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Article

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# Small and wide angle x-ray scattering studies of liquid-liquid phase separation in silicate melts.

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## Abstract

Incongruent liquid-liquid phase separation is a common phenomenon in molten oxides, but there are few structural studies due to the high temperatures involved ca. >1600°C. Here we present a high-energy x-ray combined small/wide angle scattering (SAXS/WAXS) method that can directly probe non-equilibrium phase diagrams. The Porod exponent in the SAXS signal is extracted, which measures the roughness of the interface formed between different phases. Problematic volatilization of silica in Al<sub>2</sub>O<sub>3</sub>-, CaO-, and MgO-bearing silica-rich liquids were minimized using levitation, laser heating and rapid time-resolved measurements (lasting tens of seconds), to probe the kinetics of the phase separation process. The WAXS measurement simultaneously probes the local atomic structure of the liquid state and shows that the primary structural changes are associated with the SiO<sub>2</sub> network. Cation coordination numbers extracted from pair distribution functions support the model that the origin of phase separation in binary silicate systems is due to Coulombic repulsions between poorly screened cations. For CaO-SiO<sub>2</sub>, the liquid-liquid phase separation is found to correlate with a pause in the temperature dependent atomic disorder associated with SiO<sub>4</sub> tetrahedra.

**Keywords:** silicate liquids, liquid-liquid, phase separation, x-ray diffraction, pair distribution function, aerodynamic levitation.

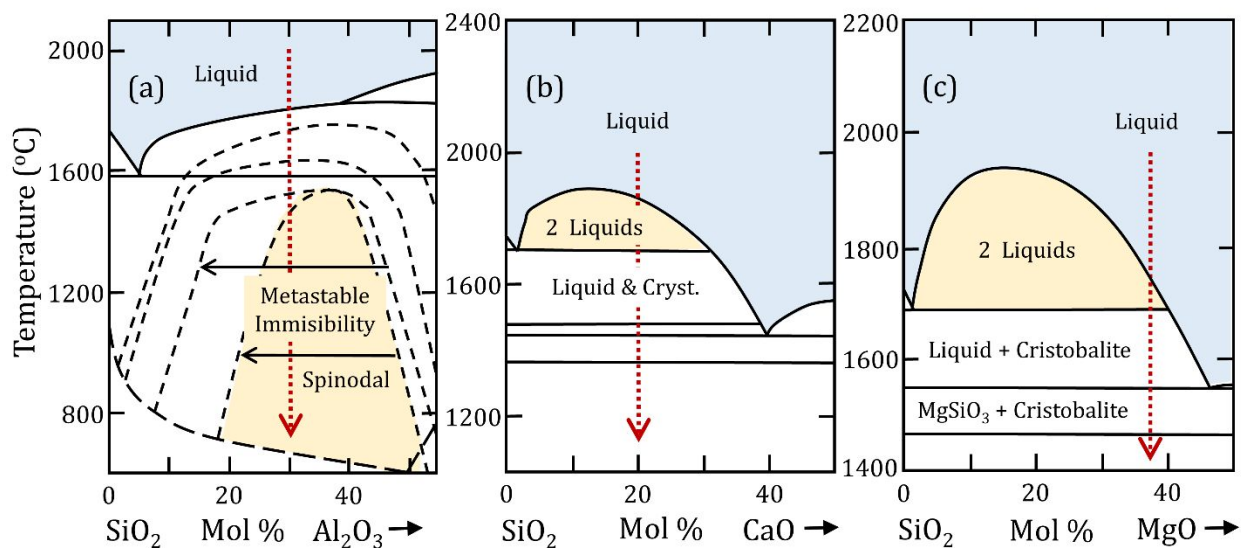
## Introduction

Calcium-Magnesium-Aluminum-Silicate (CMAS) liquids formed in the early stages of the Earth and Moon, and their structure-related properties strongly influenced the evolution of these planetary bodies<sup>1</sup>. Binaries from the CMAS model system contain major crystal and mantle minerals, e.g. quartz, forsterite, anorthite, pyroxenes, garnets, spinels, perovskite and post-perovskite structures<sup>2</sup>. These silicate-rich liquids exhibit high viscosities, as indicated by their high-temperature viscous flow activation energies as a function of metal oxide composition<sup>3</sup>. Moreover, many silicate-rich melts have a tendency to phase separate upon cooling, and this has become an important phenomena in the development of metallurgical processing and glass-ceramics<sup>4</sup>. Many binary silicate melts display stable two-liquid immiscibility during cooling, and the widths of their immiscibility gaps have been shown to vary according to ionic potential (or field strength) and coordination number<sup>5,6</sup>. Moreover, the origin of phase separation in binary silicate systems has been attributed to Coulombic repulsions between poorly screened cations, bounded by bridging oxygen that are strongly polarized towards the silicon<sup>7</sup>. The chemically inhomogeneous liquids often form two-phase glasses, but little is known about their structural evolution, domain sizes, and the interface between the phases, all of which can effect rheological behavior.

Previous small angle scattering methods on fast quenched  $\text{Al}_2\text{O}_3\text{-SiO}_2$  glasses have underestimated the consolute temperature by  $575^\circ\text{C}^{8,9}$ , which underscores the need for *in situ* measurements on the liquid state. Here we present a method that can potentially be used to probe immiscibility domes in binary silicate phase diagrams, while simultaneously providing information on average coordination numbers at high temperatures, which are not always possible using spectroscopic techniques<sup>7</sup>. We have performed temperature dependent small angle and wide angle x-ray scattering measurements (SAXS/WAXS) to investigate liquid-liquid (L-L) immiscibility in the  $\text{Al}_2\text{O}_3\text{-SiO}_2$ ,  $\text{CaO-SiO}_2$ , and  $\text{MgO-SiO}_2$  systems using aerodynamic levitation and laser heating. It is well known that incongruent volatilization of silica occurs at high-temperatures such that rapid measurements are required to minimize mass loss<sup>10</sup>. Furthermore, variable cooling rates and isothermal hold

times are required to probe the kinetics of the phase separation process. The advantages of simultaneous small-angle and wide-angle diffraction are widely recognized<sup>11,12</sup>. Our approach provides continuous coverage of reciprocal space by ensuring overlap between SAXS and WAXS patterns, and further extends the WAXS signal to high-Q by use of high-energy x-rays. In real space, the pair distribution function is obtained through a direct sine Fourier transform of the x-ray structure factor,  $S(Q)$ , giving insight into the local structural arrangements<sup>13</sup>.

Figure 1 shows that L-L immiscibility in  $\text{CaO-SiO}_2$ <sup>14,15</sup> and  $\text{MgO-SiO}_2$ <sup>16,17</sup> occurs in stable regions of their phase diagrams<sup>18</sup>. However,  $\text{Al}_2\text{O}_3\text{-SiO}_2$ <sup>19-21</sup> exhibits metastable immiscibility in the supercooled liquid region and spinodal behavior within the immiscibility dome. In our experiments, homogeneous melts of  $30\text{Al}_2\text{O}_3\text{:}70\text{SiO}_2$  (AS30),  $20\text{CaO:}80\text{SiO}_2$  (CS20), and  $37.5\text{MgO:}62.5\text{SiO}_2$  (MS37.5) were obtained at high-temperatures, and the calcium and magnesium silicate liquids were also measured as a function of controlled cooling. All compositions were found to form phase-separated glasses after cooling to room temperature.

