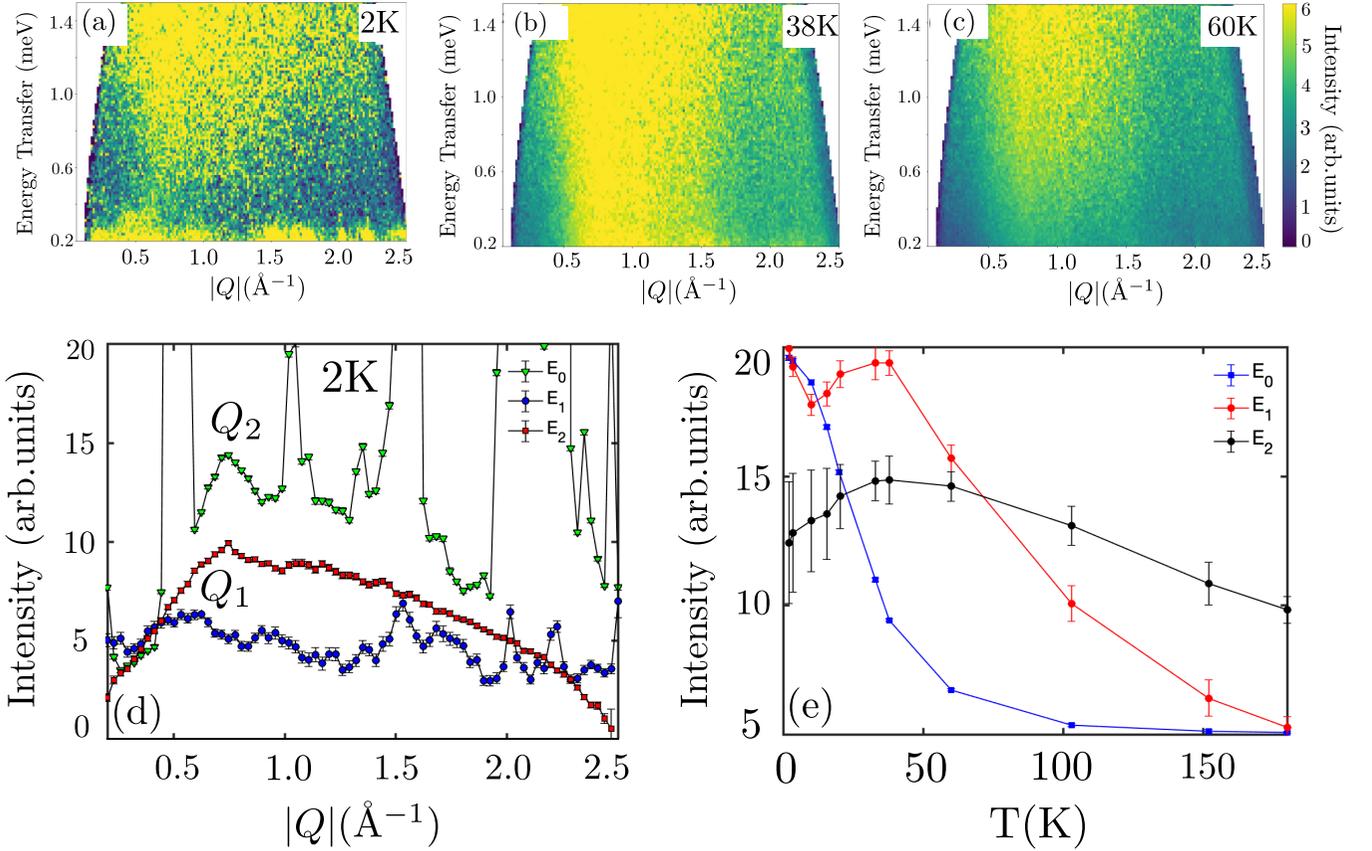


FIG. 8. Top: Part of the excitation spectrum of FeGa_2S_4 measured on LET with $E_i = 3.8$ meV ($\delta E_{0 \text{ meV}} = 0.1$ meV) at (a) $T = 2$ K, (b) 38 K, and (c) 60 K. Bottom: (d) 2 K elastic signal summed over $E_0 = [0 \cdots 0.2]$ meV (green symbols, signal divided by 50) and inelastic signals $E_1 = [0.2 \cdots 0.5]$ meV (blue symbols), $E_2 = [0.5 \cdots 3]$ meV (red symbols). (e) Temperature evolution of the elastic (blue squares) and inelastic (red and black circles) features. The elastic signal is integrated over $Q = [0.6 \cdots 1] \text{ \AA}^{-1}$ and $E_0 = [-0.1 \cdots 0.1]$ meV, the inelastic signals are corrected for the Bose factor and integrated over $Q = [0.44 \cdots 2] \text{ \AA}^{-1}$, $E_1 = [0.5 \cdots 2]$ meV and $Q = [0.3 \cdots 1.5] \text{ \AA}^{-1}$, $E_2 = [11 \cdots 13]$ meV. The last curve is extracted from the $E_i = 24.3$ meV rep mode.

The contribution of spin waves from $Q_1 = 0.6 \text{ \AA}^{-1}$ is minute in the collected INS signal and cannot be disentangled from the broad major feature centered at $Q_2 = 0.77 \text{ \AA}^{-1}$. The origin of the Q_2 feature evolves from static into dynamic with temperature increase and reaches maximum intensity at 50 K, which coincides with the broad maximum in the magnetic part of the specific heat [5]. We presume it originates from the major spins. In brief: The low-energy part of INS data is dominated by the (5 meV, 0.77 \AA^{-1}) feature, the high-energy part has a feature at 13 meV which is magnetic for $Q < 4.5 \text{ \AA}^{-1}$ and has a phonon contribution for $Q > 4.5 \text{ \AA}^{-1}$. The magnetic INS signal has maximum intensity at 50 K where the elastic short-range correlations diminish. The broad scattering background beneath these features persists even at 180 K.

