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Crossover from Kondo semiconductor to metallic antiferromagnet with 5*d*-electron doping in CeFe₂Al₁₀

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We report a systematic study of the 5*d*-electron-doped system Ce(Fe_{1-x}Ir_x)₂Al₁₀ ($0 \leq x \leq 0.15$). With increasing *x*, the orthorhombic *b* axis decreases slightly while accompanying changes in *a* and *c* leave the unit cell volume almost unchanged. Inelastic neutron scattering, along with thermal and transport measurements, reveal that for the Kondo semiconductor CeFe₂Al₁₀, the low-temperature energy gap, which is proposed to be a consequence of strong *c-f* hybridization, is suppressed by a small amount of Ir substitution for Fe and that the system adopts a metallic ground state with an increase in the density of states at the Fermi level. The charge or transport gap collapses (at *x* = 0.04) faster than the spin gap with Ir substitution. Magnetic susceptibility, heat capacity, and muon spin relaxation measurements demonstrate that the system undergoes long-range antiferromagnetic order below a Néel temperature *T_N* of 3.1(2) K for *x* = 0.15. The ordered moment is estimated to be smaller than 0.07(1) μ_B /Ce, although the trivalent state of Ce is confirmed by Ce *L*₃-edge x-ray absorption near edge spectroscopy. It is suggested that the *c-f* hybridization gap, which plays an important role in the unusually high ordering temperatures observed in Ce*T*₂Al₁₀ (*T* = Ru and Os), may not be necessary for the onset of magnetic order with a low *T_N* seen here in Ce(Fe_{1-x}Ir_x)₂Al₁₀.

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I. INTRODUCTION

Cerium-based intermetallic systems Ce*T*₂Al₁₀ (*T* = Os, Ru, or Fe) with an orthorhombic YbFe₂Al₁₀-type crystal structure (space group *Cmcm*) have attracted considerable interest in recent years [1–16]. In these materials, a hybridization gap opens in the vicinity of the Fermi level owing to the strong coupling between the localized 4*f* electrons and itinerant conduction electrons (*c-f* hybridization) at low temperatures [7,10,11]. Because of the hybridization gap, these materials display semiconducting or semimetallic behavior in the electrical resistivity and are known as “Kondo semiconductors.” In general, it is believed that Kondo semiconductors have nonmagnetic ground states, e.g., SmB₆ [17], YbB₁₂ [18], Ce₃Bi₄Pt₃ [19], and CeRhSb [20,21]. The Kondo

semiconductors CeRu₂Al₁₀ and CeOs₂Al₁₀, on the other hand, were reported to harbor an antiferromagnetic (AFM) ground state with *T_N* = 27.3 and 28.7 K, respectively, with a pseudogap at a temperature slightly higher than *T_N* [2,3,22]. The magnetic ordering temperature was unexpectedly high, despite the large separation (~ 5.2 Å) between the Ce ions. Their Gd counterparts have relatively lower ordering temperatures *T_N* = 17.5 K [23] and 18 K [24], respectively. Moreover, the small Ce ordered moments of ~ 0.3 – 0.4 μ_B are aligned along the *c* axis despite the large uniaxial anisotropy in the magnetic susceptibility ($\chi_a \gg \chi_c > \chi_b$) in the paramagnetic state [6,25,26]. These observations challenge the conventional indirect Ruderman-Kittel-Kasuya-Yosida (RKKY) exchange interaction and crystalline electric field (CEF) models and the ordering mechanism is still under discussion. An optical conductivity measurement on CeOs₂Al₁₀ has revealed that a charge-density-wavelike instability which develops along the *b* axis at temperatures slightly higher than *T_N* induces unconventional AFM ordering [16]. This mechanism contrasts

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with conventional RKKY dominated ordering as in the case of $\text{GdT}_2\text{Al}_{10}$ [7,27] and $\text{NdOs}_2\text{Al}_{10}$ [28]. The orthorhombic crystalline-electric field experienced by the f electrons was also proposed to be an important driver for the strong magnetic anisotropy and the small ordered magnetic moments in $\text{CeT}_2\text{Al}_{10}$ [2,9,29–31]. In the case of $\text{CeFe}_2\text{Al}_{10}$, the presence of strong c - f hybridization leads to a screening of the localized moments by the conduction electron spins, and hence the compound is categorized as a valence fluctuating material [9,30,32]. Due to the strong hybridization, $\text{CeFe}_2\text{Al}_{10}$ is expected to have the largest real or pseudogap feature among the $\text{CeT}_2\text{Al}_{10}$ materials [11,33]. A pseudogap of 12 meV near the Fermi level (E_F) at 10 K was identified by high-resolution photoemission spectroscopy [10]. Inelastic neutron scattering (INS) measurements also confirmed the spin gap or “Kondo gap” of 12.5 meV [34] and further confirmation of the q dependence of the gap was reported through INS studies using single crystals [33,35]. In general, a pseudogap (or narrow-gap or V-shape gap) terminology is used for the Kondo insulators or semimetals when the energy gap on the Fermi surface is not fully opened in all directions but there is a finite density of states on a specific part of the Fermi surface [36]. The band structure can reveal that the Fermi surface is gapped only at certain points. These results suggested a possible Kondo semiconducting nature for $\text{CeFe}_2\text{Al}_{10}$ similar to $\text{Ce}_3\text{Bi}_4\text{Pt}_3$ [37] and SmB_6 [38].

It can be inferred from these findings that the strength of the c - f hybridization plays an important role in the unusual magnetic ordering in $\text{CeT}_2\text{Al}_{10}$. The c - f hybridization can be controlled by the application of a magnetic field or pressure, as well as by atomic substitution. For example, previous experimental studies have shown that the magnetic properties are profoundly affected by T -site substitution. The substitution of Ir (electrons) or Re (holes) on the T site in $\text{CeOs}_2\text{Al}_{10}$ has a significant effect on the magnetic and other physical properties. In $\text{Ce}(\text{Os}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$, the Ir substitution drives the system into a more localized (Ce^{3+}) regime with an ordered moment that increases to $0.92 \mu_B$ for $x = 0.08$, along with a spin reorientation from the c direction to the easy a axis [39]. The T_N , however, decreases from 28.5 K for $x = 0$ to 21 K for $x = 0.08$ and the spin-gap excitations near 11 meV are considerably suppressed [40]. Re substitution, on the other hand, leads to an enhancement of the c - f hybridization, which causes a reduction of $T_N = 21$ K and a reduced ordered moment of $0.18(1) \mu_B$ for $x = 0.03$ [41]. However, the direction of the ordered moment remains unchanged and magnetic order is suppressed for more than 5% Re doping [40,42]. A similar chemical doping effect has also been observed in the Rh/Fe-substituted $\text{CeRu}_2\text{Al}_{10}$ [43–45]. It was seen that the hybridization gap is strongly suppressed by Rh doping despite the more localized nature of the $4f$ state, while Fe doping strengthens the c - f hybridization, leading to a delocalization of the $4f$ state [12,27,34,46]. Since the suppression of T_N in these substituted systems seems to be correlated with the suppression of the hybridization gap, it was proposed that the hybridization gap is necessary for the unusual AFM order with a high T_N [42].

The strength of c - f hybridization in most of the Ce-based compounds is increased by hydrostatic pressure P_h , leading to a suppression of the AFM ordered state. While in $\text{CeT}_2\text{Al}_{10}$

for $T = \text{Ru}$ and Os , upon increasing P_h , T_N first increases to a maximum of 32 and 39 K and then rapidly falls to zero at 4.8 and 2.5 GPa, respectively [2,47]. Since the semiconducting behavior of the resistivity remains in the AFM ordered state and then disappears along with T_N , the hybridization gap was thought to be essential for the unusual AFM order. Another puzzling feature is that application of uniaxial pressure $P \parallel b$ strongly increases T_N in $\text{CeT}_2\text{Al}_{10}$ ($T = \text{Ru}, \text{Os}$) [48].

Rh substitution in $\text{CeFe}_2\text{Al}_{10}$ leads to a similar localization of the $4f$ state but does not induce magnetic ordering for up to 20% Rh substitution down to 2 K. However, a closing of the Kondo gap and the onset of a metallic ground state are observed [49,50].