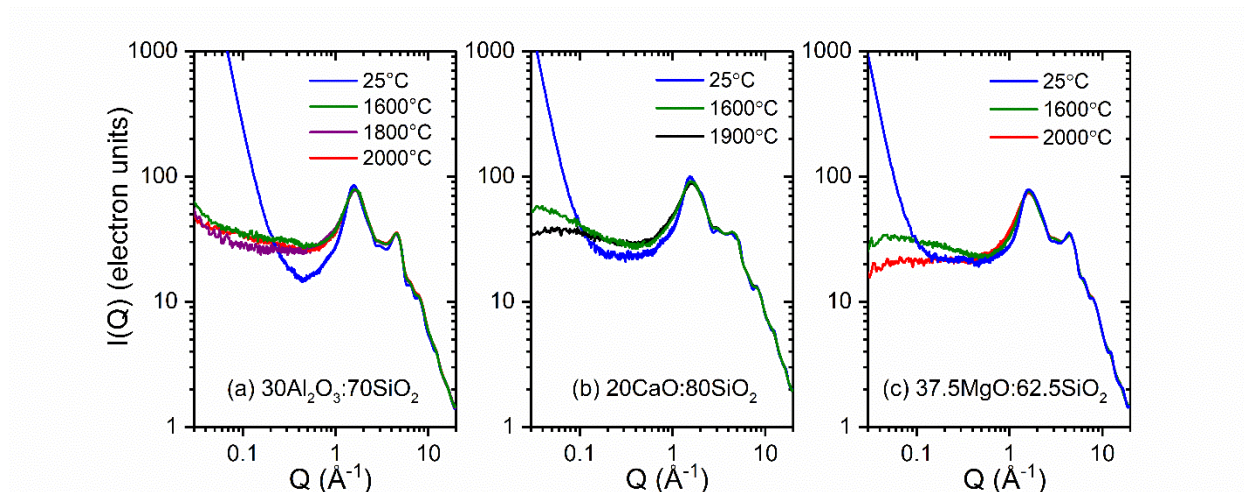


**Figure 1.** Phase diagrams of (a)  $\text{Al}_2\text{O}_3\text{-SiO}_2$ <sup>4</sup> (b)  $\text{CaO-SiO}_2$ <sup>8,9</sup> and (c)  $\text{MgO-SiO}_2$ <sup>10,11</sup>. The dashed black lines represent metastable phase boundaries and the red dotted lines represent the compositions studied here.

## Methods

High energy x-ray diffraction measurements were performed on beamline 6-ID-D at the Advanced Photon Source using an incident energy of 80keV. Simultaneous SAXS and WAXS detector measurements were carried out using a dual detector system with a continuous  $Q$  coverage over the range  $\sim 0.03$  to  $\sim 19 \text{ \AA}^{-1}$ , including an overlap region of  $\Delta Q \sim 1.5 \text{ \AA}^{-1}$ . Dexela 2315-MAM detectors (active area  $230 \text{ mm} \times 145 \text{ mm}$  and square  $74.8 \text{ }\mu\text{m}$  pixels) were mounted in each of the SAXS and WAXS positions at sample to detector distances of  $\sim 230\text{cm}$  and  $\sim 28\text{cm}$  respectively. Careful alignment of the optics ensured slit scattering was not present in the diffusely scattered intensity. A tube with Kapton windows was positioned between the SAXS and WAXS detectors, and evacuated to reduce background air scatter in the SAXS detector. A chamfered beamstop was positioned against the downstream window<sup>13</sup>.

The WAXS detector diffraction patterns were calibrated using NIST standard  $\text{CeO}_2$ , and the SAXS detector was calibrated using silver behenate to determine the precise sample to detector distances and tilts. The SAXS and WAXS data sets were analyzed using the *Fit2D* software<sup>22</sup> and corrected for flat field, polarization, rotation and tilt. The program *PDFgetX2*<sup>23</sup> was used to correct for background, oblique incidence, absorption and detector efficiency effects. Applying the correct transmission factor prior to subtracting the background was essential to obtain good agreement between SAXS and WAXS in the overlap region, where signal-to-background ratio was at its lowest. *PDFgetX2* was used to normalize the WAXS,  $I(Q)$ , data to the sample self-scattering in absolute electron units, and the background corrected SAXS intensity was normalized to the WAXS data in the  $Q$ -space overlap region. The SAXS and WAXS data were spliced together at  $Q \sim 0.5 \text{ \AA}^{-1}$  to obtain the total x-ray structure factor,  $S(Q)$ .  $S(Q)$  was truncated at a maximum  $Q$ -value,  $Q_{\text{max}}$ , corresponding to a node at  $Q \sim 18 \text{ \AA}^{-1}$  and Fourier transformed using a Lorch modification function to ensure reasonable  $r$ -space resolution and minimize spurious ripples to yield the total pair distribution function:  $T(r)$ .



**Figure 2.** Normalized SAXS-WAXS intensities obtained from isothermal measurements on single phase liquid and two phase glassy silicates.

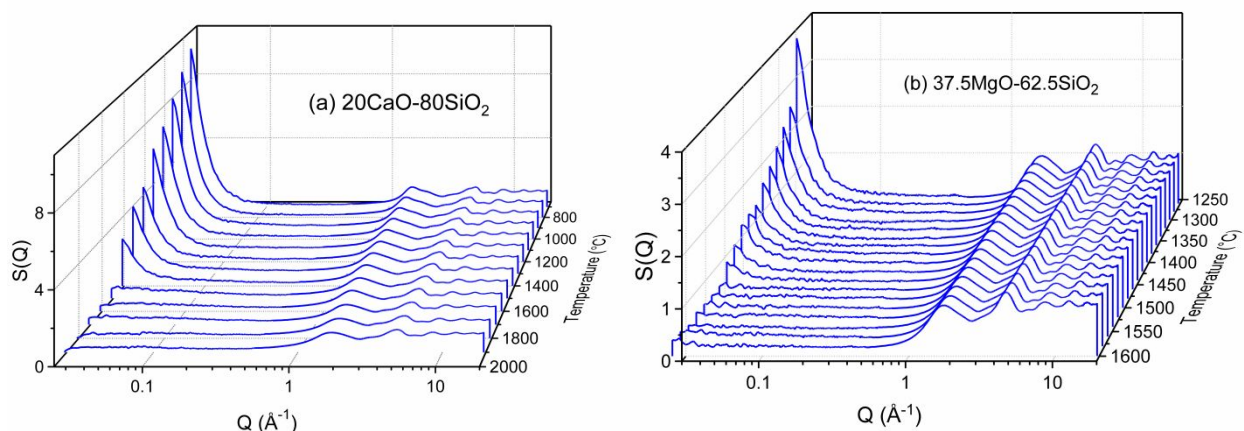
Details of the aerodynamic levitation and laser system have previously been described in depth in other publications<sup>24,25</sup>. Here, 2-3mm diameter spheres of 30:70 mole % Al<sub>2</sub>O<sub>3</sub>:SiO<sub>2</sub>, 20:80 mole % CaO:SiO<sub>2</sub>, and 37.5:62.5 mole % MgO:SiO<sub>2</sub> were prepared with masses ranging from 18-35mg. The spheres were levitated on an oxygen gas jet and melted from above using a 400W CO<sub>2</sub> laser. The typical mass loss during the experiments was ~1% indicating, at most, only a small composition change. Two types of x-ray diffraction experiments were conducted: (i) isothermal experiments, maintaining a fixed temperature for 50s, and (ii) quenching experiments using 4s detector exposures during different quench rates. For the AS30 sample, fast quench rates (~100°C/s) were required to obtain a glass, so only isothermal experiments were feasible in order to obtain adequate statistics in the WAXS signal. For the CS20 sample a quench rate of 25°C/s was required to form a glass, but for MS37.5 a rate of 5°C/s was sufficient.