IV. MODELING OF THE MAGNETIC HAMILTONIAN

We used several theoretical approaches to explain these variegated experimental observations. We start with the ideal triangular lattice and present analytical results for models with an increasing number of bilinear exchanges and with the bi-quadratic exchange (Sec. IV A). Then we test the model with three bilinear exchanges against our INS data (Sec. IV B).

A. Analytical results for models with bilinear and biquadratic exchanges

First, we try to establish the range of exchange parameters which could give rise to magnetic correlations observed at $Q_1 = 0.6 \text{ \AA}^{-1}$ for FeGa_2S_4 and 0.57 \AA^{-1} for NiGa_2S_4 [10] within the triangular lattice Heisenberg bilinear model. In this section we use the theoretical notation (TN) for the reciprocal space [see Appendix B for the definition of TN and its relation to the experimental notation (EN)].

We inspect analytically with rising complexity, the single $J_{i=1,3}$, the bilinear $J_{i=1,3} - J_{j=1,3}$ and the trilinear $J_1 - J_2 - J_3$ models on the two-dimensional triangular lattice described by the Hamiltonian,

$$H = J_1 \sum_{\langle i,j \rangle} (\mathbf{S}_i \cdot \mathbf{S}_j) + J_2 \sum_{\langle\langle i,j \rangle\rangle} (\mathbf{S}_i \cdot \mathbf{S}_j) + J_3 \sum_{\langle\langle\langle i,j \rangle\rangle\rangle} (\mathbf{S}_i \cdot \mathbf{S}_j). \quad (1)$$

Since we are interested in the region of the $J_1 - J_2 - J_3$ phase diagram with the incommensurately modulated ground states, we express the spin \mathbf{S}_i on site \mathbf{r}_i as [24]

$$\mathbf{S}_i = \mathbf{n}_1 \cos(\mathbf{k} \cdot \mathbf{r}_i) - \mathbf{n}_2 \sin(\mathbf{k} \cdot \mathbf{r}_i), \quad (2)$$

where \mathbf{n}_1 and \mathbf{n}_2 are orthonormal vectors. For the Hamiltonian in Eq. (1) we obtain the expression of the energy as a function

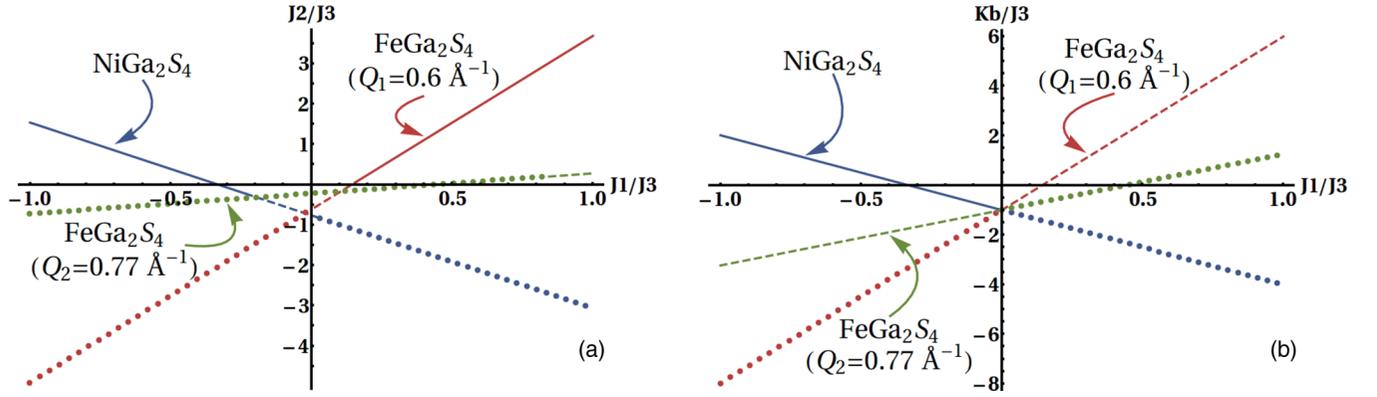


FIG. 9. The relation between (a) J_1/J_3 and J_2/J_3 and (b) J_1/J_3 and K_B/J_3 to obtain the ordering wave vectors for NiGa_2S_4 (blue) and FeGa_2S_4 (red and green) within the J_1 - J_2 - J_3 and J_1 - J_3 - K_B models. The critical points corresponding to a local maximum, a local minimum, and a global minimum of the energy at the given values of the ordering wave vectors are distinguished by the dotted, dashed, and solid lines, respectively.

of \mathbf{k} ,

$$E(\mathbf{k}) = 2J_1N \left[\cos(k_x) + 2 \cos\left(\frac{k_x}{2}\right) \cos\left(\frac{\sqrt{3}k_y}{2}\right) \right] + 2J_2N \left[2 \cos\left(\frac{3k_x}{2}\right) \cos\left(\frac{\sqrt{3}k_y}{2}\right) + \cos(\sqrt{3}k_y) \right] + 2J_3N [\cos(2k_x) + 2 \cos(k_x) \cos(\sqrt{3}k_y)]. \quad (3)$$