Given that the $\text{CeT}_2\text{Al}_{10}$ family is highly sensitive to both pressure and the nature of the d electrons [$3d$ (Fe) and $4d$ (Ru)], it is interesting to investigate the effects of adding $5d$ electrons in $\text{CeFe}_2\text{Al}_{10}$, e.g., Ir substitution, which has stronger spin-orbit coupling and a larger ionic radius than Fe and Ru [51]. Our motivation for investigating the $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$ system is, therefore, to study the relationship between the anisotropic c - f hybridization, the spin gap, the Kondo semiconducting behavior, and the onset of magnetic order.

Here we report the results of the macroscopic (thermal, transport, and magnetic) and microscopic (muon spin relaxation, elastic and inelastic neutron scattering) measurements on both polycrystalline ($x = 0, 0.04, 0.08, 0.15$) and single crystal ($x = 0.15$) samples of $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$. These results reveal a long-range ordered AFM state at around 3.1(2) K for $x = 0.15$. The substitution of Ir leads to a decrease in the b axis lattice parameter and increase in both the a and c parameters. We therefore propose that the reduced lattice parameter b , together with an increase in the number of $5d$ electrons, weakens the hybridization between the $4f$ and the conduction electrons, which results in a rapid collapse of the spin/charge gap and an increase of the density of states (DOS) at the Fermi level. As a result, an AFM metallic ground state is realized in this system.

II. EXPERIMENTAL METHODS

Polycrystalline samples of $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$ for $0 \leq x \leq 0.15$ were prepared by arc melting stoichiometric quantities of the constituent elements under a high-purity Ar atmosphere. The samples were heat treated in evacuated quartz tubes at 1000 °C for one week. Single crystals for $x = 0.15$ were prepared by an Al self-flux method using the same procedure as given in Ref. [4]. Powder neutron diffraction (PND) measurements at room temperature on the GEM diffractometer at the ISIS Facility, Rutherford Appleton Laboratory, UK, were used to determine the phase purity and crystal structure of the polycrystalline samples, and Laue x-ray diffraction was used to check the quality of the single crystal. A scanning electron microscope equipped with energy dispersive x-ray analysis was used to check the homogeneity and composition of the single crystal and the results are presented in the Supplemental Material [52].

DC electrical resistivity ρ measurements were performed as a function of temperature down to 2 K in a Quantum Design (QD) Physical Property Measurement System (PPMS) using a

standard four-probe technique with a measuring current of 10 mA. Thermoelectric power S was measured with the thermal transport option of the PPMS. Heat capacity was measured down to 0.4 K using a helium-3 option by the relaxation method in a PPMS. Magnetization M measurements were performed in the temperature range 2–300 K using a vibrating sample magnetometer option of a PPMS.

Muon spin relaxation (μ SR) measurements were performed in zero-field (ZF) using the MuSR spectrometer at the ISIS Facility. The powdered sample with $x = 0.15$ (approximately 4 g) was mounted on a 99.999% pure silver plate using diluted General Electric varnish and then covered with a thin silver foil. The ZF- μ SR spectra were recorded at several temperatures between 1.2 and 5 K. See Refs. [34,53] for a detailed description of the experimental technique. Neutron powder diffraction measurements at 1.5 and 5 K on a sample with $x = 0.15$ were performed using the WISH diffractometer at the ISIS Facility. For both the GEM and WISH data, the nuclear and magnetic intensities were refined by the Rietveld technique using the FullProf software suite [54]. Inelastic neutron scattering measurements at 5 K for $x = 0.04, 0.08,$ and 0.15 were performed using the MERLIN time-of-flight chopper spectrometer at the ISIS Facility. Ce L_3 -edge x-ray absorption near-edge structure (XANES) spectra for $x = 0.04$ and 0.15 were measured in transmission mode (at 7 K) using the general purpose x-ray absorption spectroscopy beamline B18 at the Diamond Light Source, UK. The samples were prepared by grinding the polycrystalline material into fine powder, mixing it with cellulose, and pressing the mixture into pellets.

III. RESULTS AND DISCUSSION

A. Crystal structure

Figure 1 shows the fitted powder neutron diffraction patterns of $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$ for $0 \leq x \leq 0.15$ at room temperature. The data show that all of the Ir-doped materials adopt the orthorhombic $\text{YbFe}_2\text{Al}_{10}$ -type structure with space group $Cmcm$. The crystal structures were refined by the Rietveld method and the lattice parameters and unit cell volume as a function of the Ir concentration x are shown in Fig. 2. The lattice parameters exhibit anomalous changes. The b axis decreases with increasing x up to $x = 0.15$, while a and c have minimum for $x = 0.04$ and then increase with increasing x . As shown in Fig. 2(d), the unit cell volume for $x = 0.15$ is almost identical to that for $x = 0$. This suggests that the overall chemical pressure effect will be negligible. The Fe- $3d$ and Ce- $4f$ anisotropic hybridization near the Fermi level is important for gap formation in $\text{CeT}_2\text{Al}_{10}$ [15]. Band structure calculations reveal a highly anisotropic Fermi surface that is extended along the k_y direction (Γ - Y direction of the Brillouin zone). This anisotropy in the Fermi surface would change with Ir doping and so the observed behavior of the b axis with x could be attributed to a change in the Fermi surface with doping.

It is important to note that the lattice parameters in $\text{Ce}(\text{Fe}_{1-x}\text{Rh}_x)_2\text{Al}_{10}$ isotropically increase by 0.3%–0.4% as x is increased to 0.2, leading to a negative pressure effect [49].

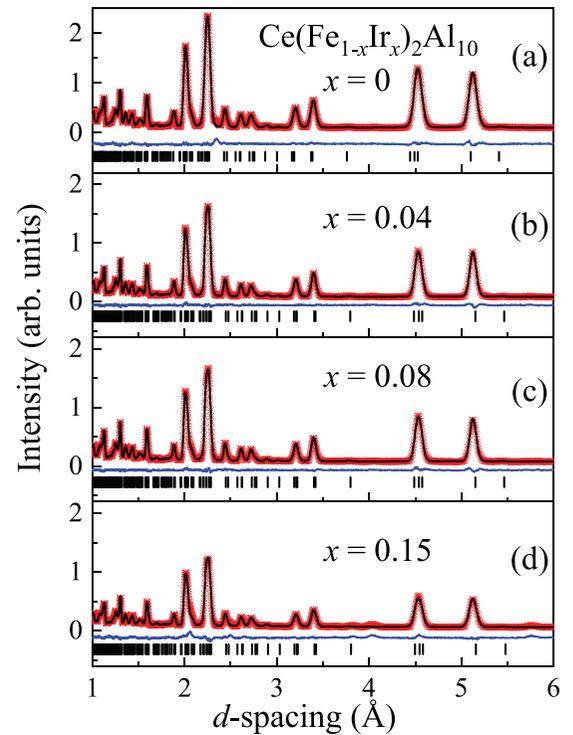


FIG. 1. Fitted powder neutron diffraction patterns of $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$ ($0 \leq x \leq 0.15$) obtained at room temperature using the GEM diffractometer. The observed and calculated intensities and their difference are plotted as red symbols, a solid black line, and a solid blue line, respectively. The vertical bars show the positions of the Bragg reflections.

Upon applying pressure, the lattice parameters of $\text{CeT}_2\text{Al}_{10}$ ($T = \text{Fe}, \text{Ru}, \text{Os}$) all decrease monotonically, but the response is anisotropic [55]. A decrease in the b axis lattice parameter under pressure leads to a concomitant increase in T_N [48,55]. We therefore anticipate a difference in the properties of Ir and Rh-doped $\text{CeFe}_2\text{Al}_{10}$, due to the different behavior of the b axis lattice parameter with chemical substitution.