## Results

The SAXS/WAXS data for all three samples shown in Figure 2 show a dramatic rise in the SAXS (Porod) region in the room temperature glassy phase compared to the corresponding high temperature melts. However, the changes in the WAXS region are much more subtle and generally show a slight sharpening of the peaks at lower temperatures. The



growth of the SAXS intensity upon quenching for CS20 and MS37.5 starts around the temperature of the liquid+crystal/crystal boundary of the stable phase diagrams (figure 1), see figure 3.

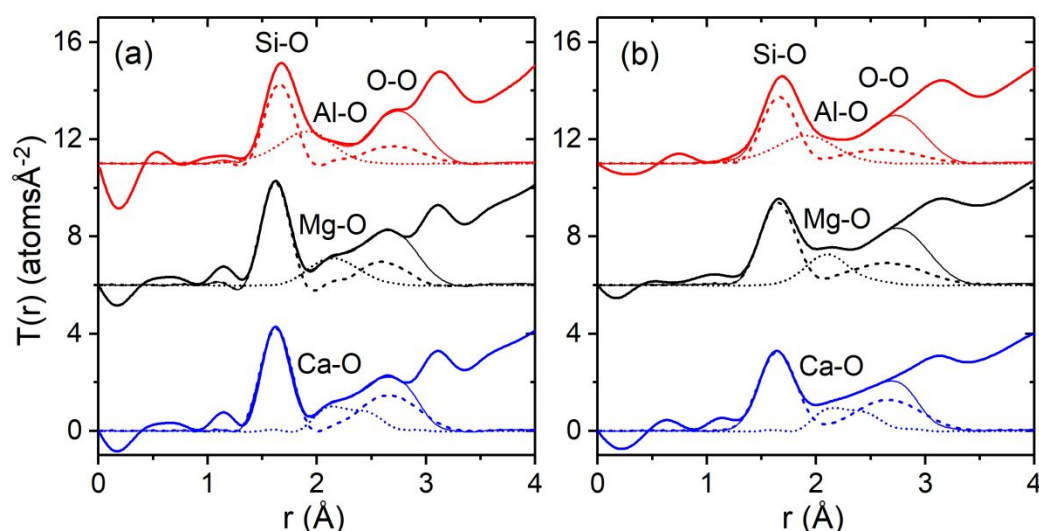


**Figure 3.** The SAXS-WAXS total x-ray structure factor changing from liquid to glass as a function of temperature during the quenching experiments for CS20 and MS37.5.

The changes in short range order in real space and the corresponding total pair distribution functions for the isothermal experiments are shown in Figure 4. Coordination numbers were extracted using NXfit<sup>26</sup> on the 2-phase glasses using estimated number densities of 0.074 atoms Å<sup>-3</sup> for AS30<sup>3</sup> and CS20<sup>27,28</sup>, and 0.082 atoms Å<sup>-3</sup> for MS37.5<sup>29</sup>. The Si-O bond length at a distance of  $r_{\text{Si-O}}=1.62\text{-}1.68$  Å was fixed to correspond to regular tetrahedral i.e.  $N_{\text{SiO}}=4$ , and the O-O distance kept at  $r_{\text{O-O}}=\sqrt{(8/3)}r_{\text{Si-O}}\sim 2.6$  Å with  $N_{\text{OO}}=12(c_{\text{Si}}/c_{\text{O}})^{30}$ . The metal-oxygen peaks are broader than the Si-O, reflecting a distribution of distorted metal-oxygen  $\text{MO}_n$  polyhedra. The effective crystallographic ionic radii given by Shannon and Prewitt<sup>31</sup> indicate  $r_{\text{Si-O}}\sim 1.64$  Å for  $\text{SiO}_4$ ,  $r_{\text{Al-O}}=1.77$  Å for  $\text{AlO}_4$ , 1.87 Å for  $\text{AlO}_5$  and 1.935 Å for  $\text{AlO}_6$ . For AS30, there are a broad distribution of Al-O correlations that overlap with the Si-O peak, and a three Gaussian fit at these fixed bond distances yielded total  $N_{\text{Al-O}}$  coordination numbers of  $4.4\pm 0.3$  (liquid) and  $4.5\pm 0.3$  (glass), indicating a significant fraction of the polyhedra can be attributed to  $\text{AlO}_4$ . A similar analysis on MS37.5 found longer Mg-O bonds at  $\sim 2.3$  Å were required to provide a good fit, in addition to Gaussians at  $R_{\text{Mg-O}}=1.95$  Å for  $\text{MgO}_4$ , 2.05 Å for  $\text{MgO}_5$  and 2.125 Å for  $\text{MgO}_6$ , presumably due to the heavily distorted polyhedra. These fits gave average Mg-O coordination numbers of



$N_{\text{Mg-O}}=5.1\pm0.3$  (liquid) and  $4.8\pm0.3$  (glass). The Ca-O peak is known to exhibit a distribution of both long and short bonds in the melt<sup>27</sup>, and to obtain a good fit short Ca-O bonds at  $\sim 2.1$  Å were needed in addition to Gaussians at  $R_{\text{Ca-O}}=2.40$  Å for  $\text{CaO}_6$  and  $2.47$  Å for  $\text{CaO}_7$ . The fits yielded average Ca-O coordination numbers of  $N_{\text{Ca-O}}=6.5\pm0.3$  (liquid) and  $6.6\pm0.3$  (glass). More accurate values for the coordination numbers require computer modeling to account for all the overlapping correlations within the 3D structure. The variation in bond distances correlate with changes in the ion size<sup>31</sup>, the metal-oxygen coordination fits were all found to be asymmetric, see figure 4.



