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# Higgs Searches and WW Scattering

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## HIGGS SEARCHES AND WW SCATTERING

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### 1. INTRODUCTION.

This lecture is about aspects of Electroweak Symmetry Breaking (EWSB). There are sections on Higgs searches in the Standard Model (SM), on  $WW$ ,  $WZ$  and  $ZZ$  scattering as probes of EWSB, and on Higgs phenomenology in the Minimal Supersymmetric Standard Model (MSSM).

The SM has one complex  $SU(2)$ -doublet of scalar fields,

$$\Phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix} = \begin{pmatrix} -iw^+ \\ (-iz + H + v)/\sqrt{2} \end{pmatrix},$$

with vacuum expectation value  $v$  arising from the self-interaction

$$V(\Phi) = \lambda[|\Phi|^2 - v^2/2]^2.$$

In the resulting EWSB pattern, where  $W$  and  $Z$  fields acquire masses, the scalar field components  $w^\pm$  and  $z$  become the new longitudinal components  $W_L^\pm$  and  $Z_L$  while  $H$  survives as a real  $SU(2)$ -singlet scalar field - the Higgs boson - with mass  $m_H = \sqrt{2\lambda}v$ . To recover standard Fermi couplings we must have  $v = (\sqrt{2}G_F)^{-1/2}$ , but the quartic coupling  $\lambda$  is not determined *a priori*.

How can we probe the EWSB dynamics?

(i) Look for  $H^0$ ; its mass measures  $\lambda$ ; its couplings to  $W, Z$  and fermions are prescribed by  $v$  and the particle masses, and should be checked.

(ii) Study  $W_L^\pm$  and  $Z_L$  scattering; they remember their origins as would-be Goldstone bosons  $w^\pm$  and  $z$ , and their scattering via  $V(\Phi)$  will be strong if  $\lambda$  is large.

These strategies, motivated here by the SM case, extend naturally to more general scenarios. We shall mostly illustrate the possibilities for the proposed Large Hadron

Collider LHC at CERN, but for convenience shall also take some examples from studies for the comparable but cancelled SSC project.

## 2. SM HIGGS SEARCHES AT HADRON COLLIDERS.

Higgs hadroproduction goes mainly through the diagrams in Fig.1 [1]:

- (a)  $gg \rightarrow H$  via heavy quark loops usually gives the biggest rate;
- (b)  $qq(\bar{q}) \rightarrow H$  via  $WW$  (or  $ZZ$ ) fusion is also big, and has taggable jets;
- (c)  $gg \rightarrow t\bar{t}H$  and (d)  $q\bar{q}' \rightarrow WH$  are smaller but have the advantage that we can tag the leptons from  $W \rightarrow \ell\nu$  and  $t \rightarrow bW \rightarrow b\ell\nu$ .

Fig.2 shows the corresponding lowest-order LHC cross sections, for  $m_t = 140$  GeV, and Fig.3 gives the principal decay branching fractions.

### 2.1 Intermediate mass range.

Light Higgses ( $m_H \lesssim M_Z$ ) should be detectable at LEP1 or LEP2, but the intermediate mass range  $M_Z \lesssim m_H \lesssim 2M_Z$  needs higher energy. The dominant  $H \rightarrow b\bar{b}$  mode was widely believed to be undetectable at hadron colliders, because of enormous  $b\bar{b}$  backgrounds from QCD; the  $\tau\bar{\tau}$  mode too is interesting but problematical. Until recently, most attention was therefore focussed on the more promising signals from  $H \rightarrow \gamma\gamma$  and  $H \rightarrow ZZ^* \rightarrow \ell\bar{\ell}\ell'\bar{\ell}'$ .

Inclusive  $H \rightarrow \gamma\gamma$  signals are difficult to see above large backgrounds from  $gg, q\bar{q} \rightarrow \gamma\gamma$  production and also from  $jet + jet$  and  $jet + \gamma$  states where  $jet \rightarrow \pi^0$  fakes  $\gamma$ . To extract a signal requires excellent mass resolution  $\delta M_{\gamma\gamma} < 1.5$  GeV and rejection factor  $R(jet \rightarrow fake \gamma) < 10^{-4}$  (see GEM studies for SSC[2]). Fig.4 shows typical predicted  $M_{\gamma\gamma}$  distributions, before and after background subtraction. Note the very low signal/background ratios here, requiring very high statistics.

Lepton-tagged  $H \rightarrow \gamma\gamma$  signals, based on the  $t\bar{t}H$  and  $WH$  production channels, are smaller but much cleaner since the lepton requirement strongly suppresses backgrounds, so less stringent mass resolution  $\delta M_{\gamma\gamma} < 3$  GeV and rejection factor  $R(jet \rightarrow fake \gamma) < 5 \times 10^{-4}$  may suffice (see SDC studies for SSC[3]). Fig.5 shows typical  $M_{\gamma\gamma}$  signal and background distributions.

Four-lepton signals, based on  $H \rightarrow ZZ^*$  decays with one Z off-shell, are also very clean and have a big enough branching fraction for  $m_H > 120$  GeV - see Fig.3; the dip near  $m_H = 2M_W = 160$  GeV is due to competition from the  $H \rightarrow W^+W^-$  channel that opens here. After suitable  $p_T$  and isolation cuts on the leptons, the backgrounds from continuum  $ZZ^*$ ,  $Zb\bar{b}$ ,  $Zt\bar{t}$  and  $t\bar{t}$  production are small; Fig.6 shows typical signal and background curves for an SSC example[3].

Very recently it has been argued that  $H \rightarrow b\bar{b}$  dijet signals may be detectable after all, with the backgrounds sufficiently suppressed by suitable tagging.