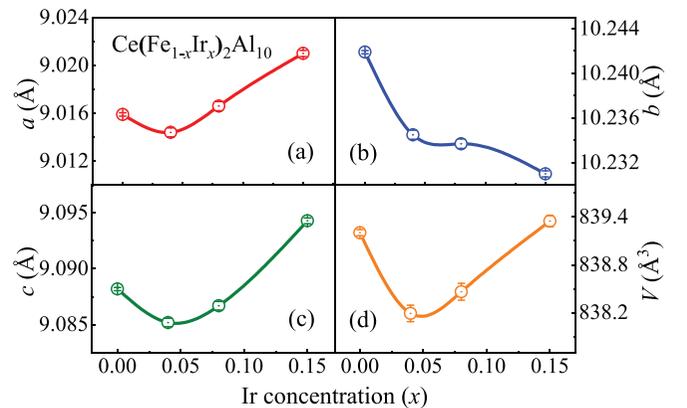


FIG. 2. Variation of the orthorhombic lattice parameters $a, b,$ and $c,$ and unit cell volume V as a function of Ir concentration x for $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$. The lines are guides for the eye.

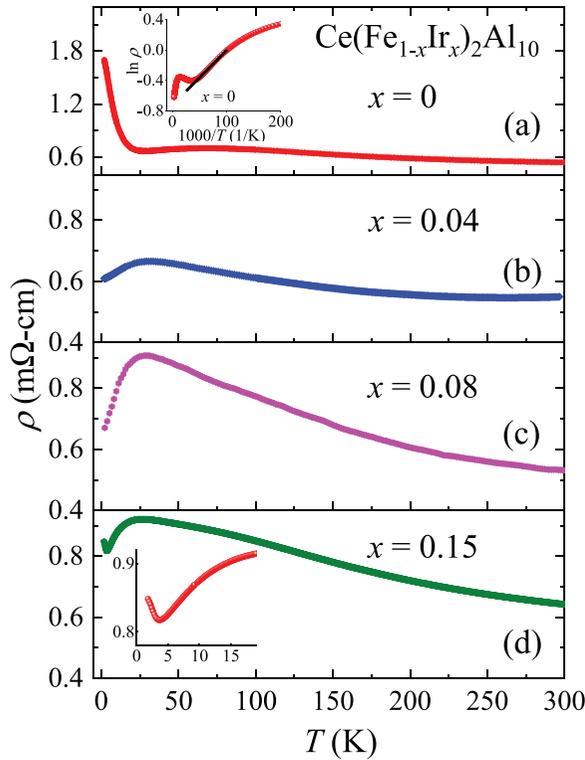


FIG. 3. Electrical resistivity vs temperature for $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$ ($0 \leq x \leq 0.15$). The inset in (a) shows the thermal activation behavior of the resistivity, while the inset in (d) shows an enlarged view of the low temperature upturn of $\rho(T)$ for $x = 0.15$.

B. Electrical resistivity and thermoelectric power

Figures 3(a)–(d) show the temperature dependence of ρ for $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$ ($x = 0, 0.04, 0.08, \text{ and } 0.15$). The $\rho(T)$ curve for $x = 0$ gradually increases with decreasing temperature with a broad hump at $T_0 \sim 75$ K and a sharp upturn below $T = 20$ K, consistent with previous reports [4]. The $-\ln T$ behavior above T_0 can be ascribed to the Kondo scattering on the crystal field excited state. The Kondo semiconducting behavior at $T < 20$ K results in a linear variation in $\ln \rho$ versus $1000/T$ as shown in the inset of Fig. 3(a). The low-temperature behavior is well described by the activation law $\rho(T) = \rho_0 \exp(\Delta/2k_B T)$. A least-squares fit to the $\rho(T)$ data between 10 and 20 K gives an energy gap $\Delta/k_B = 15$ K, consistent with previous reports [4,11].

A small amount of Ir substitution abruptly suppresses the Kondo semiconducting behavior below $T = 20$ K without any significant change in the room temperature resistivity. In fact, $\rho(T)$ of $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$ ($x = 0.04, 0.08, 0.15$) becomes metallic at low temperature. This strongly suggests that the Kondo semiconducting behavior in $\rho(T)$ is suppressed by Ir (or electron) doping, and a metallic behavior is realized. The low-temperature maximum in ρ at $T_0 \sim 30$ K for $x = 0.04$ is attributed to the onset of Kondo coherence. We note that this maximum shifts towards lower temperatures with increasing x . A similar doping effect on $\rho(T)$ has been reported in $\text{CeOs}_2\text{Al}_{10}$ where the low-temperature upturn is strongly suppressed, and a metallic ground state has been realized for

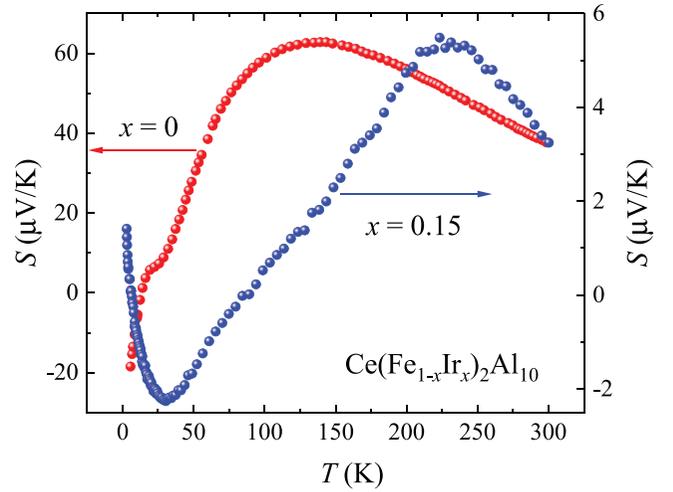


FIG. 4. Thermoelectric power versus temperature for $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$ with $x = 0$ (left axis) from Ref. [4] and $x = 0.15$ (right axis).

both electron (Ir/Rh) and hole (Re) dopings [42]. Therefore, the metallization in Fe/Os-based $\text{CeT}_2\text{Al}_{10}$ materials seems to be favored by both electron and hole doping. A similar feature in $\rho(T)$ is also seen for $\text{CeT}_2\text{Al}_{10}$ ($T = \text{Ru}$ and Os) under hydrostatic pressure [48]. The inset of Fig. 3(d) shows that for $x = 0.15$ a small upturn in $\rho(T)$ appears at 4 K, below the onset of the Kondo coherence (at 20 K). We attribute this behavior to the formation of a magnetic superzone gap associated with long-range magnetic ordering observed near 3.1(2) K in the heat capacity and magnetic susceptibility discussed in Secs. III C and III D below.

The temperature dependence of the thermoelectric power $S(T)$ for $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$ with $x = 0.15$ along with $S(T)$ for $x = 0$, obtained from Ref. [4] for comparison, are shown in Fig. 4. For $\text{CeFe}_2\text{Al}_{10}$, $S(T)$ is positive and significantly enhanced, which is typical of intermediate valence systems like CeNi_2Si_2 [56,57] and CePd_3 [58]. In contrast, a very strong suppression of $S(T)$ is seen for $x = 0.15$. A broad maximum around 225 K is followed by a sign change at 34 K and a minimum of $-2 \mu\text{V/K}$. The overall $S(T)$ behavior is very similar to that observed for the AFM Kondo lattice compound CePdGa with $T_N = 1.8$ K [59,60]. The negative peak in $S(T)$ below 30 K is attributed to Kondo coherence [61].

While $\rho(T)$ of $\text{Ce}(\text{Fe}_{0.85}\text{Ir}_{0.15})_2\text{Al}_{10}$ exhibits a clear anomaly associated with the superzone gap formation indicating an incommensurate AFM ordering, there is no clear indication of magnetic ordering in $S(T)$ except a crossover from negative to positive values of S that occurs near 7 K, at a temperature somewhat higher than the long-range AFM ordering. However, at approximately 3 K, both the temperature dependent $\chi(T)$ and $C(T)$ show a clear downward kink as expected for AFM ordering, as discussed in the following sections.