**Figure 4.** Total x-ray pair distribution functions for the isothermal experiments on binary silicates in the (a) room temperature glass and (b) liquid at 1600°C. The PDF data (thick solid lines) are shown as a function of increasing cation size:  $30\text{Al}_2\text{O}_3:70\text{SiO}_2$  (top),  $37.5\text{MgO}:62.5\text{SiO}_2$  (middle) and  $20\text{CaO}:80\text{SiO}_2$  (bottom). The Gaussian fits described in the text correspond to the Si-O and O-O correlations associated with  $\text{SiO}_4$  tetrahedra (dashed line), the modifier cation-oxygen correlations (dotted line) and the total fit which includes short modifier O-O correlations (thin solid line).

## Discussion.

Markhasev and Sedletsii<sup>5</sup> have argued that immiscibility fields expand with a decrease in ionic radius of the modifier, because it is harder for smaller modifier cations to find coordination environments within a highly polymerized flexible silica network. While some of the Si bonds to the cation-rich structure to satisfy the modifiers coordination requirements, the excess silica forms the second polymerized phase. An exhaustive review of 41 binary silicate systems by Hudon and Baker<sup>7</sup> identified three groups of cations that exhibit different immiscibility behaviors: (1) Those with a large ionic radius  $>87.2\text{pm}$  and coordination number  $\geq 5$ , for which miscibility gap increases linearly with increasing ionic potential e.g. the  $\text{CaO-SiO}_2$  system. (2) *Amphoteric* cations with small ionic radii  $<87.2\text{pm}$  (but  $>26\text{pm}$  corresponding to  $\text{Si}^{4+}$ ) and at least two coordination number environments. One of which must be 4 and the other 5 or higher e.g. the  $\text{Al}_2\text{O}_3\text{-SiO}_2$  and  $\text{MgO-SiO}_2$  systems. (3) Cations with variable crystal field stabilization energies that are difficult to predict.

### $30\text{Al}_2\text{O}_3\text{-}70\text{SiO}_2$ .

The AS30 composition studied here lies midway between  $\text{SiO}_2$  and mullite (which exhibits a range of compositions close to  $3\text{Al}_2\text{O}_3\cdot 2\text{SiO}_2$ ) which congruently melts at  $1850^\circ\text{C}$ . Glass formation and stability decreases as the alumina content increases, and for  $>30\text{ mol.}\%$  only very rapid quenching has been found to produce glasses<sup>10</sup>, consistent with our findings. High silica content  $\text{Al}_2\text{O}_3\text{-SiO}_2$  melts phase-separate readily upon cooling to form a uniform dispersion of amorphous microspheres within a silica-rich glassy matrix<sup>10</sup>. Thermal treatment leads to crystallization of dispersed mullite microspheres<sup>32</sup>. The two liquid phase separation occurs through the mechanism of nucleation and growth in the composition regions 7-20 mol% and 35-55 mol% alumina, and spinodal decomposition can occur in the unstable region in-between. This has been confirmed by the rapid quenching of glasses at  $\sim 30\text{ mol}\%$  alumina, which produces an interconnected fine microstructure of irregularly shaped alumina-rich particles regularly distributed in a silica rich glass in approximately similar volumes<sup>10</sup>.

Gibbs<sup>33</sup> described two distinct thermodynamic conditions for liquid-liquid immiscibility: (i) a spinodal region in which the host phase is unstable with respect to continuous separation, and (ii) a nucleation barrier outside this area, whereby once critical nuclei are formed they grow according to classical nucleation theory. Composition fluctuations grow in amplitude as phase boundaries are being established. It is the *roughness* of these composition gradients in this boundary region that is probed in the Porod regime of our measured SAXS signals. Porod's law states that if the interface between particles is flat, the scattering intensity reaches an asymptotic limit of  $I(Q) \sim BQ^{-n}$  where the Porod exponent  $n=4$  and  $S$  is the surface area of the particles. In this study, for AS30 the exponent was found to be  $n \approx 1$  at 1600°C indicating some degree of density fluctuations in the liquid and  $n$  was about 4 at 25°C confirming a smooth interface between the two glassy phases.

Early structural interpretations of the  $\text{Al}_2\text{O}_3$ - $\text{SiO}_2$  system suggested aluminum ions replace silicon ions in tetrahedral coordination and form oxygen triclusters to maintain charge balance<sup>34</sup>. Recent high energy x-ray diffraction data show a strong distortion of the  $\text{SiO}_4$  tetrahedral units in aluminosilicates with low  $\text{Al}_2\text{O}_3$  content, and a breakdown of intermediate range order as alumina is added<sup>3</sup>. Diffraction and modeling studies on supercooled  $\text{CaSiO}_3$ , which show octahedral metal ion polyhedra tend to edge share with each other and polymerize upon cooling, while  $\text{SiO}_4$  tetrahedra in liquid silica naturally corner share<sup>35</sup>. Our AS30 our results show overlapping Si-O and Al-O contributions, that only sharpens slightly upon quenching with  $N_{\text{AlO}} \sim 5$ , consistent with a distribution of distorted  $\text{AlO}_4$ ,  $\text{AlO}_5$ , and  $\text{AlO}_6$  polyhedra<sup>3</sup>. It has been argued that the presence of  $\text{AlO}_4$  causes bonds to exhibit a covalent character with neighboring oxygens, making them strongly polarized towards the cation<sup>7</sup>. Our low Al-O coordination number is consistent with the presence of some  $\text{AlO}_4$  polyhedra, that have bonds with a covalent component that can efficiently screen the nucleus. The screening associated with  $\text{AlO}_4$  units in the melt considerably reduces the electrostatic repulsions with other cations reducing immiscibility and resulting in metastability.

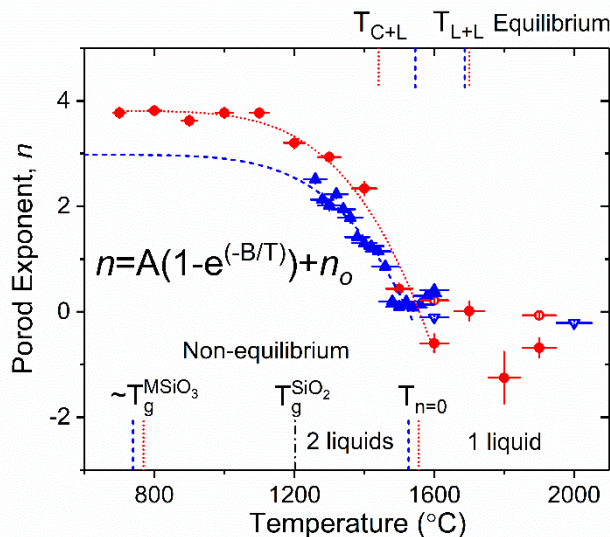
## MgO-SiO<sub>2</sub> and CaO-SiO<sub>2</sub> quenching studies.