- (a) Tag two leptonic W-decays in the  $gg \rightarrow t\bar{t}H \rightarrow (bW^+)(\bar{b}W^-)(b\bar{b})$  channel; this gives a 2-lepton + 4-jet + missing- $E_T$  signature, with a peak at  $m_H$  in the dijet invariant mass  $m(jj)$  distribution[4]. There is a combinatorial background (from



‘wrong’ dijet pairings) and a much bigger background from  $t\bar{t}jj$  production; a narrow peak from  $t\bar{t}Z$  production also has to be calculated and subtracted; but the SSC illustration in Fig.7 suggests this approach could possibly work.

(b) Tag 3 or 4  $b$ -jets in the  $gg \rightarrow t\bar{t}H \rightarrow (bW^+)(\bar{b}W^-)(b\bar{b})$  channel, using a microvertex detector to pick out the displaced vertices from  $b$ -decays, and look for a peak in the  $2b$  invariant mass spectrum[5]. With sufficiently high  $b$ -tag efficiency and purity, all background channels except  $t\bar{t}Z$  (with  $Z \rightarrow b\bar{b}$ ) and  $t\bar{t}b\bar{b}$  are suppressed. Fig.8 shows an SSC illustration with 3- $b$ -tagging; the upper curves assume tagging efficiencies  $\epsilon_b = 0.4$  and  $\epsilon_g = 0.005$  for  $b$ -jets and gluon-jets, respectively; the lower curves (displaced by 100 units) assume values 0.3 and 0.01 instead. Note once more the low signal/background ratios, requiring high statistics in this game ! For LHC, taking  $m_H = 100$  GeV and  $m_t = 140$  GeV and the less optimistic tagging efficiencies, we need integrated luminosity  $L = 200 fb^{-1}$  to get a signal  $S = 600$  events over a background  $B = 14000$  events with statistical significance  $S/\sqrt{B} = 5$  standard deviations. But the situation improves if  $t$  is heavier; with  $m_t = 180$  GeV,  $L = 60 fb^{-1}$  is enough to give  $S = 210$ ,  $B = 1800$ , and  $S/\sqrt{B} = 5$  again[5].

(c) Rapidity-gap tagging may also work[6]. The  $qq \rightarrow qqH$  mechanism has no colour exchange and is therefore unlikely to radiate additional soft gluons or  $q\bar{q}$  pairs in the central region, unlike the other  $H$  production processes or typical background channels. By requiring that there is no particle production (apart from an  $H \rightarrow b\bar{b}$  dijet candidate) in a wide central interval of rapidity, it may be possible to suppress backgrounds enough to extract a  $qq \rightarrow qqH, H \rightarrow b\bar{b}$  dijet signal. But such rapidity gaps can get filled in by soft interactions of spectator partons (‘the underlying event’), or faked by statistical fluctuations. Detailed studies are needed[6]; the intermediate-mass Higgs case has received little attention so far[7].

We see that one or other of the popular  $\gamma\gamma$  and 4-lepton signals should be detectable across the whole intermediate mass range  $M_Z < m_H < 2M_Z$ . New ideas make the  $b\bar{b}$  dijet signal appear promising too, at least in the lower part of the range.

## 2.2 Heavy Higgs searches.

For heavy Higgses ( $m_H > 2M_Z$ ), the decay chain  $H \rightarrow ZZ \rightarrow 4\ell$  offers a very clean ‘gold-plated’ signal with a nice peak in the invariant mass  $m(\ell\ell\ell\ell)$  and relatively little background, mostly from continuum  $ZZ$  production. Fig.9 shows cross sections for this signal versus  $m_H$ ; note that they are an order of magnitude smaller at LHC than at the late lamented SSC, requiring that much more luminosity. Fig.10 shows the mass peaks for  $m_H = 600$  and 800 GeV at LHC after suitable cuts[8]. We see that the mass peak broadens and becomes harder to detect as  $m_H$  increases; in fact

$$\Gamma_H \simeq (0.5 TeV)(m_H/1 TeV)^3.$$

Thus the range  $m_H < 0.6$  TeV is relatively easy;  $m_H > 0.8$  TeV is hard.

An alternative ‘silver-plated’  $H \rightarrow ZZ \rightarrow (\ell^+\ell^-)(\nu\bar{\nu})$  signal is also promising. It has a somewhat less clean signature, namely one leptonic  $Z$  plus missing- $E_T$ , but

has six times bigger branching fraction than the gold-plated signal - which could be helpful at large  $m_H$ . The main backgrounds from  $Z + jets$ ,  $t\bar{t}$  and  $ZZ$  continuum production can be suppressed by suitable cuts, especially by requiring large missing- $E_T$ , since the  $H \rightarrow ZZ$  decay gives a Jacobian peak near  $p_T(Z) = \frac{1}{2}\sqrt{m_H^2 - 4M_Z^2}$  that translates into a peak in missing- $E_T$ ; see Fig.11. The mass  $m_H$  can be estimated from the missing- $E_T$  distribution, but a cleaner estimate (from a narrower peak) can be made using the ‘transverse mass’ variable  $m_T(\ell\ell, \nu\nu)$ [9] defined by

$$m_T(\ell\ell, \nu\nu)^2 = [\sqrt{p_T(\ell\ell)^2 + M_Z^2} + \sqrt{p_T(\nu\nu)^2 + M_Z^2}]^2 - [\vec{p}_T(\ell\ell) + \vec{p}_T(\nu\nu)]^2$$

where  $\vec{p}_T(\nu\nu) = \vec{E}_T$ -missing. Both  $p_T(\ell\ell)$  and  $p_T(\nu\nu)$  have Jacobian peaks that are smeared by the transverse motion of  $H$ , but this smearing approximately cancels in the combination  $m_T$ .