C. Heat capacity

The double logarithmic plots of C/T versus T for $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$ ($x = 0, 0.04, 0.08, 0.15$) and $\text{LaFe}_2\text{Al}_{10}$

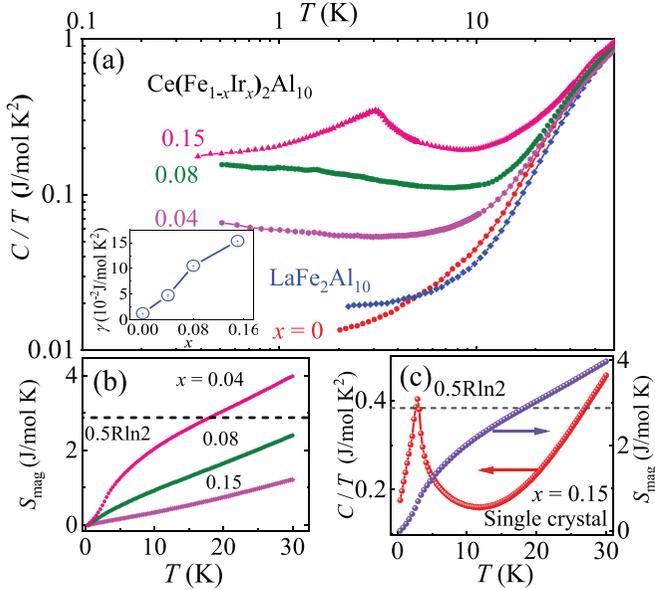


FIG. 5. (a) Temperature dependence of C/T for polycrystalline samples of $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$ ($x = 0, 0.04, 0.08, 0.15$) and $\text{LaFe}_2\text{Al}_{10}$, on a log-log plot. Lower inset: Variation of γ [calculated in the temperature range ($7 \lesssim T \lesssim 20$ K)] as a function of Ir concentration x for the polycrystalline samples. (b) Magnetic entropy S_{mag} as a function of temperature for the polycrystalline samples. (c) C/T versus T (left axis) and S_{mag} versus T (right axis) for a single crystal sample of $x = 0.15$.

are shown in Fig. 5(a). For $x = 0$, C/T decreases with decreasing temperature and becomes smaller than its La counterpart, supporting the existence of a pseudogap at E_F . For $x = 0.04$ and 0.08 , the low-temperature C/T is considerably enhanced without any sign of magnetic ordering, reminiscent of heavy-fermion-like behavior. For $x = 0.15$, however, a λ -type anomaly is observed at $T \sim 3$ K. This is the same temperature at which the $\chi(T)$ data exhibit a peak (see Sec. III D), indicating the onset of long-range AFM ordering for $x = 0.15$. Here it is important to note that no magnetic ordering was seen down to 2 K in $\text{Ce}(\text{Fe}_{0.8}\text{Rh}_{0.2})_2\text{Al}_{10}$, despite the enhancement of the localized nature of the $4f$ electron state [49].

At temperatures 7–20 K, C/T varies linearly with T^2 . Fitting to the data with the form $C = \gamma T + \beta T^3$, the values of γ were estimated as a function of x as shown in the inset of Fig. 5(a). For $x = 0$, γ is almost zero, suggesting a very small or zero density of states at the Fermi level. However, for $x = 0.04$, γ is dramatically enhanced and reaches $0.154(3)$ J/mol K² for $x = 0.15$. In other T -site substituted systems, e.g., $\text{Ce}(\text{Ru}_{1-x}\text{Rh}_x)_2\text{Al}_{10}$ [62] or $\text{Ce}(\text{Os}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$ [42], the γ value increases rapidly with x , which was attributed to a rapid collapse of the spin gap and the appearance of conduction electrons with high effective mass at the Fermi level. We, therefore, anticipate that the enhancement of γ in the heat capacity of $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$ is associated with a change in the gap structure (especially the charge or transport gap in $x = 0.04$) and the existence of a finite density of states close to the Fermi level. Support for this scenario comes from the behavior of the resistivity shown in Fig. 3(b). In addition, it is to

be noted that our results for electron doping differ from those of isoelectronic substitution in $\text{Ce}(\text{Fe}_{1-x}\text{Ru}_x)_2\text{Al}_{10}$, where the Kondo semiconducting ground state with the gap is maintained in all the solid solutions [7,34]. This suggests that the observed behavior in the Ir-substituted $\text{CeFe}_2\text{Al}_{10}$ is essentially due to an excess of electrons rather than any lattice imperfections or disorder, because Ru substitution produces the same amount of disorder but does not produce any change in the Kondo semiconducting ground state. As such, it seems that the electron doping achieved by substituting Fe with Ir (or Rh), weakens the c - f hybridization and destroys the Kondo semiconducting character and the spin/charge gapped state at low temperatures. The observation of a long-range ordered magnetic ground state with Ir substitution rather than the paramagnetic ground state seen with Rh substitution could be attributed to the b axis behavior and also strength of spin-orbit effects.

The contribution of $4f$ electrons to the heat capacity was estimated as $C_{4f} = C[\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}] - C[\text{LaFe}_2\text{Al}_{10}]$. The integration of C_{4f}/T with respect to T gives the magnetic entropy S_{mag} , as shown in Fig. 5(b). For $x = 0.15$, S_{mag} is $0.11R \ln 2$ at $T_N = 3.1$ K and $0.87R \ln 2$ at 30 K. The reduced value of S_{mag} indicates the presence of strong Kondo screening of the $4f$ moments by the conduction electrons even in the magnetically ordered state. Another possible source for a reduced entropy could be the presence of short-range magnetic fluctuations that exist at temperatures well above T_N . A reduced value of $S_{\text{mag}} = 0.3R \ln 2$ at T_N has also been observed in $\text{CeOs}_2\text{Al}_{10}$ [29].

The single crystal sample of $\text{Ce}(\text{Fe}_{0.85}\text{Ir}_{0.15})_2\text{Al}_{10}$ displays a sharp λ type anomaly in $C(T)$ at 3 K, as shown in Fig. 5(c), which is consistent with the data for the polycrystalline sample of $x = 0.15$. The $S_{\text{mag}}(T)$ for the single crystal agrees well with that of the polycrystalline sample with $x = 0.15$.

D. Magnetic susceptibility

Figure 6 shows the temperature dependence of the magnetic susceptibility $\chi(T) = M(T)/H$ [$H = 10$ kOe] for polycrystalline samples of $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$ ($x = 0, 0.04, 0.08, 0.15$) and $\text{LaFe}_2\text{Al}_{10}$. At $T > 100$ K, χ^{-1} vs T data shows a Curie-Weiss behavior as shown in the lower inset of Fig. 6. The broad peak in $\chi(T)$ near 75 K for $x = 0$ moves to 40 K for $x = 0.04$ and then disappears for $x = 0.08$. A similar trend in $\chi(T)$ with electron doping was also seen for Rh-doped $\text{CeFe}_2\text{Al}_{10}$ and was attributed to a localization of $4f$ electrons as a consequence of an increase in the Fermi energy by electron doping [49]. However, no signature of magnetic ordering could be seen down to 2 K for up to 20% Rh doping. On the other hand, $\chi(T)$ of $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$ for $x = 0.15$ shows an anomaly at $T = 3.1(2)$ K (an enlarged view is shown in the upper inset of Fig. 6), indicating a phase transition to an AFM ordered state. A least-squares fit to the χ^{-1} vs T data above 100 K with the Curie-Weiss law including a temperature independent term (lower inset of Fig. 6), yields an effective magnetic moment $\mu_{\text{eff}} = 2.78(2), 2.23(1), 2.10(1),$ and $2.12(1)$ μ_B/Ce , and paramagnetic Weiss temperatures Θ of $-439(11), -140(2), -81.9(1),$ and $-77.2(2)$ K for the samples with $x = 0, 0.04, 0.08,$ and 0.15 , respectively. The value of μ_{eff} is slightly larger than that of a free Ce^{3+} ion ($2.54 \mu_B$)