The MS37.5 composition is on the edge of the 2-liquid region in the stable phase diagram. Here, our quenching experiments pass from the single to two liquid state at ~1730°C, into the liquid+cristobalite region between 1546-1687°C, and the MgSiO<sub>3</sub>+cristobalite region between 1465-1546°C (Figure 1c). For liquid MgSiO<sub>3</sub>, diffraction and modeling studies have found a mean MgO coordination number of 4.8 (integrating up to 2.8 Å)<sup>20</sup>. Our results on MS37.5 yield a higher value of  $N_{\text{Mg-O}}=5.2$  consistent with the presence of distorted MgO<sub>4</sub>, MgO<sub>5</sub>, and MgO<sub>6</sub> polyhedra<sup>36</sup>. Consequently, as with Al<sub>2</sub>O<sub>3</sub>-SiO<sub>2</sub>, MgO-SiO<sub>2</sub> falls into the amphoteric category. However, the slightly higher cation coordination number leads to stable phase separation.

In CS20, liquid-liquid phase separation is present between 1700-1855°C in the stable phase diagram, cristobalite+liquid forms between 1480-1700°C and tridymite+liquid between 1440-1480°C (Figure 1b). Liquid CaSiO<sub>3</sub> shows a substantial broadening of the first Ca-O bond length distribution in the pair distribution function of the melt compared to the glass<sup>27</sup>. This broadening has been explained by a redistribution of Ca-O bond lengths of primarily 6- and 7-fold coordinated Ca-polyhedra, toward longer distances in the liquid. As high temperature liquid CaSiO<sub>3</sub> is cooled, it has been demonstrated that dispersed short chains of edge-shared Ca octahedra polymerize within the silicate network<sup>35</sup>. Hess<sup>6</sup> has argued that when Ca<sup>2+</sup> is added to liquid SiO<sub>2</sub>, calcium cations that are partly or wholly coordinated by bridging oxygens are poorly shielded, because the oxygens have strong covalent bonds with Si<sup>4+</sup>. As a consequence substantial Coulombic repulsions occur between network modifying cations, which leads to stable phase separation.

In order to correlate the rise in SAXS intensity associated with L-L phase separation we fit the log of the SAXS intensity (interface roughness) versus log temperature with a straight line to extract the Porod exponent:  $n$ . For both CS20 and MS37.5, within the 2 phase liquid region,  $>T_{\text{L-L}}$ , the Porod exponent tends to approximately zero, indicating no heterogeneity in the liquid up to a length-scale of ~200Å. The exponent  $n$  is found to decrease sharply upon cooling to a value of  $n \sim 3$  to 4 between  $T_{\text{L-L}}$  and  $T_{\text{C-L}}$ , as the interface

between the two phases becomes smoother. This is far below the L-L immiscibility dome indicating that our measurements were not in equilibrium. The flat boundaries appear to be established by the time the  $\text{SiO}_2$  glass transition temperature,  $T_g^{\text{SiO}_2}$ , is reached. Viscosity measurements on high temperature alkaline earth binary silicate liquids have been shown to exhibit Arrhenius behavior in the silica-rich region<sup>37,38</sup>. This behavior is expected for strong liquids with good glass forming ability. In this spirit, we find that the temperature dependence of the surface roughness between phases (Porod exponent) can be adequately described using an Arrhenius equation, as shown in figure 6. From this we determine that the phase separation on the few hundred Angstrom length-scale in CS20 occurs at  $1556 \pm 50^\circ\text{C}$  and in MS37.5 at  $1527 \pm 10^\circ\text{C}$ . Despite systematic errors in the data, due to the temperature gradient across the sample from top to bottom, differences in metal ion content and the variation in quenching rates, the change in  $n$  with temperature between the calcium- and magnesium-silicate liquids appears to be similar. This is consistent with the polymerization of the host silicate matrix upon cooling being a major factor during the phase separation process.



**Figure 5.** Temperature variation of the Porod exponent,  $n$ , in  $I(Q)$  for liquid 20CaO:80SiO<sub>2</sub> (red circles denotes quenched sample experiments and red open circles the isothermal measurements) and liquid 37.5MgO:62.5SiO<sub>2</sub> (blue solid up-triangles denotes quenched sample experiments and blue open-down triangles the isothermal measurements). The curves represent Arrhenius fits to the data. The markings at the top correspond to the

equilibrium phase diagram temperatures: the lower 2-phase liquid boundary ( $T_{L+L}$ ) and the crystal plus liquid boundary below ( $T_{C+L}$ ). The markings at the bottom correspond to the non-equilibrium temperatures: the pure  $\text{SiO}_2$  glass transition temperature ( $T_g^{\text{SiO}_2}$ ), the single phase  $\text{MSiO}_3$  glass transition temperatures ( $T_g^{\text{MSiO}_3}$ ) and the temperatures at which the fits cross  $n=0$  ( $T_{n=0}$ ).

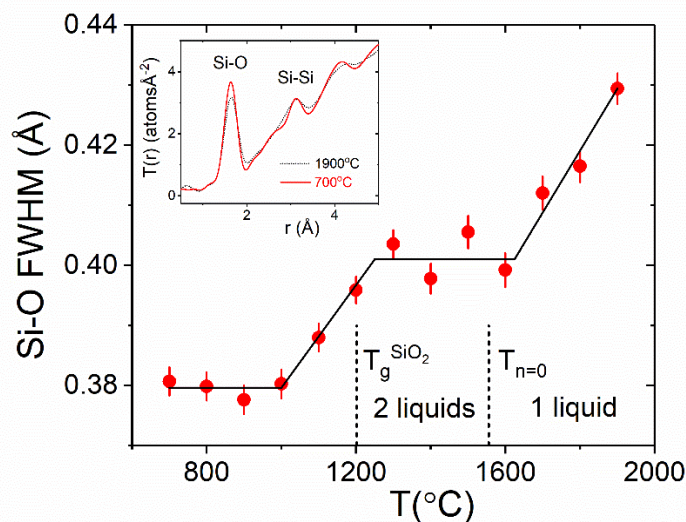
Both quenching studies show a subtle (<1%) shortening of the average Si-O bond and lengthening of the O-O distance upon cooling from a liquid to a glass. The most notable effects in the x-ray pair distribution functions is the expected sharpening of all peaks with decreasing temperature, see Figure 4. Similar results have been reported by Benmore *et al.*<sup>35</sup> for  $\text{CaSiO}_3$ , upon quenching from a liquid to a glass; there it was argued that the presence of isosbestic points in the diffraction patterns was consistent with the polymerization of  $\text{CaO}_6$  edge shared polyhedra. In this study the presence of isosbestic points are not apparent and the changes in the x-ray pair distribution function are dominated by changes in the silicate network rather than calcium polymerization i.e. the main local changes are associated with the Si-O bond intensity at  $\sim 1.64$  Å and Si-Si distance at  $\sim 3.1$  Å. The atomic disorder (root mean square deviation from the average atomic position) within the structure is directly related to the width of each individual atom pair correlation, so in Figure 5 we plot the full width half maximum (FWHM) of the Si-O bond length distribution in CS20 as a function of temperature. Time resolved studies on high temperature liquid silica by Skinner *et al.*<sup>39</sup> have shown a constant FWHM of the Si-O peak for temperatures above  $\sim 1227^\circ\text{C}$  and a linear decrease in Si-O bond ordering as the temperature is decreased below that temperature. For CS20, three regions can be identified corresponding to the changes in the Si-O FWHM peak:

- (i) Normal behavior - a linear increase in Si-O bond ordering with decreasing temperature (i.e. thermal ordering) is initially observed in the homogenous stable liquid region.
- (ii) a plateau in the atomic ordering within  $\text{SiO}_4$  tetrahedra occurs as the 2-phase boundary regions are established. Although thermal ordering will continue to increase with decreasing temperature, phase separation will lead to the

formation of polymerized silica-rich regions with 4-bridging oxygens ( $Q^4$  species) and silica-poor regions which have fewer bridging oxygens e.g.  $Q^2$  species, leading to an overall Si-O peak broadening.