It is important to note that there is no explicit dependence of the energy on the vectors \mathbf{n}_1 and \mathbf{n}_2 , reflecting the $\text{SO}(3)$ global symmetry of the model. In order to find the possible ordering vectors we minimize $E(\mathbf{k})$ with respect to \mathbf{k} . Depending on the values of the parameters J_1 , J_2 and J_3 the minima of this model lie along the following two sets of directions: (i) $\pm(1, 0)$, $\pm(\frac{1}{2}, \frac{\sqrt{3}}{2})$, $\pm(-\frac{1}{2}, \frac{\sqrt{3}}{2})$ and (ii) $\pm(\frac{\sqrt{3}}{2}, \frac{1}{2})$, $\pm(0, 1)$, and $\pm(\frac{\sqrt{3}}{2}, \frac{1}{2})$. Since the ordering vector $\mathbf{k} \approx (\frac{1}{6}, \frac{1}{6}, 0)$ in EN observed in $M\text{Ga}_2\text{S}_4$ ($M = \text{Ni}, \text{Fe}$) corresponds to set (i), we focus on this direction and search for a minimum along the $\hat{\mathbf{x}}$ direction (or, equivalently, along any direction of this set). With this condition the value of k should satisfy,

$$\frac{J_1}{J_3} = -\frac{2[\sin(k) + \sin(2k)] + 3\frac{J_2}{J_3} \sin(\frac{3k}{2})}{\sin(\frac{k}{2}) + \sin(k)}. \quad (4)$$

From this equation we obtain linear relations among J_1 , J_2 and J_3 presented in Fig. 9(a). This linear relation expresses the values of the parameters for which the energy develops a critical point. The critical points gain stability when we move along each line, running from a local maximum (represented by dots) to a local minimum (dashed segment) and finally to a global minimum (solid line). For FeGa_2S_4 the Q_2 vector (green line) becomes a global minimum for $J_1/J_3 > 1.72$. Further restrictions on J_1/J_3 should be included for these critical points to belong in set (i): for NiGa_2S_4 $J_1/J_3 > -1$ and to obtain either the Q_1 or the Q_2 vectors for FeGa_2S_4 requires $J_1/J_3 < 0.6$ and $J_1/J_3 < 4.3$, respectively.

The sign of the slope for a modulated state with $k \approx 0.155 \times 4\pi$ for NiGa_2S_4 (blue) and with $k \approx 0.1737 \times 4\pi$ for

FeGa_2S_4 (red) is different. This change in the sign takes place at the critical wave-vector $\mathbf{k} = (\frac{1}{6}, \frac{1}{6}, 0)$.

It is important to note that the single $J_{i=1,3}$ —exchange models and the bilinear J_1 - J_2 and J_1 - J_3 exchange models are not sufficient to explain the $Q_1 = 0.6 \text{ \AA}^{-1}$ feature observed for FeGa_2S_4 . For example, the ordering vector $k \approx 0.155 \times 4\pi$ for NiGa_2S_4 can be obtained from the J_1 - J_3 model [25], and this is not the case for $k \approx 0.1737 \times 4\pi$ for FeGa_2S_4 . In those models the ordering vector implies either a uniform (ferromagnetic) state, a commensurate 120° structure or it does not match the direction [the set indicated in (i)] signaled by the experimental results. For the J_1 - J_2 - J_3 exchange model such solutions, however, are available.

Now we consider the ordering vector with the length $k \approx 0.222 \times 4\pi$, which could correspond to the center of the diffuse feature at $Q_2 = 0.77 \text{ \AA}^{-1}$ observed for FeGa_2S_4 . The parameters of the ideal triangular lattice model are related through a linear equation depicted in Fig. 9 by the green line. These solutions strongly differ from the Q_1 lines and require significant J_1 coupling.

We proceed with the “model engineering” and raise the complexity by adding the biquadratic interaction K_B between first nearest-neighbors $K_B \sum_{\langle i,j \rangle} (\mathbf{S}_i \cdot \mathbf{S}_j)^2$. We repeat the previous procedures for two models: J_1 - J_3 - K_B and J_1 - J_3 - K_B .

The energy of a modulated state for the J_1 - J_3 - K_B model reads

$$E(\mathbf{k}) = 2J_1N \left[\cos(k_x) + 2 \cos\left(\frac{k_x}{2}\right) \cos\left(\frac{\sqrt{3}k_y}{2}\right) \right] + 2J_3N [\cos(2k_x) + 2 \cos(k_x) \cos(\sqrt{3}k_y)] + 2K_B N [3 + \cos(2k_x) + 2 \cos(k_x) \cos(\sqrt{3}k_y)]. \quad (5)$$

As we did before we look for the minimum of the energy along the $\hat{\mathbf{x}}$ direction. With this condition the value of k should satisfy

$$\frac{J_1}{J_3} = -\frac{2\left(\frac{K_B}{J_3} + 1\right)[\sin(k) + \sin(2k)]}{\sin(\frac{k}{2}) + \sin(k)}. \quad (6)$$

From this equation we obtain the relations between the values of J_1 , J_3 , and K_B (Fig. 9) right for which modulated

states with $k \approx 0.155 \times 4\pi$ for NiGa_2S_4 , $k \approx 0.1737 \times 4\pi$, and $k \approx 0.222 \times 4\pi$ for FeGa_2S_4 are the ground states. The role of K_B is significant, but in the real system we expect K_B to be a perturbative and not the leading parameter.

Finally, if we add the J_2 exchange interaction to the previous model, the energy as a function of \mathbf{k} is as follows:

$$\begin{aligned}
 E(\mathbf{k}) = & 2J_1N \left[\cos(k_x) + 2 \cos\left(\frac{k_x}{2}\right) \cos\left(\frac{\sqrt{3}k_y}{2}\right) \right] \\
 & + 2J_2N \left[2 \cos\left(\frac{3k_x}{2}\right) \cos\left(\frac{\sqrt{3}k_y}{2}\right) + \cos(\sqrt{3}k_y) \right] \\
 & + 2J_3N [\cos(2k_x) + 2 \cos(k_x) \cos(\sqrt{3}k_y)] \\
 & + 2K_B N [3 + \cos(2k_x) + 2 \cos(k_x) \cos(\sqrt{3}k_y)]. \quad (7)
 \end{aligned}$$

Since we are interested in the states with \mathbf{k} along the $\hat{\mathbf{x}}$ direction, we look for the minimum of the energy along this direction. With this condition the value of k should satisfy

$$\frac{J_1}{J_3} = \frac{2\left(\frac{K_B}{J_3} + 1\right) [\sin(k) + \sin(2k)] + 3\frac{J_2}{J_3} \sin\left(\frac{3k}{2}\right)}{\sin\left(\frac{k}{2}\right) + \sin(k)}. \quad (8)$$

From this linear equation the values of J_1 , J_2 , and K_B for which the ICM ground states with $k \approx 0.155 \times 4\pi$, $k \approx 0.1737 \times 4\pi$, and $k \approx 0.222 \times 4\pi$ are obtained.