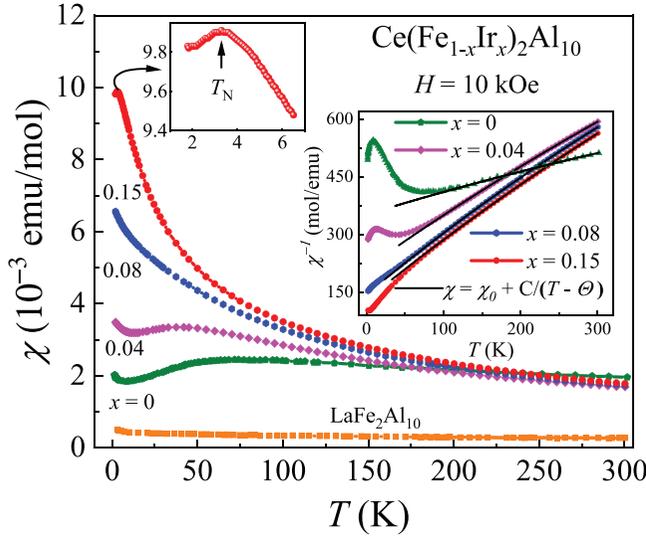


FIG. 6. Temperature dependence of magnetic susceptibility $\chi(T)$ for polycrystalline samples of $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$ ($x = 0, 0.04, 0.08, 0.15$) and $\text{LaFe}_2\text{Al}_{10}$ measured at $H = 10$ kOe. Upper left inset shows the peak in $\chi(T)$ for $x = 0.15$. Lower right inset shows χ^{-1} vs T for $x = 0, 0.04, 0.08, 0.15$. The solid lines are fits to the data with the modified Curie-Weiss behavior including a temperature independent term χ_0 .

for $x = 0$, while it is slightly smaller than expected for the Ir-doped alloys. This discrepancy may be due to crystal-field effects in $\chi(T)$. A large and negative value of Θ is a common feature in Ce-based compounds with strong c - f hybridization [63]. The decrease of $|\Theta|$ from 439 K for $x = 0$ to 77 K for $x = 0.15$ also suggests a decrease in T_K because the value of T_K for the overall CEF levels is proportional to $|\Theta|$ [64].

Magnetization isotherms for the polycrystalline samples of $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$ ($x = 0.04, 0.08, 0.15$), measured at various temperatures (see the Supplemental Material [52]), increase linearly with field. The magnetization at fixed temperature and field increases with x . However, the magnetization for $x = 0.15$ ($0.12 \mu_B/\text{Ce}$ at $H = 70$ kOe) is significantly smaller than the theoretical saturation magnetization of $gJ = 2.14 \mu_B$ for a free ion of Ce^{3+} . The magnetization data thus hint at a weak AFM staggered moment in the magnetically ordered state which is most likely a consequence of a Kondo effect. Further evidence of the reduced moment ordering in $x = 0.15$ comes from the muon spin rotation study presented in Sec. III F.

Now we discuss the anisotropy of $\chi(T)$ for the single crystalline sample with $x = 0.15$. As shown in Fig. 7, the observed susceptibility is highly anisotropic, i.e., $\chi_a \gg \chi_c > \chi_b$ over the whole measured temperature range. The easy-magnetization along the a axis is a common characteristic among the $\text{CeT}_2\text{Al}_{10}$ family. The anisotropy in $\chi(T)$ mainly arises from the CEF effects as seen in $\text{CeRu}_2\text{Al}_{10}$ and $\text{CeOs}_2\text{Al}_{10}$ [26,29]. As presented in the Supplemental Material [52], the magnetization M_a with $H \parallel a$ is strongly enhanced over M_b and M_c below T_N [52]. The magnetic moment per Ce ion along the easy a axis reaches only $0.25 \mu_B$ at 50 kOe, which is still far from the $2.14 \mu_B/\text{Ce}$ expected for the ordered state moment for a free Ce^{3+} ion. M vs H increases linearly up to 50 kOe without showing a spin-flip transition.

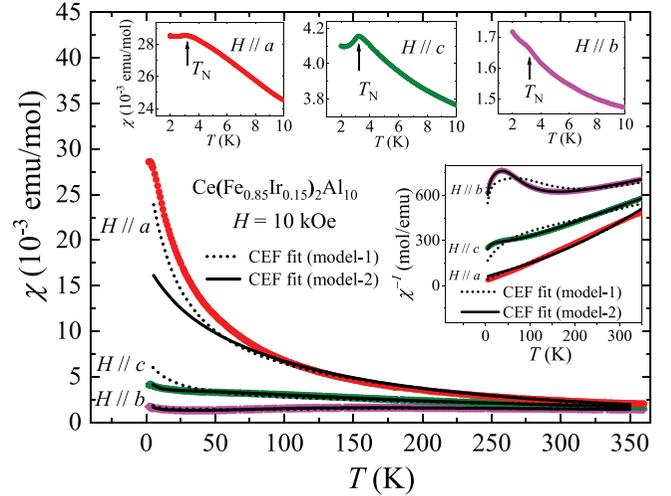


FIG. 7. Temperature dependence of magnetic susceptibility $\chi(T)$ of single crystal $\text{Ce}(\text{Fe}_{0.85}\text{Ir}_{0.15})_2\text{Al}_{10}$ in a field of 10 kOe applied along the three principal axes. Upper insets: χ vs T at low temperature. Lower inset: χ^{-1} vs T along the three principal axes. The dotted and solid lines are fits to the susceptibility data with CEF model 1 and model 2, respectively, discussed in the text.

The upper insets of Fig. 7 show $\chi(T)$ along the three principal axes at low temperature. For $H \parallel c$ there is a clear maximum at $T_N = 3.1(2)$ K while for $H \parallel a$ and b , a more diffuse feature is centered at T_N . This is in agreement with other compounds of this family, where pronounced peaks in $\chi(T)$ are found for $H \parallel c$ and $H \parallel a$ [42,62].

At higher temperatures $\chi_b(T)$ and $\chi_c(T)$ exhibit a broad maximum at $T \sim 150$ K and a shoulder at $T \sim 75$ K, respectively, well above T_N , that can be attributed to CEF effects. The point symmetry of the Ce ion on the $4c$ site is orthorhombic C_{2v} and hence the CEF Hamiltonian, with the quantization axis along the c axis, is given by the following expression:

$$H_{\text{CEF}} = B_2^0 O_2^0 + B_2^2 O_2^2 + B_4^0 O_4^0 + B_4^2 O_4^2 + B_4^4 O_4^4, \quad (1)$$

where B_n^m are the CEF parameters and O_n^m are the Stevens operators [65]. In the mean-field approximation, $\chi^\alpha(T)$ ($\alpha = x, y, z$ or a, b, c) is expressed as $\chi^\alpha(T) = \chi_0^\alpha + \chi_{\text{CEF}}^\alpha(T)/[1 - \lambda_\alpha \chi_{\text{CEF}}^\alpha(T)]$, where λ_α is the mean-field parameter and χ_0^α is the temperature independent susceptibility. The expression for $\chi_{\text{CEF}}^\alpha(T)$ can be found in Ref. [66]. Analysis of the single crystal susceptibility [$\chi_{a,b,c}(T)$] and inelastic neutron scattering data to determine the CEF parameters was carried out using the software available in the Mantid program [67]. We have analyzed the $\chi_{a,b,c}(T)$ and INS data of $x = 0.15$ using two models: In model 1 we fitted the $\chi_{a,b,c}(T)$ and INS data simultaneously to the CEF model. Fits to the $\chi_{a,b,c}(T)$ at 5–350 K and INS data using model 1 are shown by the dotted curves in Fig. 7 and by the solid olive curve in Fig. 8(d). However, the magnetic susceptibility data could not be reproduced well when fitting the INS and susceptibility data simultaneously (model 1). Therefore, in model 2, we fitted just the $\chi_{a,b,c}(T)$ data using the B_n^m obtained from model 1 as the initial parameters. The fits using model 2 are shown by the solid black curves in Fig. 7. Model 2 gives a good fit to the susceptibility data and reproduces the broad maximum in χ_b ,