- (iii) once  $T_g^{SiO_2}$  is reached the phase boundaries have been established and the glassy silica-rich matrix becomes frozen in such that thermal ordering dominates again.

An identical analysis on MS73.5 was inconclusive due to larger error-bars associated with the FWHM and the narrower temperature range.



**Figure 6.** The change in full width half maximum of the Si-O peak upon cooling. Insert. The total pair distribution functions of 20CaO:80SiO<sub>2</sub> liquid and glass. The SiO<sub>2</sub> glass transition temperature ( $T_g^{SiO_2}$ ) and temperature at which phase separation begins in the SAXS signal ( $T_{n=0}$ ) are marked. The line is a guide to the eye.

## Conclusions

Understanding stable and metastable liquid-liquid immiscibility is important for predicting the properties of natural magmatism and melts. Although this is a common phenomenon of many binary silicate systems, it is difficult to determine the metal-oxygen coordination numbers in the molten state. The coordination numbers obtained here for



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3  $\text{Al}_2\text{O}_3$ -,  $\text{CaO}$ - and  $\text{MgO}$ -silicate melts are consistent with the model proposed by Hudon and  
4 Baker<sup>7</sup>, that asserts the presence of 4-fold cations can efficiently polarize a neighbouring  
5 oxygen and exhibit strong covalent character. In their model, shared electrons that surround  
6 both the anion and cation shield the charge of the cation reducing the repulsions of the other  
7 modifier cations, narrowing the immiscibility gap or making it metastable in the case of  
8  $\text{Al}_2\text{O}_3$ - $\text{SiO}_2$ . However, more extensive studies are needed to map out the widths of the  
9 immiscibility gaps, to test if the model holds for these and other systems. In addition, the  
10 temperature of the upper consolute point (solvus) are still unknown in many silicate systems  
11 due to the high temperatures involved, and provides another avenue for future studies.  
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21 While the SAXS/WAXS/high-temperature instrumentation presented here is shown  
22 to be sensitive to nanoscale liquid-liquid phase separation, it does not appear that our  
23 measurements reached equilibrium because the SAXS signal is observed far below the  
24 equilibrium dome. This suggests that complex kinetics can play an important role in  
25 determining the morphology of the resulting materials e.g. in the macroscopic structural  
26 evolution of planetary materials such as chondrules that often form from supercooled droplets  
27 of molten oxides. In order to explore the equilibrium phase diagram, time resolved studies  
28 of longer durations are required, either isothermally or at slower cooling rates, although  
29 such experiments will be limited by the evaporation of  $\text{SiO}_2$ .  
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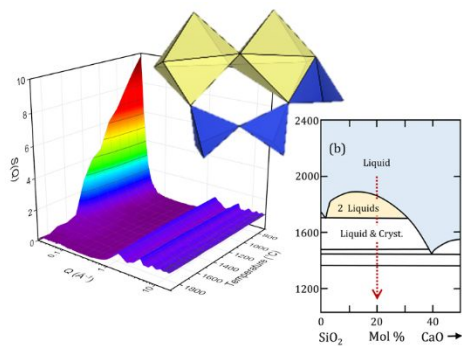
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For TOC Only



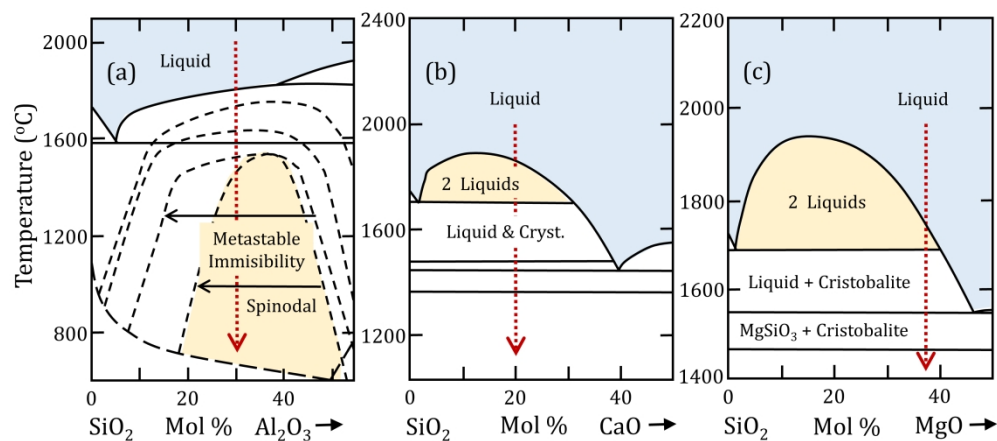


Figure1. Phase diagrams of (a) Al<sub>2</sub>O<sub>3</sub>-SiO<sub>2</sub>[4] (b) CaO-SiO<sub>2</sub>[8,9] and (c) MgO-SiO<sub>2</sub>[10,11]. The dashed black lines represent metastable phase boundaries and the red dotted lines represent the compositions studied here.

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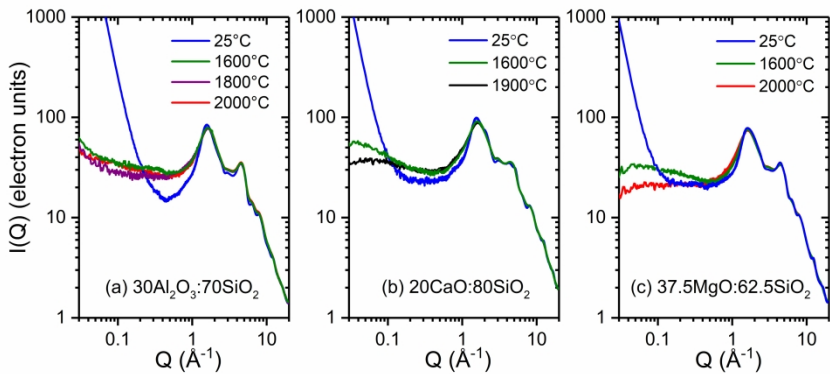


Figure 2. Normalized SAXS-WAXS intensities obtained from isothermal measurements on single phase liquid and two phase glassy silicates.