The  $H \rightarrow W^+W^- \rightarrow (\ell\nu)(\ell'\nu')$  signal has the biggest branching fraction of the all-leptonic modes; the signature is two isolated large- $p_T$  leptons plus missing- $E_T$ , but there is a horrendous background from  $t\bar{t} \rightarrow bW^+\bar{b}W^-$ . A strategy of jet-tagging and anti-tagging (vetoing) has been proposed to rescue this signal. Note first that the important  $qq \rightarrow qqH$  production subprocess (see Figs.1 and 2) contains two jets with typically large pseudo-rapidity  $|\eta| \sim 3 - 5$ , but no central jets when  $H \rightarrow \ell\nu\ell'\nu'$ . In contrast, the QCD background process  $gg, q\bar{q} \rightarrow t\bar{t} \rightarrow bW^+\bar{b}W^-$  contains typically no forward jets but has two central  $b$ -jets. Hence, by requiring at least one forward jet with  $3 < |\eta| < 5$  and no central jet with  $|\eta| < 3$ , the background can be suppressed relative to the signal. [Jet tagging/vetoing can help to reduce backgrounds to the previous  $H \rightarrow ZZ$  signals also]. It has been shown that the  $H \rightarrow WW$  signal can be separated by these and other suitable cuts, at least for  $0.6 \lesssim m_H \lesssim 1$  TeV[10]. The mass  $m_H$  can then be estimated from the dilepton invariant mass  $m(\ell\ell')$  or another transverse mass  $m(\ell\ell', \nu\nu')$  defined by[11]

$$m_T(\ell\ell', \nu\nu')^2 = [\sqrt{p_T(\ell\ell')^2 + m(\ell\ell')^2} + p_T(\nu\nu')]^2 - [\vec{p}_T(\ell\ell') + \vec{p}_T(\nu\nu')]^2$$

where  $\vec{p}_T(\nu\nu') = \vec{E}_T$ -missing; this differs from the previous transverse mass variable because we no longer have the constraints  $m(\ell\ell) = m(\nu\nu) = M_Z$  and indeed  $m(\nu\nu')$  cannot be measured. These variables peak at  $m(\ell\ell') \simeq \frac{1}{2}m_H$  and  $m_T(\ell\ell', \nu\nu') \simeq \frac{3}{4}m_H$ , respectively.

Combining the coverage of  $H \rightarrow ZZ \rightarrow 4\ell$ ,  $H \rightarrow ZZ \rightarrow 2\ell 2\nu$  and  $H \rightarrow WW \rightarrow 2\ell 2\nu$  signals, we see that heavy Higgses will be detectable for  $m_H \lesssim 1$  TeV.

### 2.3. Studying Higgs couplings separately.

In principle, the strengths of  $H$  couplings to  $WW$ ,  $ZZ$ ,  $t\bar{t}$ ,  $b\bar{b}$  can be separated in various ways; examples follow. Note that the signal rate in each particular channel has the general form

$$\sigma(pp \rightarrow H \rightarrow channel) = \sigma(pp \rightarrow H) \times \Gamma(H \rightarrow channel)/\Gamma_H$$

(a) The dominant untagged or lepton-tagged  $\gamma\gamma$  signals depend directly on the  $Ht\bar{t}$  coupling, both at the  $H$  production vertex ( $t$ -quark loop or associated production with  $t\bar{t}$ ) and at the  $H$  decay (via  $t$ -quark loop), but the total decay width in the denominator is dominated by  $Hb\bar{b}$  at the relevant low-intermediate masses. Thus the rate determines  $(Ht\bar{t})^4/(Hb\bar{b})^2$  approximately.

(b) If the  $WH$  and  $t\bar{t}H$  lepton-tagged  $\gamma\gamma$  signals can be separated via final-state criteria, their ratio will determine

$$(WH \rightarrow \gamma\gamma \text{ rate})/(t\bar{t}H \rightarrow \gamma\gamma \text{ rate}) \sim (HWW)^2/(Ht\bar{t})^2$$

(c) The  $t\bar{t}H \rightarrow t\bar{t}(b\bar{b})$  tagged dijet signals depend on the  $Ht\bar{t}$  coupling for  $H$  production, with branching fraction  $B(H \rightarrow b\bar{b}) \sim 1$  for decay. Thus the signal rate determines  $(Ht\bar{t})^2$  approximately, and the ratio to  $\gamma\gamma$  rates determines

$$(\text{tagged } bb \text{ dijet rate})/(\gamma\gamma \text{ rate}) \sim (Hb\bar{b})^2/(Ht\bar{t})^2.$$

(d) For high-intermediate masses  $m_H > 120$  GeV, the total width  $\Gamma_H$  depends non-trivially on  $Hb\bar{b}$ ,  $HWW$  and  $HZZ$  couplings, so nothing simple can be said about the  $H \rightarrow 4\ell$  signals here

(e) For heavy Higgses, the ratio of  $WW/ZZ$  signals could determine the ratio of  $(HWW)/(HZZ)$  couplings.

(f) The ratio of jet-tagged/untagged heavy Higgs signals could determine the ratio of  $qq \rightarrow qqH$  and  $gg \rightarrow H$  production mechanisms, that depends directly on the  $(HV\bar{V})/(Ht\bar{t})$  coupling ratio, where  $V = W, Z$  but  $W$  dominates.

(g)  $\Gamma_H$  for a heavy Higgs, directly measurable from the width of the mass peak, should be dominated by the  $HWW$  coupling with smaller contributions from  $HZZ$  and  $Ht\bar{t}$ .

### 3. WW, WZ AND ZZ SCATTERING.

In the SM, the coupling strength of the scalar potential is

$$\lambda = \frac{m_H^2}{2v^2} = \left[ \frac{m_H}{348 \text{ GeV}} \right]^2$$

which is large if  $H$  is heavy, implying strong scattering of the Goldstone bosons  $w^\pm$  and  $z$  that become  $W_L^\pm$  and  $Z_L$ . This can also happen more generally, outside the SM. Figure 12 shows a generic  $W_L, Z_L$  scattering process at LHC. Different final states are sensitive to different physics:  $W_L^+ W_L^-$  and  $Z_L Z_L$  states probe Higgs-like resonances;  $W_L^+ W_L^+$  and  $W_L^- W_L^-$  states probe non-resonant scattering (except in some exotic models);  $W_L Z_L$  states probe techni- $\rho$ -type resonances.