Our analytical approach shows that the parameter space of the ideal triangular model which fits the experimental ordering wave vectors is quite extended, however, constrained by Eq. (8), and additional input is necessary to select the unique set of exchange parameters. Despite the broad range of parameters, we emphasize on the relevance of the constraints imposed by Eqs. (4), (6), and (8) for searching the correct set of couplings.

B. Extraction of exchange parameters from the INS spectrum using linear spin-wave theory

We narrow the exchange parameter space calculating the spin excitation spectrum and fitting it to the experimental $S(Q, \omega)$. We consider the triangular lattice Heisenberg bilinear model of Eq. (1) and focus on the $Q_2 = 0.77 \text{ \AA}^{-1}$ feature observed in the INS spectra assuming that it emerges from the spin waves. We take the 180 K data after the Bose factor correction as an empirical background (even though it contains a featureless magnetic contribution) and attribute the rest of the 2 K data to spin-wave excitations. Using the ground state of Eq. (3), we calculate spin-wave excitations with the SPINW program [26] and compare the resulting spectra with the INS data measured at 2 K. To avoid regions in data that are saturated by elastic scattering, only energy transfers above 2.4 and 0.75 meV are considered for the two setups of $E_i = 24.3$ and $E_i = 7.7$ meV, respectively. In the simulation, the experimental energy resolution of each setup is approximated by a constant corresponding to its nominal (energy-dependent) value at the peak of the magnetic excitation. No intrinsic broadening is considered. The nominal uncertainties on the measured intensity are obtained from the data itself and are assumed to be underestimated for bins with low neutron counts. Therefore, these uncertainties are thresholded to a minimum value determined by the actual

variance across low-intensity bins in regions of data without large-scale features. The model is evaluated on a discretized grid of values ranging from -2 to 2 meV in increments of 0.1 meV for each of exchange parameters J_1, J_2, J_3 . Figure 10 shows the maximum logarithm likelihood at each point after optimizing the magnitude of the spin-wave contributions. The maximum logarithm likelihood suggests that J_1, J_2 and J_3 are antiferromagnetic. The best fit (see Fig. 11) is obtained for $J_1 = 1.7$, $J_2 = 0.9$, $J_3 = 0.8$ meV, which is consistent with the relation imposed by Eq. (4).

We note that the general locations of the observed excitations can be approximately reproduced by this model, however, the detailed structure of the simulated spin waves is not evident in the data, and this set of parameters is out the range indicated in Fig. 9(a). In particular, the $E_i = 7.7$ meV setup reveals that the predicted drop in intensity at the low-energy transfer is less rapid than what can be observed in data. These discrepancies are not removed by inclusion of the single-ion anisotropy $D_n \sum_i (S_i)^2$, which should be 20% of exchange and planar according to the magnetic susceptibility measurements.

We conclude that the best fit to our powder INS data provides the set of exchange parameters within the J_1 - J_2 - J_3 bilinear model but this model is not sufficient to explain the whole observed excitation spectrum.

V. SUMMARY AND DISCUSSION

Our extensive experimental study of the triangular antiferromagnet FeGa_2S_4 implies that this material, and most probably also NiGa_2S_4 , has significant mixing of the M ($M = \text{Ni, Fe}$) and Ga cations between the octahedrally coordinated $1(b)$ and tetrahedrally coordinated $2(d)$ positions. Nearly 20% of the $1(b)$ sites forming magnetic triangular layers are occupied by nonmagnetic ions and nearly 10% of the $2(d)$ sites forming nonmagnetic triangular layers host magnetic M ions.

This mixing is an important ingredient of highly nontrivial magnetic properties. It introduces a long-range magnetic order at $T_N = 5.5$ K revealed by the $Q_1 = 0.6 \text{ \AA}^{-1}$ peak in neutron powder diffraction, which we associated with the $\mathbf{k} = [0.1737(1), 0.1737(1), 0]$ propagation vector. This magnetic order is dominated by the amplitude modulated z component of the minor Fe spins at the $2(d)$ sites. The amount of the minor Fe ions are well below the percolation limit of the stacked triangular antiferromagnetic lattice ($p_c^{\text{side}} = 0.26240(5)$ [27]), so the layers of the major Fe ions possibly mediate this exchange.