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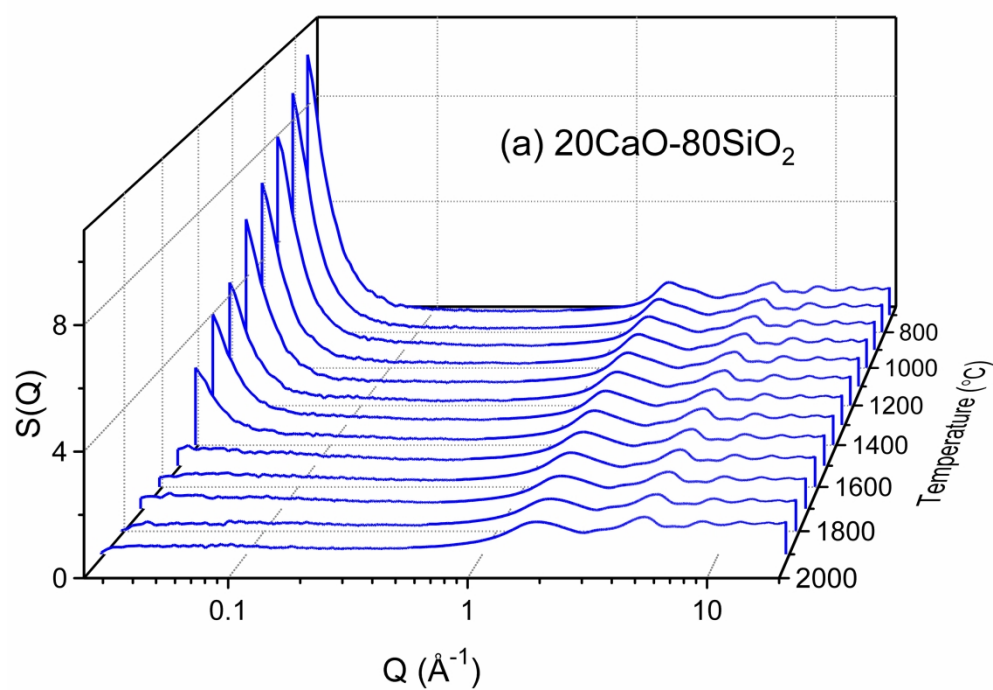


Figure 3(a). The SAXS-WAXS total x-ray structure factor changing from liquid to glass as a function of temperature during the quenching experiments for CS20.

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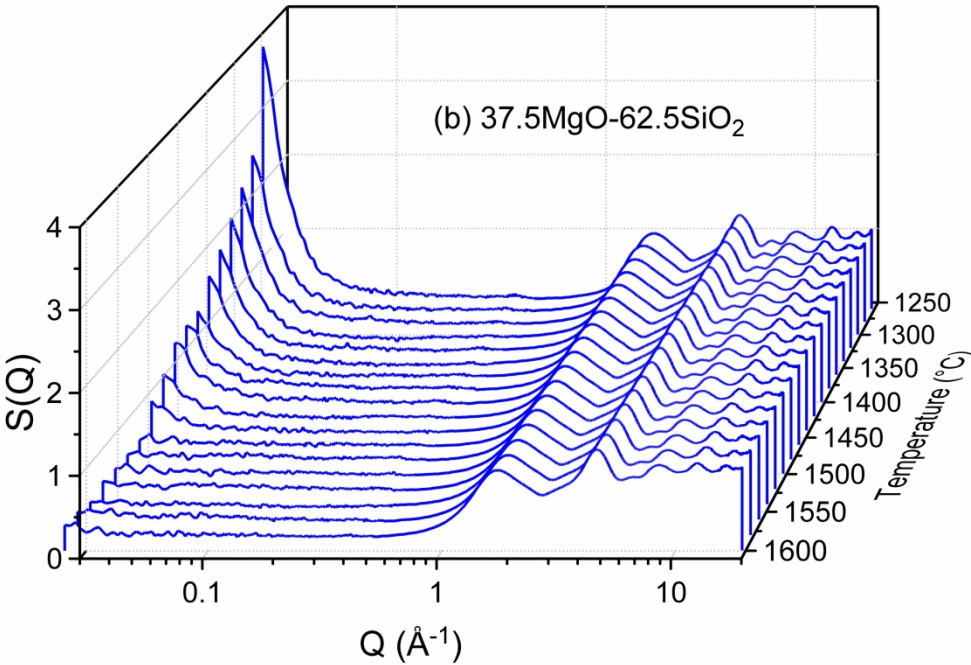


Figure 3(b). The SAXS-WAXS total x-ray structure factor changing from liquid to glass as a function of temperature during the quenching experiments for MS37.5.

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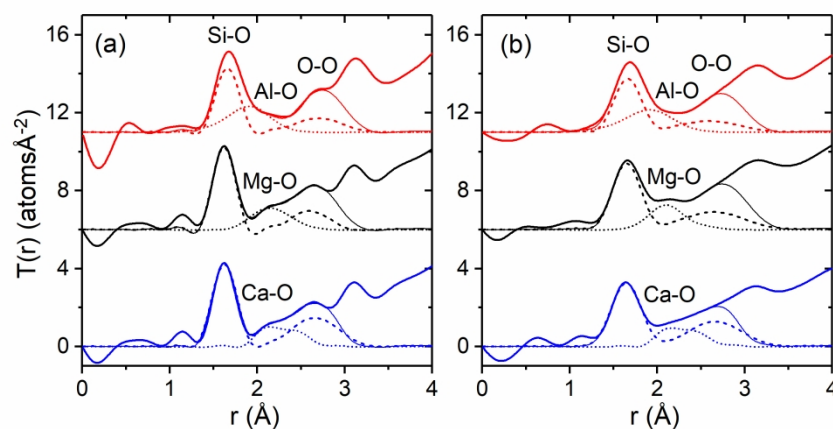


Figure 4. Total x-ray pair distribution functions for the isothermal experiments on binary silicates in the (a) room temperature glass and (b) liquid at 1600°C. The PDF data (thick solid lines) are shown as a function of increasing cation size: 30Al<sub>2</sub>O<sub>3</sub>:70SiO<sub>2</sub> (top), 37.5MgO:62.5SiO<sub>2</sub> (middle) and 20CaO:80SiO<sub>2</sub> (bottom). The Gaussian fits described in the text correspond to the Si-O and O-O correlations associated with SiO<sub>4</sub> tetrahedra (dashed line), the modifier cation-oxygen correlations (dotted line) and the total fit which includes short modifier O-O correlations (thin solid line).