The idea is that enhanced  $WW, WZ, ZZ$  production may be attributed to strong  $W_L$  and  $Z_L$  scattering, since the transversely polarized states  $W_T$  and  $Z_T$  only have the weak  $SU(2) \times U(1)$  gauge interactions. Details of the enhancement will shed light on EWSB. To discuss this scattering, we must first introduce a number of ideas, approximations and constraints.

### 3.1 The effective W approximation (EWA).

In analogy with the Weizsäcker-Williams approximation for photons, the incident quark beams can be replaced by beams of approximately on-shell  $W$  and  $Z$  bosons. Writing  $P_{W/q}^\alpha(x)$  as the known probability distribution (splitting function) for finding a  $W$  with polarization  $\alpha$  and momentum fraction  $x$  in quark  $q$ , the subprocess cross section for  $q_1 q_2 \rightarrow q_3 q_4 W_3^\gamma W_4^\delta$  is

$$\sigma(q_1 q_2 \rightarrow q_3 q_4 W_3^\gamma W_4^\delta) = \sum_{\alpha, \beta} \int dx_1 dx_2 P_{W_1/q_1}^\alpha(x_1) P_{W_2/q_2}^\beta(x_2) \sigma(W_1^\alpha W_2^\beta \rightarrow W_3^\gamma W_4^\delta)$$

The physical cross section for  $pp \rightarrow q_3 q_4 W_3 W_4 X$  is found by further integrating over incident quark distributions and summing over final  $W$  spins. The splitting functions for  $W_L$  and  $Z_L$  are

$$P_{W^+/u}^L = P_{W^-/d}^L = P_{W^+/\bar{d}}^L = P_{W^-/\bar{u}}^L = \frac{g^2}{16\pi^2} \frac{(1-x)}{x},$$

$$P_{Z/q}^L = P_{Z/\bar{q}}^L = \frac{g^2}{32\pi^2} \frac{1 - 4x_W |Q| + 8x_W^2 Q^2 (1-x)}{1-x_W} \frac{(1-x)}{x},$$

where  $x_W = \sin^2 \theta_W = 0.23$ ,  $Q$  is the electric charge of quark  $q$  and  $g^2 = 8M_W^2 G_F / \sqrt{2}$  is the  $SU(2)$  gauge coupling squared. The EWA is the only known way to separate the contributions of  $W_L$  and  $Z_L$  scattering in a high energy process. The approximation is collinear and neglects transverse momenta for the initial  $W_1, W_2$  and for the recoiling quarks  $q_3, q_4$ .

### 3.2 The Goldstone Boson Equivalence Theorem (GBET).

This theorem[12] relates any scattering amplitude for real  $W_L$  and  $Z_L$  to the amplitude for the corresponding Goldstone bosons  $w$  and  $z$ :

$$M[W_L(p_1), W_L(p_2), \dots] = M[w(p_1), w(p_2), \dots]_R + \mathcal{O}(M_W/E_W),$$

where  $R$  indicates a renormalizable  $R_\xi$  gauge. The  $p_i$  are momenta (masses are neglected here). The EWA provides essentially real incoming  $W_L$  and  $Z_L$ ; the GBET allows us to compute their scattering from any given model of the Goldstone boson sector, up to corrections of order  $M_W/E_W$ .

### 3.3 Isospin, crossing and unitarity.

The various  $ww$ ,  $wz$  and  $zz$  scattering amplitudes are all related by  $SU(2)$  isospin and crossing symmetries, just like  $\pi\pi$  scattering. In terms of components  $w_i$  ( $i = 1, 2, 3$ ;  $w^\pm = (w_1 \mp w_2)/\sqrt{2}$ ,  $z = w_3$ ), the general amplitude has the form

$$M(w_a w_b \rightarrow w_c w_d) = A(s, t, u) \delta_{ab} \delta_{cd} + A(t, s, u) \delta_{ac} \delta_{bd} + A(u, t, s) \delta_{ad} \delta_{bc},$$

where  $s = (p_a + p_b)^2$ ,  $t = (p_a - p_c)^2$ ,  $u = (p_a - p_d)^2$  and  $A$  is symmetrical in its last two arguments:  $A(s, t, u) = A(s, u, t)$ . In terms of this single basic amplitude  $A$ , the various channel amplitudes are

$$\begin{aligned} M(w^+ w^- \rightarrow w^+ w^-) &= A(s, t, u) + A(t, s, u), \\ M(w^+ w^- \rightarrow z z) &= A(s, t, u), \\ M(z z \rightarrow z z) &= A(s, t, u) + A(t, s, u) + A(u, t, s), \\ M(w^\pm z \rightarrow w^\pm z) &= A(t, s, u), \\ M(w^+ w^+ \rightarrow w^+ w^+) &= A(t, s, u) + A(u, t, s). \end{aligned}$$

The amplitudes for s-channel isospin  $T = 0, 1, 2$  are

$$\begin{aligned} M(T = 0) &= 3A(s, t, u) + A(t, s, u) + A(u, t, s), \\ M(T = 1) &= A(t, s, u) - A(u, t, s), \\ M(T = 2) &= A(t, s, u) + A(u, t, s). \end{aligned}$$

These pure-isospin channels diagonalize the S-matrix, so their s-channel partial wave amplitudes  $a_L^T$  defined by

$$M(T) = 32\pi \sum_L (2L + 1) a_L^T P_L(\cos \theta)$$

should satisfy the unitarity condition  $|2a_L^T - i| \leq 1$ , i.e. lie within a circle in the complex plane.