The broad feature at $Q_2 = 0.77 \text{ \AA}^{-1}$ in neutron powder diffraction corresponds to short-range magnetic correlations within the triangular layers of the major Fe sites. These in-plane correlations are static at low temperatures, evolve into dynamic correlations at elevated temperatures 30–50 K, and fade away at temperatures comparable to $|\Theta|_{\text{cw}} = 160$ K. These dynamic correlations could be confined spin waves, the so-called Halperin-Saslow modes [17,28] of the major Fe moments, which freeze in due to numerous nonmagnetic impurities. The nonmagnetic defects possibly trigger formation-dissociation of the Z_2 vortices. According to the MC simulations [29] the characteristic temperature T_{KM} related to the pairing dissociation of the Z_2 vortices is correlated

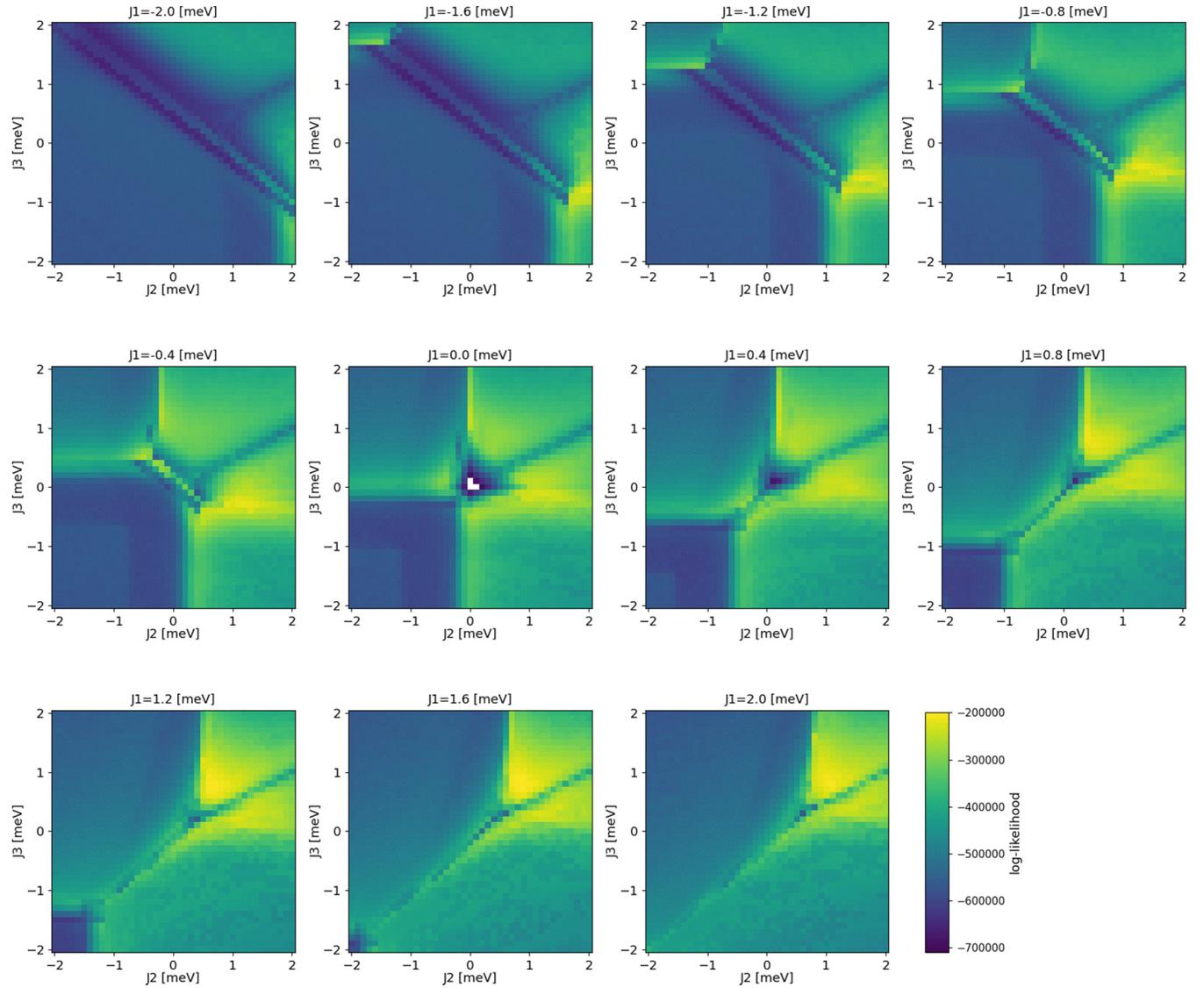


FIG. 10. Maximum logarithm likelihood after optimizing the magnitude of the spin-wave contributions.

with the effective exchange as $T_{KM} = 0.66JS^2$. For our case $J = 13$ K (estimated from susceptibility) and $S = 2$, which this results in $T_{KM} = 34$ K. This temperature corresponds to the anomalies found in muon spectroscopy ($T^* = 33$ K) [7,9] and to the change between static and dynamic natures of magnetic short-range correlations in our neutron scattering. Thus, even if the $M\text{Ga}_2\text{S}_4$ family is not an ideal TLA FM system, it might realize interesting phenomena predicted theoretically for this model.

Our extensive theoretical study of the ideal triangular lattice bilinear-biquadratic Heisenberg model has value by itself. The analytical study provided in Sec. IV A could be applied to a generic triangular system and as such serves as guide to study other compounds. It rationalizes the ratios J_1/J_3 , J_2/J_3 , and K_B/J_3 for a provided ground-state propagation vector. For the specific case of FeGa_2S_4 it notifies that the Q_1 and Q_2 features require possibly different sets of exchange parameters as they reside on the lines with one intercept point. We reduce the range of possible exchange parameters for FeGa_2S_4 by modeling the distinct features of

the experimental low-temperature INS spectra as conventional spin waves within the J_1 - J_2 - J_3 bilinear Hamiltonian. The best fit is obtained for the set of AF couplings $J_1 = 1.7$, $J_2 = 0.9$, $J_3 = 0.8$ meV, which is close to the analytical solutions for Q_2 . However, only the gross features of the INS spectra are explained. The origin of the broad scattering background remains elusive, and for its understanding it is important to disentangle magnetic properties of inversion-free and inversion-containing triangular antiferromagnetic materials.