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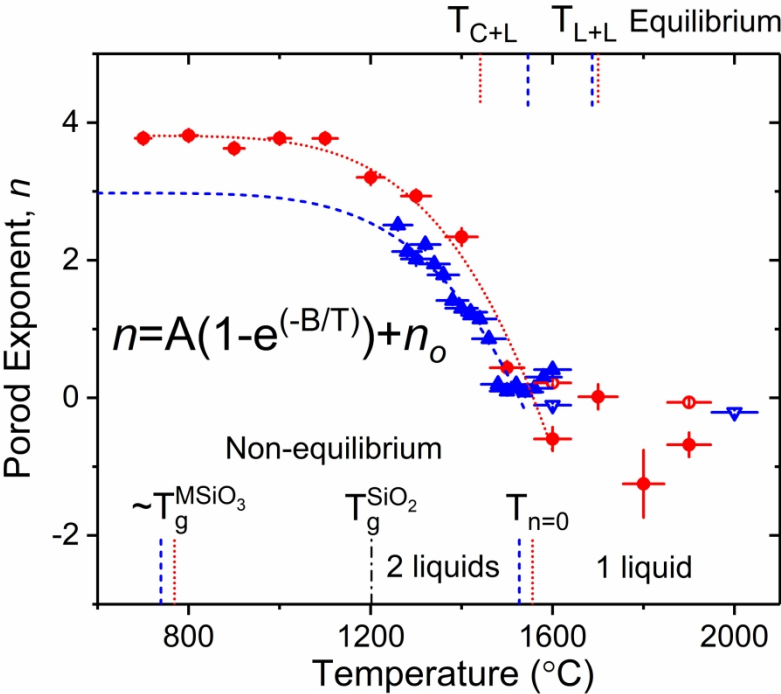


Figure 5. Temperature variation of the Porod exponent,  $n$ , in  $I(Q)$  for liquid  $20\text{CaO}:80\text{SiO}_2$  (red circles denotes quenched sample experiments and red open circles the isothermal measurements) and liquid  $37.5\text{MgO}:62.5\text{SiO}_2$  (blue solid up-triangles denotes quenched sample experiments and blue open-down triangles the isothermal measurements). The curves represent Arrhenius fits to the data. The markings at the top correspond to the equilibrium phase diagram temperatures: the lower 2-phase liquid boundary ( $T_{L+L}$ ) and the crystal plus liquid boundary below ( $T_{C+L}$ ). The markings at the bottom correspond to the non-equilibrium temperatures: the pure  $\text{SiO}_2$  glass transition temperature ( $T_g^{\text{SiO}_2}$ ), the single phase  $\text{MSiO}_3$  glass transition temperatures ( $T_g^{\text{MSiO}_3}$ ) and the temperatures at which the fits cross  $n=0$  ( $T_{n=0}$ ).

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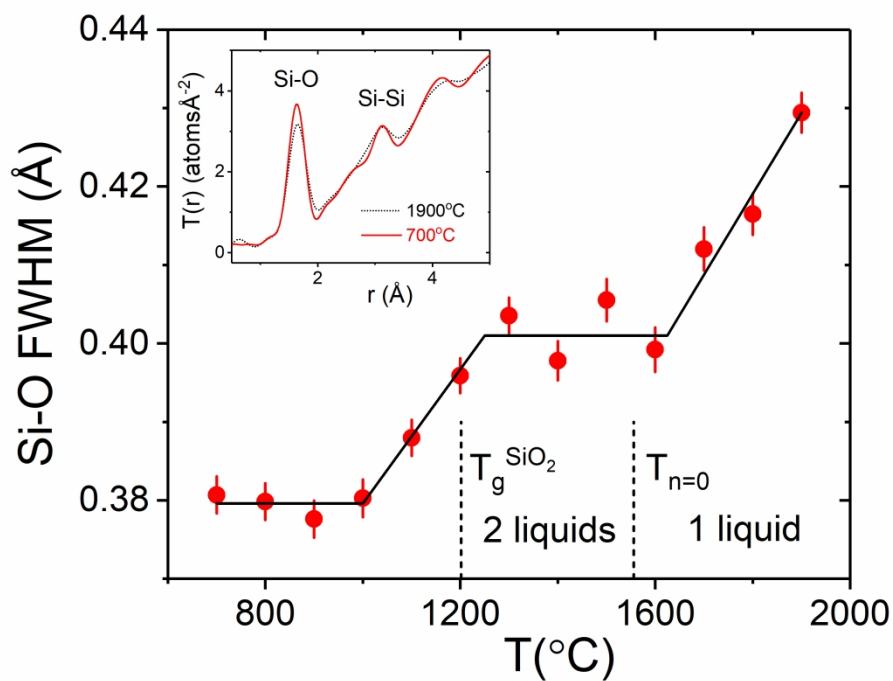
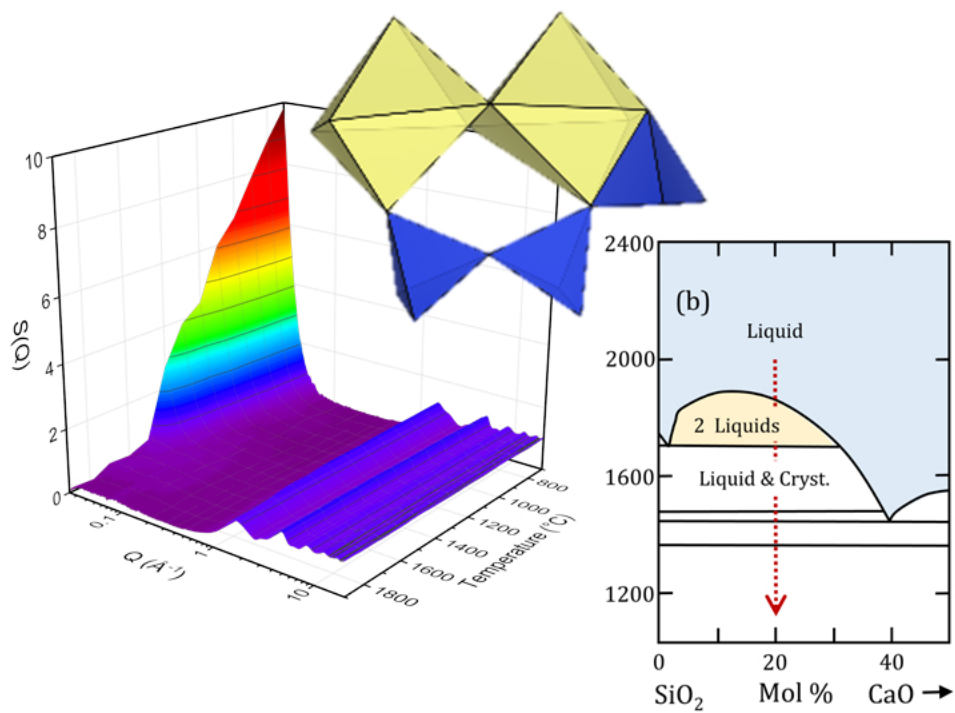


Figure 6. The change in full width half maximum of the Si-O peak upon cooling. Insert. The total pair distribution functions of 20CaO:80SiO<sub>2</sub> liquid and glass. The SiO<sub>2</sub> glass transition temperature ( $T_g^{\text{SiO}_2}$ ) and temperature at which phase separation begins in the SAXS signal ( $T_{n=0}$ ) are marked. The line is a guide to the eye.

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SAXS signal associated with liquid-liquid phase separation in silicate melts

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