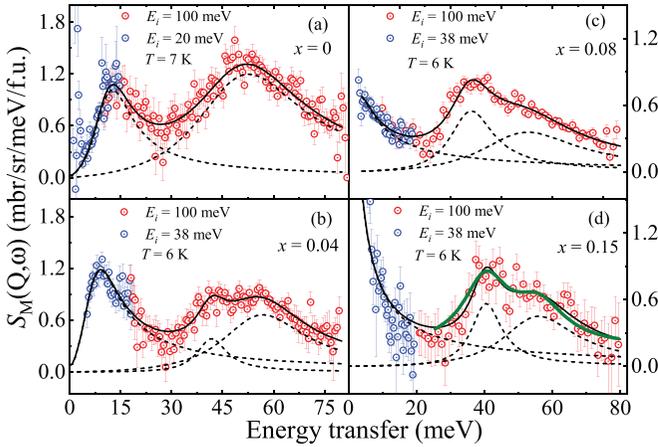


FIG. 8. Inelastic neutron scattering data at 7 K after subtracting the phonon contribution for (a) $\text{CeFe}_2\text{Al}_{10}$ (data from Ref. [34] are given for comparison), (b) $\text{Ce}(\text{Fe}_{0.96}\text{Ir}_{0.04})_2\text{Al}_{10}$, (c) $\text{Ce}(\text{Fe}_{0.92}\text{Ir}_{0.08})_2\text{Al}_{10}$, and (d) $\text{Ce}(\text{Fe}_{0.85}\text{Ir}_{0.15})_2\text{Al}_{10}$ at 6 K. The Q -integration range for the 20 meV data in (a) is 0 to 2 \AA^{-1} , for the 38 meV data in (b)–(d) is 0 to 1.5 \AA^{-1} , and for the 100 meV data in (a)–(d) is 0 to 4 \AA^{-1} . The solid black curves represent fits to the INS peaks with a triple-Lorentzian function (dashed curves represent the components of the fit) multiplied by the population factor (i.e., Bose factor). The fit parameters, i.e., the peak positions, widths, and amplitudes are given in Table S2 of the Supplemental Material [52]. The solid olive curve in (d) shows the fit using model 1.

but gives smaller values for Δ_1 and Δ_2 , which are the energy splittings of the first and second excited levels, respectively. We have simulated the INS spectra using the CEF parameters obtained from model 2 and the result is presented in the Supplemental Material [52]. Although model 1 (simultaneous fit to the INS and single crystal susceptibility data) gives a reasonable description of both data sets, it may not be a unique solution. Hence, it is desirable in the future to include an analysis of the CEF excitations measured using resonant inelastic x-ray scattering, which can give the CEF excitations within the $J = 5/2$ ground state multiplet and between the $J = 5/2$ and $J = 7/2$ multiplets, to obtain a unique set of CEF parameters [68]. The final set of CEF parameters obtained from model 1 and model 2 are given in Table I. For model 1, the values for the molecular field constants [in (mol/emu)] are $\lambda_a = -55.2$, $\lambda_b = -303$, $\lambda_c = -153$ and the corresponding temperature independent susceptibilities [in (10^{-4} emu/mol)]

TABLE I. Crystalline electric field (CEF) parameters and CEF energy levels (Δ_1 and Δ_2) in K, of the Ce-4*f* electrons obtained by analyzing the inelastic neutron scattering and single crystal magnetic susceptibility data of $\text{Ce}(\text{Fe}_{0.85}\text{Ir}_{0.15})_2\text{Al}_{10}$ using model 1 and model 2, as discussed in the text. Literature values of these parameters for $\text{Ce}(\text{Fe}_{0.8}\text{Rh}_{0.2})_2\text{Al}_{10}$ [49], $\text{CeFe}_2\text{Al}_{10}$ [30], $\text{CeOs}_2\text{Al}_{10}$ [66], and $\text{CeRu}_2\text{Al}_{10}$ [66] are provided for comparison.

CEF parameters (K)	B_2^0	B_2^2	B_4^0	B_4^2	B_4^4	Δ_1 and Δ_2
$\text{Ce}(\text{Fe}_{0.85}\text{Ir}_{0.15})_2\text{Al}_{10}$ (model 1)	6.07	-32.9	1.39	-1.27	-6.38	468, 649
$\text{Ce}(\text{Fe}_{0.85}\text{Ir}_{0.15})_2\text{Al}_{10}$ (model 2)	1.62	-29	0.75	-2.48	-2.97	212, 456
$\text{Ce}(\text{Fe}_{0.8}\text{Rh}_{0.2})_2\text{Al}_{10}$	-5	-20	1	-0.5	-5	350, 455
$\text{CeFe}_2\text{Al}_{10}$	-1.33	-15.4	1.42	0.41	-7.93	550, 560
$\text{CeOs}_2\text{Al}_{10}$	1.6	-39	1.4	-2.5	-6.0	433, 704
$\text{CeRu}_2\text{Al}_{10}$	1.58	-38.9	0.714	-1.95	-4	326, 530

are $\chi_0 = 5.2, 3.2, 1.1$. For model 2 we obtained $\lambda_a = -33.1$, $\lambda_b = -160$, $\lambda_c = -147$, and $\chi_0 = 6.8, 2.5, 3.5$.

Here it is important to compare the results of the $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$ and $\text{Ce}(\text{Fe}_{1-x}\text{Rh}_x)_2\text{Al}_{10}$ systems in order to discuss the origin of the magnetic ordering in the former. The substitution of either Rh or Ir for Fe in $\text{CeFe}_2\text{Al}_{10}$ leads to the addition of electrons. The substitution of Rh up to 20% does not induce magnetic order. However, in the case of $\text{Ce}(\text{Fe}_{0.85}\text{Ir}_{0.15})_2\text{Al}_{10}$, this results in a magnetically ordered ground state. Here we suggest that the 4*d*-electron doping weakens the Kondo semiconducting character of $\text{CeFe}_2\text{Al}_{10}$ but not sufficiently to lead to the onset of magnetic order. We propose that two contributions lead to the magnetic ground state in Ir-doped $\text{CeFe}_2\text{Al}_{10}$. One is the increase in the density of states at the Fermi level due to the doped electrons, and the other is the contraction along the *b* axis, as discussed in Sec. III A. Here it is important to note that in $\text{CeT}_2\text{Al}_{10}$ ($T = \text{Ru, Os}$) there is a gap related to the charge- and spin-density waves along the *b* axis, in addition to a hybridization gap along all three axes [16,27]. Moreover, it is also found that the application of uniaxial pressure $P \parallel b$ strongly enhanced the T_N of $\text{CeT}_2\text{Al}_{10}$ ($T = \text{Ru, Os}$). In $\text{Ce}(\text{Fe}_{0.85}\text{Ir}_{0.15})_2\text{Al}_{10}$ we have observed contraction of *b* axis, which may be taken as an effective uniaxial pressure in the system and hence gives magnetic ordering compared to Rh doping. Our results further suggest that the hybridization gap is not mandatory for the AFM ordering observed in the $x = 0.15$ sample, since the low-temperature Kondo semiconducting increase in ρ disappeared and shows a metallic ground state along with a long-range AFM ordering in $C(T)$ and $\chi(T)$.

Furthermore, it is to be noted that spin-orbit coupling (SOC) (which varies as Z^4 , where Z is atomic number) is stronger for Ir than for Rh and hence the SOC may also be playing an important role in the observed differences.

E. Inelastic neutron scattering

We have performed inelastic neutron scattering measurements on polycrystalline samples of $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$ with $x = 0.04, 0.08$, and 0.15 , in order to investigate whether the spin gap has disappeared and to determine the crystal field excitations. We also measured $\text{LaFe}_2\text{Al}_{10}$ in order to estimate the phonon scattering. The Q -integrated energy vs intensity 1D cuts from low- Q and high- Q regions for an incident neutron energy of $E_i = 38$ and 100 meV are given in the Supplemental Material [52] (Figs. S5