### 3.4 Low energy theorem (LET).

In the low-energy limit, Goldstone boson scattering is expected to be controlled by the dynamics of EWSB. Since EWSB in the SM is essentially the non-linear sigma model with chiral  $SU(2) \times SU(2)$  symmetry, it has been pointed out[13] that the low-energy theorems of  $\pi\pi$  scattering[14] can be directly applied to the case of  $w$  and  $z$  scattering, simply replacing the pion decay constant  $F_\pi = 94$  MeV by the vev  $v = 246$  GeV. Hence in all channels the threshold behaviour is approximately specified by  $v$ :

$$A(s, t, u) \simeq s/v^2.$$

Hence the low-energy partial wave amplitudes are

$$a_0^0 = \frac{s}{16\pi v^2}, \quad a_1^1 = \frac{s}{96\pi v^2}, \quad a_0^2 = -\frac{s}{32\pi v^2}.$$

This linear rise with  $s$  cannot be extrapolated indefinitely without violating unitarity. Strictly speaking, since these formulae give purely real  $a_L^T$ , any non-zero value lies outside the unitarity circle, but this could at first be cured by adding a small imaginary part. However, the real part of  $a_0^0$  exceeds its unitarity limit  $\Re a_L^T \leq \frac{1}{2}$  when  $\sqrt{s} >$

$\sqrt{8\pi}v = 1.2$  TeV, while the  $T=2$  amplitude exceeds this limit for  $\sqrt{s} > 1.7$  TeV. We see that unitarity is likely to be an important constraint in the TeV range.

### 3.5 Models for Goldstone boson scattering.

A wide variety of models have been proposed, to illustrate and parameterize the scattering of  $w^\pm$  and  $z$ . We confine ourselves here to the models evaluated in a recent survey by Bagger et al[15] of possible strong  $WW$ ,  $WZ$ ,  $ZZ$  scattering at hadron colliders.

(i) Standard Model.

This gives the form

$$A(s, t, u) = \frac{-m_H^2}{v^2} \left( 1 + \frac{m_H^2}{s - m_H^2 + im_H \Gamma_H \theta(s)} \right),$$

where  $m_H$  is the Higgs mass,  $v = 246$  GeV is the usual vev, and a Breit-Wigner form has been imposed for the Higgs resonance.  $\theta$  is the step-function:  $\theta(s) = 1(0)$  for  $s > 0(s \leq 0)$ .  $A(t, s, u)$  and  $A(u, t, s)$  are obtained by permuting  $s, t, u$ . For illustration we shall take  $m_H = 1$  TeV[15].

(ii)  $O(2N)$  Model [16].

Motivated by the isomorphism between  $SU(2)_L \times SU(2)_R$  and  $O(4)$  symmetries, and using a large- $N$  approximation, this model gives

$$A(s, t, u) = \frac{16\pi^2 s}{16\pi^2 v^2 - sN[2 + \ln(\Lambda^2/|s|) + i\pi\theta(s)]},$$

where  $\theta(s)$  is the step-function as before. Following Ref.[15], we take the case  $N = 2$  with physical cut-off  $\Lambda = 3$  TeV.

(iii) Chirally-Coupled Scalar Model[15].

This model describes the low-energy behaviour of a technicolor-type model with a techni-sigma scalar resonance, through the amplitude

$$A(s, t, u) = \frac{s}{v^2} - \left( \frac{g^2 s^2}{v^2} \right) \frac{1}{s - M_S^2 + iM_S \Gamma_S \theta(s)},$$

where  $M_S$  and  $\Gamma_S$  are the scalar resonance mass and its decay width into Goldstone fields,  $\Gamma_S = 3g^2 M_S^3 / (32\pi v^2)$ . We choose  $M_S = 1.0$  TeV and  $\Gamma_S = 0.35$  TeV, following Ref.[15].

(iv) Chirally-Coupled Vector Model[15, 17].

This model describes the low-energy behaviour of a technicolor-type model with a techni-rho vector resonance, through the amplitude

$$A(s, t, u) = \frac{s}{4v^2} (4 - 3a) + \frac{aM_V^2}{4v^2} \left[ \frac{u - s}{t - M_V^2 + iM_V \Gamma_V \theta(t)} + \frac{t - s}{u - M_V^2 + iM_V \Gamma_V \theta(u)} \right],$$

where  $M_V$  and  $\Gamma_V$  are the vector resonance mass and width while  $a = 192\pi v^2 \Gamma_V / M_V^3$ . We choose the two cases  $M_V = 2.0$  TeV with  $\Gamma_V = 0.7$  TeV and  $M_V = 2.5$  TeV with  $\Gamma_V = 1.3$  TeV, following Ref.[15].

(v) LET-CG Model[13]

This model simply extrapolates the low-energy amplitudes, prescribed by low-energy theorems (LET) in terms of the vev  $v$ :

$$A(s, t, u) = s/v^2.$$

These amplitudes eventually violate unitarity, as we saw above, so the partial wave amplitudes are held constant after they reach the bound  $|a_L^T| \leq 1$  (less stringent than the bound  $\Re a_L^T \leq \frac{1}{2}$  we mentioned earlier).

(vi) LET-K Model[18].

Here the LET amplitudes above are unitarized instead by the K-matrix prescription,

$$a_L^T \rightarrow a_L^T / (1 - ia_L^T),$$

that enforces the elastic unitarity condition  $|2a_L^T - i| = 1$ .

(vii) Delay-K Model[15].