Our results imply that the short-range correlations at Q_2 and the anomalies around 30–50 K are the properties of the major magnetic sites of the FeGa_2S_4 system. The main exchange couplings are antiferromagnetic and $J_1 > J_3 \approx J_2$. How strongly the behavior of major Fe triangular sublattice is influenced by the minor Fe sites remains unclear. Theoretical predictions are presently limited to only small amounts of impurities and to the first nearest neighbors [30,31]. Extensions to the experimentally found values can bring answers to this question. Preliminary Monte Carlo simulations with the experimentally observed amount of impurity seem to

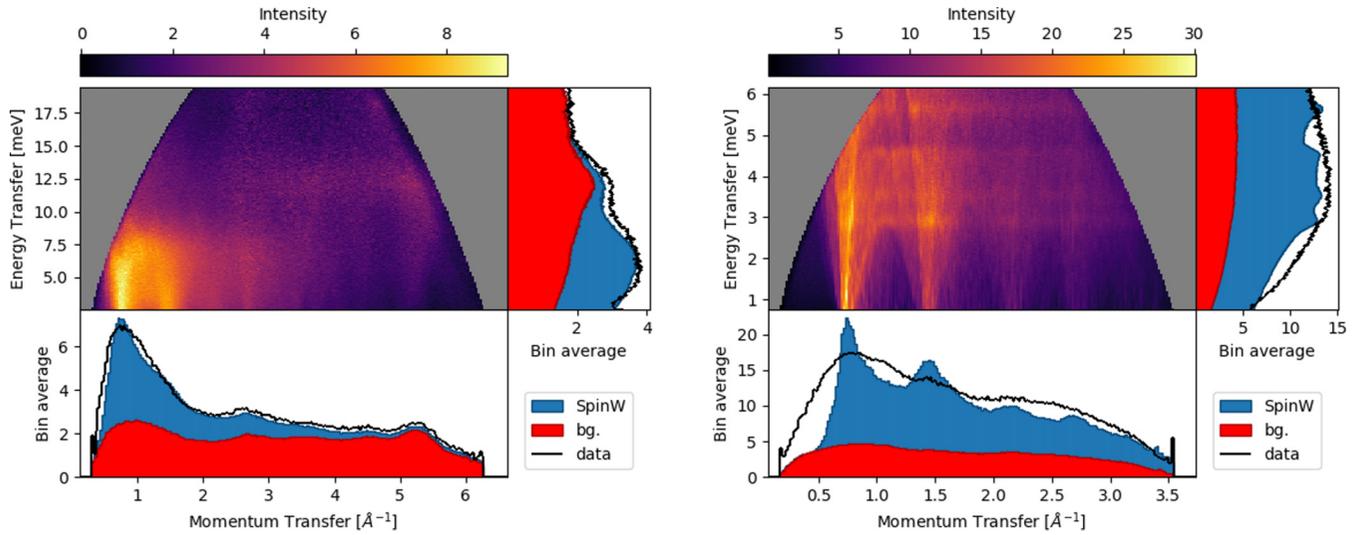


FIG. 11. Predicted $E_i = 24.3$ meV (left) and $E_i = 7.7$ meV (right) INS spectra at 2 K, constructed from an empirical background model measured at 180 K and spin-wave simulations for the set of the exchange values $J_1 = 1.7$, $J_2 = 0.9$, $J_3 = 0.8$ meV. The margin plots show comparisons with data measured at 2 K.

reproduce the Q_1 and Q_2 features observed in inelastic neutron scattering. However further exploration would be necessary. Novel synthetic routes to obtain inversion free members of the MGa_2S_4 family could in the future facilitate experimental validation of the ideal TLAFM model.

ACKNOWLEDGMENTS

This work was performed at SINQ, Paul Scherrer Institute, Villigen, Switzerland with financial support from the Swiss National Science Foundation (Grant No. 200020-182536) and Centro Lanitoamericano-Suizo (Seed money Grant No. SMG1811) and the Swiss Data Science Center (Project No. BISTOM C17-12). We acknowledge F. Krumeich for recording scanning electron microscopy (SEM) images and EDXS analysis.

APPENDIX A: MATERIALS AND METHODS

Polycrystalline $FeGa_2S_4$ and $NiGa_2S_4$ samples were prepared by solid-state synthesis from FeS (NiS) and GaS starting materials. The mixture was annealed for 1 week at 900 °C in an evacuated quartz ampule. Then the sample was homogenized by grinding, resealed, annealed again, and cooled within 24 h. Single crystals were grown by the chemical-vapor transport method using iodine as a transport agent and a temperature gradient 1000/900 °C. The crystals were then quenched.

The purity of the samples and the details of the crystal structure for $FeGa_2S_4$ in the temperature range of 5–300 K were determined for polycrystalline material on the x-ray powder diffractometer of the X04SA Material Science beamline at the Swiss Light Source synchrotron ($\lambda = 0.641090$ Å) and for $FeGa_2S_4$ and $NiGa_2S_4$ single crystals on a Bruker SMART diffractometer equipped with an Apex I detector

and an Apex II detector ($Mo K\alpha = 0.71073$ Å) at ETH Zürich at 300 and 100 K, respectively. Cambridge Crystallographic Data Center (CSD) 2078453 and CSD 2078454 contain the Supplemental crystallographic data for $FeGa_2S_4$ and $NiGa_2S_4$, respectively. These data can be obtained free of charge from FIZ Karlsruhe via Ref. [32]. Powder patterns were refined using the FULLPROF suite [33] for single-crystal refinements SHELX [34] was used. SEM images of the as-obtained samples were recorded with a secondary electron detector on a Gemini 1530 (Zeiss) microscope. EDXS was performed with a solid-state drive system (Noran) attached to this microscope.

Magnetic susceptibility was measured in the temperature range of 1.8–350 K in an applied magnetic field of 0.1 T using a magnetic properties measurement system superconducting quantum interference device magnetometer, Quantum Design.