and S6). The magnetic scattering of the 38 meV data of $x = 0.04, 0.08,$ and 0.15 was estimated using a direct subtraction of the nonmagnetic $\text{LaFe}_2\text{Al}_{10}$ data from the Ce data as $S(Q, \omega)_M = S(Q, \omega)_{\text{Ce}} - \alpha \times S(Q, \omega)_{\text{La}}$, where α is the scaling factor obtained from the ratio of the total scattering cross section of the Ce by La compounds. The magnetic scattering of the 100 meV data was estimated as $S(Q, \omega)_M = S(Q, \omega, \text{low-}Q)_{\text{Ce}} - S(Q, \omega, \text{high-}Q)_{\text{Ce}} / [S(Q, \omega, \text{high-}Q)_{\text{La}} / S(Q, \omega, \text{low-}Q)_{\text{La}}]$. We then combined the magnetic scattering of the 38 meV data using a scaling factor to match with the 100 meV data. The estimated magnetic scattering after subtracting the phonon scattering is shown in Figs. 8(b)–8(d). For comparison, in Fig. 8(a) we also present the results for $\text{CeFe}_2\text{Al}_{10}$ taken from Ref. [34]. Figure 8(b) shows that for $x = 0.04$ the spin gap is still present, but the gap value is reduced to 8 from 12.5 meV for $x = 0$. On the other hand, for $x = 0.08$ the spin gap has closed completely (within the resolution) and the low-energy response transforms into broad quasielastic scattering as shown in Fig. 8(c). For $x = 0.04$, a spin gap of 8 meV exists in the INS spectrum, but there is no charge gap in the resistivity down to 2 K (see Fig. 3). A very similar behavior has been observed in $\text{Ce}(\text{Fe}_{1-x}\text{Rh}_x)_2\text{Al}_{10}$ with $x = 0.05$, which has a spin gap of 9(2) meV in its INS spectrum [50], but has no charge gap in the resistivity [49]. We attribute this behavior to either the development of an in-gap density of states or a shift of the Fermi level position from the middle of the lower and upper hybridized band (i.e., E_F positioned in the gap) to the bottom of the upper hybridized band. The high-energy peak observed near 55 meV in $x = 0$ has moved to lower energy, 41, 37, and 40 meV, for $x = 0.04, 0.08,$ and 0.15 , respectively, and these compounds reveal two peaks, the second one between 50 and 54 meV (depending on x). This lowering in the first peak position of the high-energy peak is due to a reduction in the c - f hybridization. It is surprising that even though the susceptibility of $x = 0.08$ reveals Curie-Weiss behavior of trivalent Ce ions (see inset of Fig. 6) and the single crystal susceptibility of $x = 0.15$ exhibits strong anisotropy (see Fig. 7), the high energy CEF excitations are very broad. Now let us compare the CEF excitations observed in $x = 0.04$ – 0.15 with that observed in $\text{CeRu}_2\text{Al}_{10}$ and $\text{CeOs}_2\text{Al}_{10}$ [69]. In $\text{CeRu}_2\text{Al}_{10}$ there are two well-defined CEF excitations at 30 and 45 meV at 5 K. At 44 K (i.e., above $T_N = 27$ K), the two clearly resolved CEF excitations are transformed into one broad excitation near 30 meV with a tail up to 80 meV (a second possible CEF excitation is seen near 45 meV in the tail). In $\text{CeOs}_2\text{Al}_{10}$ the CEF excitations are broad and not well resolved both at 5 and 65 K ($T_N = 28.9$ K). The first CEF excitation is at 36 meV with a tail going up to 80 meV with the possibility of a second CEF excitation near 60 meV. The high energy CEF response seen here in $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$ with $x = 0.04$ – 0.15 [Figs. 8(b)–8(d)] is very similar to that observed for $\text{CeOs}_2\text{Al}_{10}$.

F. Neutron diffraction and muon spin relaxation

In order to understand the magnetic interactions and magnetic structure at the microscopic level, we have performed neutron diffraction measurements on a polycrystalline sample

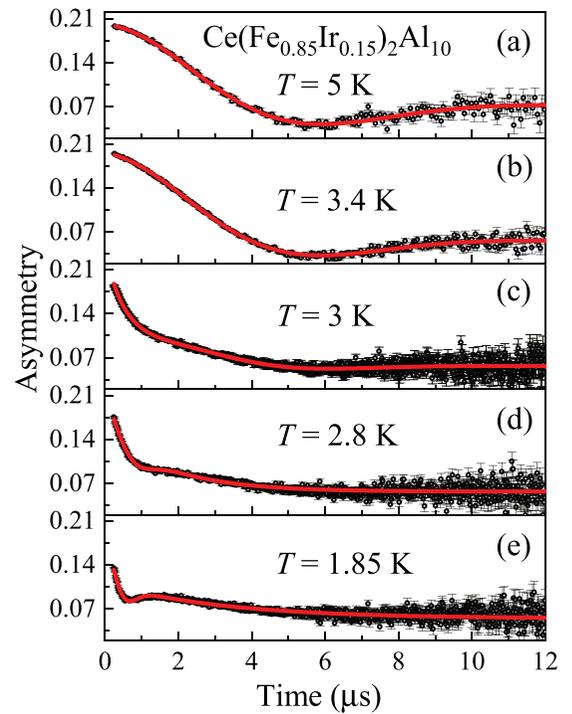


FIG. 9. Zero-field μSR spectra for polycrystalline $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$ ($x = 0.15$) at various temperatures. The solid lines are least-squares fits to the data as described in the text.

of $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$ with $x = 0.15$ using the WISH diffractometer (see the Supplemental Material [52]). No clear sign of magnetic Bragg peaks could be observed in the diffraction data collected below T_N , which indicates that the magnetic moment in the ordered state is very small. Our simulation of the magnetic scattering, using models reported previously for undoped and carrier-doped $\text{CeT}_2\text{Al}_{10}$ ($T = \text{Ru}$ and Os) systems [6,70], allowed us to set an upper limit for the ordered moment of $\sim 0.07(1) \mu_B/\text{Ce}$.

Given the very small ordered moment for $x = 0.15$, we performed a positive muon spin relaxation measurement. The muon spin relaxation technique is a very sensitive local probe for characterizing static and dynamic magnetism and has been extensively used to trace the onset of AFM order in $\text{CeT}_2\text{Al}_{10}$ materials [6,71]. The zero-field μSR asymmetry spectra for $x = 0.15$ collected at several temperatures ranging from 1.8 to 5 K, are shown in Figs. 9(a)–9(e). As shown in Figs. 9(a) and 9(b) at 3.4–5 K, the ZF- μSR spectra show a Kubo-Toyabe (KT) type behavior, which originates from a static internal field with a Gaussian distribution of nuclear dipole moments [72]. In the paramagnetic regime, the μSR spectra can be described by

$$A(t) = A_0 G_{\text{KT}}(t) \exp(-\lambda t) + A_{\text{bg}}, \quad (2)$$

where

$$G_{\text{KT}}(t) = \frac{1}{3} + \frac{2}{3}(1 - \Delta^2 t^2) \exp\left(-\frac{\Delta^2 t^2}{2}\right) \quad (3)$$

is the Kubo-Toyabe function, A_0 is the initial asymmetry at $t = 0$, Δ/γ_μ represents the distribution width of the local Gaussian fields, $\gamma_\mu/2\pi = 135.5$ MHz/T is the muon gyromagnetic ratio, λ is the depolarization rate caused by

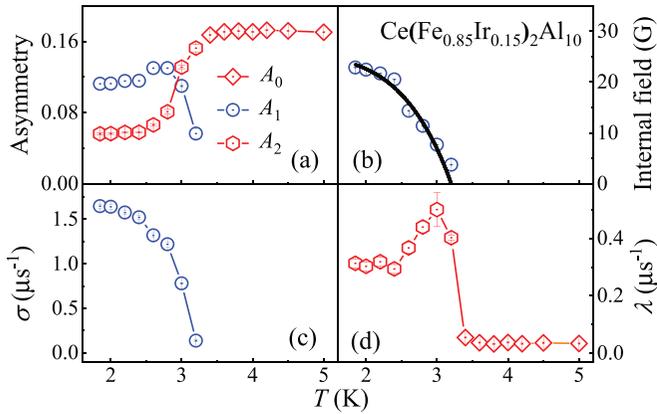


FIG. 10. Temperature dependence of (a) the initial asymmetry, (b) the internal field at the muon stopping site, obtained by zero-field μ SR experiment on $\text{Ce}(\text{Fe}_{0.85}\text{Ir}_{0.15})_2\text{Al}_{10}$. The solid line represents the fit using Eq. (5). (c) Temperature dependence of the distribution width of the local Gaussian field and (d) the depolarization rate.

fluctuating electronic spins, and A_{bg} is a constant background. Best fits to the spectra using Eqs. (2) and (3), shown by the solid lines in Figs. 9(a) and 9(b), reveal a nearly T independent Δ equal to $0.295(1) \mu\text{s}^{-1}$ above T_N . The background component arising from muons stopping in the silver sample holder, was estimated to be $A_{\text{bg}} = 0.027$ from the 3.4 to 5 K data.