This is an example of non-resonant models, based on an effective Lagrangian method[19]. To order  $p^4$  in the momentum expansion, all model amplitudes have the form

$$A(s, t, u) = \frac{s}{v^2} + \frac{1}{4\pi^2 v^4} (2L_1(\mu)s^2 + L_2(\mu)(t^2 + u^2)) + \frac{1}{16\pi^2 v^4} \left[ -\frac{t}{6}(s+2t) \ln\left(\frac{-t}{\mu^2}\right) - \frac{u}{6}(s+2u) \ln\left(\frac{-u}{\mu^2}\right) - \frac{s^2}{2} \ln\left(\frac{-s}{\mu^2}\right) \right],$$

where  $\mu$  is the renormalization scale and  $L_i(\mu)$  are renormalized coefficients in the effective Lagrangian. The parameters  $L_1(\mu)$ ,  $L_2(\mu)$  and  $\mu$  essentially cover all possible non-resonant physics in this approximation. Following Ref.[15] we choose the example  $L_1(\mu) = -0.26$ ,  $L_2(\mu) = 0.23$  with  $\mu = 1.5$  TeV, for which unitarity breakdown is delayed until  $\sqrt{s} = 2$  TeV. These amplitudes are complex; for simplicity, unitarity is imposed by the K-matrix prescription based on the real part of  $a_L^T$ , i.e.  $a_L^T \rightarrow \Re a_L^T / (1 - i\Re a_L^T)$ .

### 3.6 Model results

At a hadron collider we can only hope to recognize  $W \rightarrow \ell\nu$  and  $Z \rightarrow \ell\ell$  leptonic final states in the face of QCD multijet backgrounds. Even so, there remain backgrounds from electroweak  $W$  and  $Z$  production, from Drell-Yan lepton pairs and from the semileptonic decays of heavy quarks. Selection cuts to enhance signal/background include lepton isolation, high lepton  $p_T$ , central leptons with  $|\eta(\ell)| \lesssim 2$ , high invariant mass  $m(\ell\ell')$  for  $WW$  and  $m(ZZ)$  for  $ZZ$ ; in  $WW$  cases it also helps to require the two leptons to be back-to-back in azimuth and have high relative momentum.



Finally, it can be helpful to tag one of the spectator jets and/or veto central jets with  $|\eta(j)| < 3$  (as in Section 2.2 for heavy Higgs searches). The following table shows results from Ref.[15] for the LHC, with typical realistic cuts. The signals here are the total production of  $W_L W_L \rightarrow \ell \nu \ell \nu$  (etc); the background column (Bkgd) includes SM production of  $W_T W_T$ ,  $W_T W_L$  (etc) calculated using small  $m_H$ .

Events for luminosity  $100 fb^{-1}$ , assuming  $m_t = 140$  GeV,  $\sqrt{s} = 16$  TeV.

| Case      | Bkgd | SM  | Scalar | $O(2N)$ | Vec2.0 | Vec2.5 | LET CG | LET K | Delay K |
|-----------|------|-----|--------|---------|--------|--------|--------|-------|---------|
| $ZZ$      | 0.1  | 3.9 | 2.7    | 1.8     | 0.4    | 0.6    | 1.1    | 0.9   | 0.6     |
| $W^+ W^-$ | 15   | 32  | 21     | 16      | 7.4    | 6.1    | 8.3    | 6.3   | 5.5     |
| $W^+ Z$   | 0.3  | 0.3 | 0.4    | 0.3     | 3.3    | 1.8    | 1.6    | 1.4   | 1.7     |
| $W^+ W^+$ | 1.7  | 3.7 | 5.2    | 4.3     | 4.8    | 7.3    | 16     | 14    | 8.3     |

We see that every model predicts a signal in at least one channel, although more luminosity would be desirable, and that the different channels are helpfully complementary. There seem to be good prospects for probing EWSB via weak boson scattering.

Fig.13 illustrates some of the more promising signals versus invariant mass  $m(ZZ)$  for  $ZZ$ ,  $m(\ell\ell')$  for  $WW$  and a suitable  $ll\nu$  transverse mass variable  $m_T$  for  $WZ$  cases [15]. These illustrations are for the defunct SSC, but something similar should hold for LHC.

#### 4. SUSY HIGGS POSSIBILITIES AT LEP AND LHC.

The Higgs sector is the shakiest part of the SM, where something extra may well be added. Let us consider the new degrees of freedom coming from some possible extensions[1].

(a) SM has one complex scalar doublet  $\phi$  with vev  $\sqrt{2} \langle \phi^0 \rangle = v = 246$  GeV. Its 4 degrees of freedom show up as  $W_L^+$ ,  $W_L^-$ ,  $Z_L$  and  $H^0$ . There is just 1 free parameter  $m_H$  in the scalar sector.

(b) MSSM (minimal SUSY SM) has two scalar doublets with  $\sqrt{2} \langle \phi_1^0 \rangle = v \cos \beta$  and  $\sqrt{2} \langle \phi_2^0 \rangle = v \sin \beta$ . Their 8 degrees of freedom show up as  $W_L^+$ ,  $W_L^-$ ,  $Z_L$  plus five spin-0 Higgs bosons  $h^0$ ,  $H^0$ ,  $A^0$ ,  $H^+$ ,  $H^-$ .  $h^0$  and  $H^0$  have  $CP = +1$  (by convention  $m_h < m_H$ ) and  $A$  has  $CP = -1$ . There are now 2 free parameters, often taken to be  $m_A$  and  $\tan \beta = v_2/v_1$ .

(c) NMSSM (next-to-minimal SUSY SM) has an extra neutral singlet scalar field  $n$  with vev  $\langle n \rangle = x$  non-zero but free. The 10 degrees of freedom show up as  $W_L^+$ ,  $W_L^-$ ,  $Z_L$  plus seven spin-0 Higgs bosons  $h^0$ ,  $H_1^0$ ,  $H_2^0$ ,  $A_1^0$ ,  $A_2^0$ ,  $H^+$ ,  $H^-$  (where  $A_1$  and  $A_2$  have  $CP = -1$ ). The number of free parameters now jumps to 6, however, because there are suddenly many more possible terms in the general scalar potential. This model has a richer spectrum and also looser limits.

For today we shall concentrate on the more constrained example of MSSM.