Neutron powder diffraction patterns for $FeGa_2S_4$ were measured on the DMC diffractometer at SINQ ($\lambda = 2.4575$ Å). Data were collected at several temperatures between 1.3 and 180 K with the measuring time up to 12 h per pattern. XYZ-polarized neutron powder diffuse scattering was measured on the D7 spectrometer at ILL ($E_i = 3.8$ meV) at 1.4 K (4 h) and 60 K (10 h). The magnetic scattering was extracted from isotropic magnetic scattering the magnetic, $(\frac{d\sigma}{d\Omega})_{mag}$ the incoherent $(\frac{d\sigma}{d\Omega})_{inc}$, and the nuclear $(\frac{d\sigma}{d\Omega})_{nuc}$ cross sections were evaluated by the following equations [35]:

$$\left(\frac{d\sigma}{d\Omega}\right)_{mag} = 2\left(\frac{d\sigma}{d\Omega}\right)_{sf}^x + 2\left(\frac{d\sigma}{d\Omega}\right)_{sf}^y - 4\left(\frac{d\sigma}{d\Omega}\right)_{sf}^z, \quad (A1)$$

where x , y , z refer to the direction of the incident polarization, sf and nsf stand for spin flip and nonspin flip.

Time-of-flight inelastic neutron scattering (INS) was measured for $FeGa_2S_4$ on the LET spectrometer [23] at ISIS.

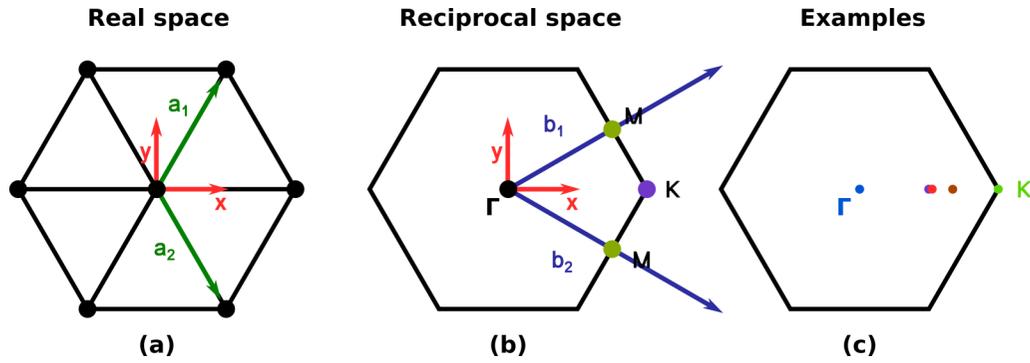


FIG. 12. The red arrows represent the \hat{x} and \hat{y} unit vectors in all the cases. (a) Basis vectors $\{\mathbf{a}_1, \mathbf{a}_2\}$ (in green) for the real space of the triangular lattice. (b) The first Brillouin zone for the triangular lattice. The M point (green circles), K point (purple circle), and Γ point (black circle). The blue arrows represent the basis vectors \mathbf{b}_1 and \mathbf{b}_2 in the reciprocal space. (c) Some examples of interest from the Γ point $(0, 0, 0)$ in light blue to the K point $(\frac{1}{3}, \frac{1}{3}, 0)$ in light green we have the points (expressed in EN): $(\frac{1}{6}, \frac{1}{6}, 0)$ in purple, $(0.1737, 0.1737, 0)$ in red, and $(0.222, 0.222, 0)$ in brown.

We used the rep-rate multiplication mode with the Fermi chopper rotating at 240 Hz in the high-flux setup, which allowed in a single time frame to collect data from incident neutron energies of 1.5, 2.24, 3.38, 7.7, and 24.3 meV. The Al can was subtracted, and data were corrected for the Bose factor.

APPENDIX B: CONVENTIONS AND NOTATIONS FOR THE RECIPROCAL SPACE

Two different notations can be encountered in the literature depending on the type of article (experimental or pure theoretical). We distinguish them by the names EN and TN.

In the EN notation a vector \mathbf{k} in the reciprocal space is expressed in terms of the basis vectors \mathbf{b}_1 and \mathbf{b}_2 as follows $\mathbf{k} = k_1\mathbf{b}_1 + k_2\mathbf{b}_2$. In the TN notation a vector \mathbf{k} is expressed in terms of the basis vectors \hat{x} and \hat{y} as follows $\mathbf{k} = k_x\hat{x} + k_y\hat{y}$ (see Fig. 12). The connection between both notations is given by a change in basis (from $\{\mathbf{b}_1, \mathbf{b}_2\}$ to $\{\hat{x}, \hat{y}\}$). The basis vectors \mathbf{b}_1 and \mathbf{b}_2 (in blue) are expressed in terms of the vectors

\hat{x} and \hat{y} (in red) as follows:

$$\mathbf{b}_1 = \frac{2\pi}{a}\hat{x} + \frac{2\pi}{\sqrt{3}a}\hat{y}, \quad (\text{B1})$$

$$\mathbf{b}_2 = \frac{2\pi}{a}\hat{x} - \frac{2\pi}{\sqrt{3}a}\hat{y}. \quad (\text{B2})$$

So, for instance, in EN the state $(\frac{1}{3}, \frac{1}{3}, 0)$ (the K point) corresponds to the triplet $(\frac{4\pi}{3a}, 0, 0)$ in TN,

$$\frac{1}{3}\mathbf{b}_1 + \frac{1}{3}\mathbf{b}_2 = \frac{4\pi}{3}\hat{x}. \quad (\text{B3})$$

The M point in EN is identified with $(\frac{1}{2}, 0, 0)$ and in the TN with the triplet $(\frac{\pi}{a}, \frac{\pi}{\sqrt{3}a}, 0)$,

$$\frac{1}{2}\mathbf{b}_1 = \frac{\pi}{a}\hat{x} + \frac{\pi}{\sqrt{3}a}\hat{y}. \quad (\text{B4})$$

Thus, when in the EN notation we refer to the $(0.155, 0.155)$ wave vector, it corresponds to the wave-vector $k \approx 0.155 \times 4\pi$ in the TN notation (taking $a = 1$).