The Larmor precession of the muon spin around the internal fields of the magnetically ordered system gives rise to an oscillatory muon polarization as a function of time t . Our μ SR spectra exhibit oscillations below 3.2 K, confirming the long-range magnetic ordering of the Ce moments. Figures 9(c)–9(e) show these spectra can be well fitted by

$$G_z(t) = A_1 \cos(\omega t + \phi) \exp(-\sigma^2 t^2/2) + A_2 \exp(-\lambda t) + A_{\text{bg}}, \quad (4)$$

where A_1 , A_2 , λ , $\omega (= \gamma_\mu B_{\text{int}})$, and ϕ , are the associated asymmetries, exponential depolarization rate, muon spin rotation frequency (B_{int} is the internal field at the muon site), and the initial phase, respectively. The first term of Eq. (4) represents the transverse components of the internal fields seen by the muons along which they precess, while the second term represents the longitudinal component. A different value of $A_{\text{bg}} = 0.054$ was observed in the temperature range 1.85 to 3.2 K. This indicates that below 3.4 K an additional oscillatory component with an initial asymmetry ~ 0.027 may be present, which is in agreement with two oscillatory components observed below T_N in the ZR- μ SR spectra of $\text{CeRu}_2\text{Al}_{10}$ [6]. However, due to the very low values of the frequency and relaxation rate of this component, their values were set to zero, and the component folded into A_{bg} in order to allow the fit to converge. The fitting parameters as a function of temperature, determined from the best fits, are shown in Figs. 10(a)–10(d). Figure 10(b) shows the internal field (muon precession frequency) at the muon site as a function of temperature. This shows that the internal field (or frequency) appears just below 3.2 K, indicating the onset of bulk long-range magnetic order, which agrees with the heat capacity and magnetic susceptibility data. The value of the internal field is 22.4 G at

the base temperature (i.e., 1.85 K). This is smaller than the maximum field seen in $\text{CeRu}_2\text{Al}_{10}$ (120 G) [6] and $\text{CeOs}_2\text{Al}_{10}$ (50 G) with the ordered moment along the c axis [71]. For $\text{Ce}(\text{Fe}_{0.85}\text{Ir}_{0.15})_2\text{Al}_{10}$, we assumed that the ordered moment lies along the easy axis of the CEF (i.e., a axis). A rough estimate of the ordered moment from the observed internal field at the muon stopping site, made using the results of the dipolar field calculation from Ref. [73], gives $0.42 \mu_B/\text{Ce} \times (22.4/142) = 0.066 \mu_B/\text{Ce}$. This is in agreement with the absence of visible magnetic Bragg peaks in the WISH data. Below 3 K, the depolarization rate also increases as shown in Fig. 10(d). In principle, this could originate from various phenomena related to a change in the distribution of internal fields. The relaxation rate λ associated with the local field fluctuation rates sensed by the muon spin exhibits a sharp peak at $T = 3$ K. Notably, such behavior in λ is expected across a magnetic phase transition.

We examined the temperature dependence of the internal fields, which appear at temperatures below 3.2 K and signify the onset of long-range magnetic order, in order to determine the nature of the magnetic interactions. The temperature dependence of the internal field was fitted using

$$B_{\text{int}}(T) = B_0 \left[1 - \left(\frac{T}{T_N} \right)^\alpha \right]^\beta. \quad (5)$$

The fit is shown by the solid curve in Fig. 10(b). When we allowed all the parameters to vary freely including β , the errors on the fit parameters were large. Hence, we kept the value of β fixed at 0.97, which was estimated by first allowing all the parameters to vary. The fitting parameters are $B_0 = 26(3)$ G, $\alpha = 4(2)$, and $T_N = 3.2(1)$ K. The value of $\beta \sim 0.97$ suggests the magnetic interactions in the electron-doped system are not purely of a mean-field type for which β is expected to be 0.5. In fact, $\alpha > 1$ indicates complex magnetic interactions within this system [74,75].

G. Ce L_3 -edge x-ray absorption spectroscopy

We performed Ce L_3 -edge x-ray absorption near-edge spectroscopy (XANES) at 7 K on polycrystalline samples with $x = 0.04$ and 0.15, in order to obtain more information about the valence state of the Ce ions as a function of Ir doping. The spectrum is sensitive to electronic transitions from the core level to the higher unfilled or half-filled orbitals of the absorbing atom. XANES is therefore uniquely placed to measure valence states. As shown in Fig. 11, the spectra for both $x = 0.04$ and 0.15 have a prominent peak at about 5728 eV, which corresponds to a signal from a bulk Ce^{3+} configuration. A weak shoulder centered at around 5738 eV in the absorption spectra of $x = 0.04$ is due to a contribution from Ce ions in the 4+ oxidation state. For $x = 0.04$, both Ce^{3+} and Ce^{4+} contributions are clearly visible, indicating a valence fluctuating state for this compound, which is in agreement with the broad peak in $\chi(T)$ near 40–50 K (see Fig. 6). As expected, the intensity of the Ce^{4+} component for $x = 0.15$ is strongly suppressed as compared to its value for $x = 0.04$. The observed behavior reflects a crossover from a valence fluctuating state for the Ce $4f$ state to a stable trivalent state between $x = 0.04$ and $x = 0.15$. This finding is

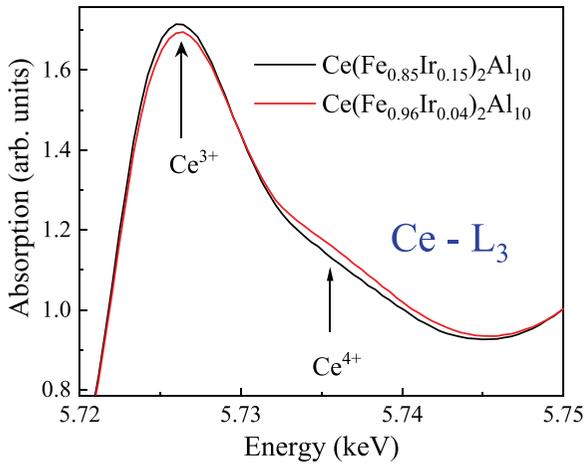


FIG. 11. Ce L_3 x-ray absorption edge spectra of $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$ for $x = 0.04$ and 0.15 at 7 K.

in accordance with the results obtained by our thermodynamic and transport experiments.

IV. SUMMARY

In summary, we have investigated the effects of $5d$ electron doping on the Kondo semiconducting ground state of $\text{CeFe}_2\text{Al}_{10}$ using magnetic, transport, and thermal properties, μSR , and elastic and inelastic neutron scattering measurements for $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$ ($x \leq 0.15$). With increasing x to 0.15 , the b axis parameter decreases while changes in a and c leave the unit cell volume almost unchanged. The low-temperature semiconducting behavior in the resistivity with a charge gap is completely suppressed for $x \geq 0.04$, and instead a metallic-like behavior appears. Inelastic neutron scattering results reveal that the spin gap of 12.5 meV for $x = 0$

decreases to 8 meV for $x = 0.04$. For $x = 0.08$, however, the spin gap is closed and the INS response is transformed into a quasielastic line. It has been shown that the DOS at the Fermi level is considerably changed by $5d$ electron doping, which results in the destruction of the spin-gap excitation for $x \geq 0.08$. We observe that $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$ undergoes a long-range AFM transition below $T_N = 3.1(2)$ K for $x = 0.15$. Ce L_3 -edge XANES measurements provide direct evidence for a stable trivalent Ce^{3+} state in the $x = 0.15$ sample. The appearance of AFM order is in contrast to the $4d$ electron doped system $\text{Ce}(\text{Fe}_{1-x}\text{Rh}_x)_2\text{Al}_{10}$ ($x < 0.2$) where the lattice expands isotropically and no long-range magnetic order appears down to 2 K. We propose that the appearance of AFM ordering is not only related to c - f hybridization but that a lattice contraction along the b axis plays an important role. Our results also suggest that the c - f hybridization gap may be necessary to form the AFM order with a very high T_N seen in $\text{CeT}_2\text{Al}_{10}$ ($T = \text{Ru}$ and Os), but is not necessary in $\text{Ce}(\text{Fe}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$, which has a lower T_N .

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