##### 4.1 MSSM at tree level.



All MSSM Higgs masses and couplings, plus a mixing angle  $\alpha$  that relates  $h$  and  $H$  to  $\Re\phi_1$  and  $\Re\phi_2$ , are determined at tree level by  $m_A$  and  $\tan\beta$ :

$$\begin{aligned}\tan 2\alpha &= \tan 2\beta (m_A^2 + M_Z^2)/(m_A^2 - M_Z^2) \\ m_h^2, m_H^2 &= \frac{1}{2}[m_A^2 + M_Z^2 \mp \sqrt{(m_A^2 + M_Z^2)^2 - 4m_A^2 M_Z^2 \cos^2 2\beta}] \\ m_{H^\pm}^2 &= m_A^2 + M_W^2\end{aligned}$$

with  $-\frac{\pi}{2} \leq \alpha \leq 0$ . Hence at tree level

$$m_h \leq M_Z, m_A; m_H \geq M_Z; m_{H^\pm} \geq M_W, m_A.$$

Thus there is always at least one Higgs boson  $h$  lighter than  $Z$ . However, in the limit  $m_A \gg m_Z$ , all the other bosons  $H$ ,  $A$  and  $H^\pm$  become very heavy and approximately degenerate while  $m_h \simeq M_Z \cos 2\beta$ , so it is conceivable that only this one light boson may be accessible.

#### 4.2 MSSM with radiative corrections.

MSSM Higgs physics does not depend only on the scalar-sector parameters  $m_A$  and  $\tan\beta$ , but also has important loop corrections because the top quark is so heavy (Fig.14). These radiative corrections depend on  $m_t$ ,  $m_{\tilde{t}}$  (the mean  $t$ -squark mass),  $m_Q$ ,  $m_U$  and  $m_D$  (soft SUSY-breaking squark masses),  $A_t$  and  $A_b$  (coefficients of trilinear  $\tilde{t}_L \tilde{t}_R \phi_2$  and  $\tilde{b}_L \tilde{b}_R \phi_1$  soft SUSY-breaking terms), and  $\mu$  (coefficient of  $\phi_1 \phi_2$  mixing in the superpotential); see e.g. Ref.[20]. This dependence is mainly on  $m_t$  and (logarithmically) on  $m_{\tilde{t}}$ ; neglecting the other parameters, the upper limit on  $m_h$  becomes

$$m_h^2 \leq M_Z^2 + \frac{3g^2 m_t^4}{4\pi^2 M_W^2} \ln(m_{\tilde{t}}/m_t),$$

in one-loop approximation.

In the following we shall estimate these radiative corrections by assuming that  $m_t \simeq 150$  GeV,  $m_{\tilde{t}} \simeq 1$  TeV, and that squark mixing is moderate (explicitly  $m_Q = m_U = m_D = 2A_t = 2A_b = 4\mu = 1$  TeV, following Ref.[21]). With this choice, the  $m_h$  upper limit is  $m_h \lesssim 115$  GeV; the full dependence of  $m_h$ ,  $m_H$  and  $m_{H^\pm}$  on the remaining parameters  $m_A$  and  $\tan\beta$  is shown in Fig.15[21]. Searches for  $h$  at LEP1 (via  $e^+e^- \rightarrow Zh, Ah$ ) have already covered the region  $m_h \lesssim 50$  GeV, depending somewhat on  $\tan\beta$ ; the higher energy  $\sqrt{s} \sim 170 - 190$  GeV at LEP2 will arguably allow searches up to  $m_h \sim 90$  GeV; but Fig.15 shows there is a large region of parameter space ( $m_A \gtrsim 90$  GeV,  $\tan\beta \gtrsim 2$ ) where  $h$  and all the heavier Higgses could be hiding undetected. This is LHC territory.

Compared to the SM Higgs coupling to fermions and gauge bosons, given by  $L = -(m_i/v)\bar{f}_i f_i H + \frac{1}{2}g^2 v W W H + \frac{1}{4}(g^2 + g'^2)v Z Z H$ , the MSSM neutral Higgs couplings

have the following extra factors:

|                            | $h$                         | $H$                        | $A$                     |
|----------------------------|-----------------------------|----------------------------|-------------------------|
| $t\bar{t}$                 | $\cos \alpha / \sin \beta$  | $\sin \alpha / \sin \beta$ | $-i\gamma_5 \cot \beta$ |
| $b\bar{b}, \tau\bar{\tau}$ | $-\sin \alpha / \cos \beta$ | $\cos \alpha / \cos \beta$ | $-i\gamma_5 \tan \beta$ |
| $WW, ZZ$                   | $\sin(\beta - \alpha)$      | $\cos(\beta - \alpha)$     |                         |
| $ZA$                       | $\cos(\beta - \alpha)$      | $\sin(\beta - \alpha)$     |                         |

We see that  $h$  and  $H$  share their coupling strengths, that  $A$  does not couple directly to  $WW$ ,  $ZZ$  or  $ZA$ , and that for large  $\tan \beta$  (small  $\cos \beta$ ) all the  $b\bar{b}$  couplings are greatly enhanced. These coupling factors vary enormously as  $\alpha$  varies, across the  $(m_A, \tan \beta)$  plane.

The charged scalars  $H^\pm$  couple to typical fermions by

$$L = \frac{g}{2\sqrt{2}M_W} H^+ [m_t V_{tb} \cot \beta \bar{t}(1 - \gamma_5)b + m_b V_{tb} \tan \beta \bar{t}(1 + \gamma_5)b + m_c V_{cs} \cot \beta \bar{c}(1 - \gamma_5)s + m_\tau \tan \beta \bar{\nu}(1 + \gamma_5)\tau],$$

but have no tree-level coupling to  $WZ$ .