-
- [1] P. W. Anderson, *Mater. Res. Bull.* **8**, 153 (1973).
 [2] T. Jolicoeur, E. Dagotto, R. Gagliano, and S. Bacci, *Phys. Rev. B* **42**, 4800(R) (1990).
 [3] T. Okubo, S. Chung, and H. Kawamura, *Phys. Rev. Lett.* **108**, 017206 (2012).
 [4] L. D. Smiri, N. H. Dung, and M. P. Pardo, *Mater. Res. Bull.* **15**, 861 (1980).
 [5] S. Nakatsuji, H. Tonomura, K. Onuma, Y. Nambu, O. Sakai, Y. Maeno, R. T. Macaluso, and J. Y. Chan, *Phys. Rev. Lett.* **99**, 157203 (2007).
 [6] B. R. Myoung, S. J. Kim, and C. S. Kim, *J. Korean Phys. Soc.* **53**, 750 (2008).
 [7] S. Zhao, P. Dalmas de Réotier, A. Yaouanc, D. E. MacLaughlin, J. M. Mackie, O. O. Bernal, Y. Nambu, T. Higo, and S. Nakatsuji, *Phys. Rev. B* **86**, 064435 (2012).
 [8] C. Stock, S. Jonas, C. Broholm, S. Nakatsuji, Y. Nambu, K. Onuma, Y. Maeno, and J. H. Chung, *Phys. Rev. Lett.* **105**, 037402 (2010).
 [9] P. Dalmas de Réotier, A. Yaouanc, D. E. MacLaughlin, S. Zhao, T. Higo, S. Nakatsuji, Y. Nambu, C. Marin, G. Lapertot, A. Amato, and C. Baines, *Phys. Rev. B* **85**, 140407(R) (2012).
 [10] S. Nakatsuji, Y. Nambu, H. Tonomura, O. Sakai, S. Jonas, C. Broholm, H. Tsunetsugu, Y. Qiu, and Y. Maeno, *Science* **309**, 1697 (2005).
 [11] I. I. Mazin, *Phys. Rev. B* **76**, 140406(R) (2007).
 [12] H. Tsunetsugu and M. Arikawa, *J. Phys. Soc. Jpn.* **75**, 083701 (2006).
 [13] A. Läuchli, F. Mila, and K. Penc, *Phys. Rev. Lett.* **97**, 087205 (2006).
 [14] S. Bhattacharjee, V. B. Shenoy, and T. Senthil, *Phys. Rev. B* **74**, 092406 (2006).
 [15] M. E. Valentine, T. Higo, Y. Nambu, D. Chaudhuri, J. Wen, C. Broholm, S. Nakatsuji, and N. Drichko, *Phys. Rev. Lett.* **125**, 197201 (2020).
 [16] H. Tsunetsugu and M. Arikawa, *J. Phys.: Condens. Matter* **19**, 145248 (2007).

- [17] D. Podolsky and Y. B. Kim, *Phys. Rev. B* **79**, 140402(R) (2009).
- [18] Details of sample preparation and experimental setups are documented in Appendix A.
- [19] H. Takeya, K. Ishida, K. Kitagawa, Y. Ihara, K. Onuma, Y. Maeno, Y. Nambu, S. Nakatsuji, D. E. MacLaughlin, A. Koda, and R. Kadono, *Phys. Rev. B* **77**, 054429 (2008).
- [20] Y. Nambu, R. T. Macaluso, T. Higo, K. Ishida, and S. Nakatsuji, *Phys. Rev. B* **79**, 214108 (2009).
- [21] B. E. Warren, *Phys. Rev.* **59**, 693 (1941).
- [22] J. A. M. Paddison, J. R. Stewart, and A. L. Goodwin, *J. Phys.: Condens. Matter* **25**, 454220 (2013).
- [23] R. I. Bewley, J. W. Taylor, and S. M. Bennington, *Nucl. Instrum. Methods Phys. Res. Sect. A* **637**, 128 (2011).
- [24] R. Tamura and N. Kawashima, *J. Phys. Soc. Jpn.* **77**, 103002 (2008).
- [25] R. Tamura and N. Kawashima, *J. Phys. Soc. Jpn.* **80**, 074008 (2011).
- [26] <https://spinw.org>.
- [27] K. J. Schrenk, N. A. M. Araújo, and H. J. Herrmann, *Phys. Rev. E* **87**, 032123 (2013).
- [28] B. I. Halperin and W. M. Saslow, *Phys. Rev. B* **16**, 2154 (1977).
- [29] Y. Ajiro, H. Kikuchi, S. Sugiyama, T. Nakashima, S. Shamoto, N. Nakayama, M. Kiyama, N. Yamamoto, and Y. Oka, *J. Phys. Soc. Jpn.* **57**, 2268 (1988).
- [30] A. Wollny, L. Fritz, and M. Vojta, *Phys. Rev. Lett.* **107**, 137204 (2011).
- [31] V. S. Maryasin and M. E. Zhitomirsky, *Phys. Rev. Lett.* **111**, 247201 (2013).
- [32] www.ccdc.cam.ac.uk/structures.
- [33] J. Rodríguez-Carvajal, *Physica B* **192**, 55 (1993).
- [34] G. M. Sheldrick, *Acta Crystallogr., Sect. C: Struct. Chem.* **71**, 3 (2015).
- [35] J. R. Stewart, P. P. Deen, K. H. Andersen, H. Schober, J. F. Barthelemy, J. M. Hillier, A. P. Mjurani, T. Hayes, and B. Lindenau, *J. Appl. Crystallogr.* **42**, 69 (2009).