These new coupling factors and new kinds of coupling show that the production and decay of MSSM Higgses are not just trivial extensions of the SM situation, in general. There is however one particularly simple region, where  $m_A$  becomes large ( $\gtrsim 300$  GeV); here  $A$ ,  $H$  and  $H^\pm$  become approximately degenerate,  $\alpha$  approaches  $\beta - \pi/2$ , and all  $h$  couplings approach SM values. In this region,  $h$  fakes  $H_{SM}$  while the heavier Higgses are largely irrelevant; we essentially recover the SM but with the extra constraint  $m_h \lesssim 130$  GeV (from MSSM with radiative corrections), whereas the SM alone has a much weaker bound  $m_{H_{SM}} \lesssim 600 - 1000$  GeV from triviality and perturbative-unitarity considerations.

### 4.3 Parameter constraints.

What are the constraints on the MSSM parameters  $\tan \beta$  and  $m_A$ ?

- (a) Requiring the charged-Higgs couplings to  $t\bar{b}$  above to remain perturbative gives  $m_t/500\text{GeV} \lesssim \tan \beta \lesssim 500\text{GeV}/m_b$  [22]; the precise limits are somewhat subjective. Essentially, values  $\tan \beta \ll 1$  and  $\tan \beta \gg 30$  are disfavoured.
- (b) Proton decay sets limits in SUSY-GUT models, typically  $\tan \beta \lesssim 85$  [23].
- (c) Since up-type (down-type) quarks get their masses via the vev  $v_2$  ( $v_1$ ), the empirical mass hierarchy  $m_c \gg m_s$  and  $m_t \gg m_b$  suggests a corresponding hierarchy of vevs  $v_2 \gg v_1$ , i.e.  $\tan \beta \gg 1$  [24].
- (d) SUSY-GUT models generally find solutions with  $1 \lesssim \tan \beta \lesssim m_t/m_b$ . For example, Ref.[25] obtains solutions with  $2 < \tan \beta < 40$  while Ref.[26] finds solutions in the range  $0.6 < \tan \beta < 60$ .
- (e) SUSY-GUT models where electroweak symmetry is broken radiatively (a Higgs mass-square goes negative during evolution downward from the GUT scale) require

$\tan\beta > 1$  (see e.g. Ref.[25]).

The consensus on  $\tan\beta$  is therefore

$$0 \lesssim \tan\beta \lesssim 60.$$

What now about the other parameter,  $m_A$  ?

(f) Higgs boson searches at LEP1 give  $20 \text{ GeV} \lesssim m_A$  (assuming  $\tan\beta > 1$ ).

(g) In SUSY-GUT models,  $m_A \lesssim M_{SUSY} \lesssim 1 - 2 \text{ TeV}$ .

(h) Global electroweak analysis in the MSSM finds a preferred value for  $m_A$  below 100 GeV or so, but much larger values are not excluded [27].

The consensus on  $m_A$  is therefore

$$20 \text{ GeV} \lesssim m_A \lesssim 1 - 2 \text{ TeV}.$$

Various other indirect constraints should also be mentioned.

(i) LEP1 searches for  $e^+e^- \rightarrow H^+H^-$  exclude a parameter region with  $\tan\beta < 0$  [28].

(j) Virtual  $H^\pm$  can contribute to  $B \rightarrow \tau\nu X$ , but essentially not to  $B \rightarrow e\nu X$ ,  $\mu\nu X$ , breaking lepton universality. The ALEPH measurement of  $B(B \rightarrow \tau\nu X)$  sets a limit on this contribution and hence a bound  $\tan\beta < 0.54(m_H/1 \text{ GeV})$  [29]. This is not very stringent, because the virtual  $H^\pm$  and standard  $W^\pm$  contributions add incoherently, i.e. a 10% amplitude gives only a 1% correction.

(k) Virtual  $H^-t$  loop contributions to  $b \rightarrow s\gamma$  decays apparently offer a much more stringent constraint; they add coherently to the SM  $W^-t$  loop amplitudes. Neglecting possible additional SUSY loops, the present CLEO upper bound on  $B(B \rightarrow \gamma X) \simeq B(b \rightarrow s\gamma)$  gives rather strong lower bounds on the charged-Higgs mass and hence on regions of the  $(m_A, \tan\beta)$  plane [30]. However, in the present MSSM context we cannot ignore SUSY loops, especially chargino-stop loops, that can interfere strongly and destructively with the SM amplitude[31]. To apply this constraint we need more information about the sparticle spectrum, e.g. a complete SUSY-GUT model with all masses and mixings prescribed.

#### 4.4 MSSM Higgs production and decay at LHC.

Production and decay of neutral Higgses can proceed by the SM processes, modulo the additional factors discussed above. However, there are new non-SM decay modes like  $h \rightarrow AA$ ,  $H \rightarrow AZ$ ,  $H \rightarrow hh$ , that tend to dominate when kinematically allowed, blotting out the familiar SM signals in various regions of parameter space; see Fig.16. Note that  $H \rightarrow hh$  is allowed almost everywhere (except in the shaded region and along a dashed line where the  $Hhh$  coupling vanishes), making  $H$  usually hard to detect at LHC.

Production of charged Higgses is copious only via top production with  $t \rightarrow bH^+$  decays, when  $m_{H^\pm} < m_t - m_b$ ; in this case the principal decays are  $H^\pm \rightarrow cs, \tau\nu$  and the signal could be excess taus compared to other leptons [32]. But for heavier  $m_{H^\pm} > m_t$  there can still be signals from  $gg \rightarrow t\bar{b}H^-$  production with  $H^- \rightarrow b\bar{t}$  decay, leading to a  $b\bar{b}\bar{b}W^+W^-$  final state; multiple  $b$ -tagging is essential here[33].

There are regions of SUSY parameter space where SUSY decay modes like  $h \rightarrow \chi_1^0 \chi_1^0$  to lightest neutralino pairs are allowed; this is potentially dangerous since  $\chi_1^0$  is usually the lightest sparticle (LSP), stable, weakly interacting and essentially invisible. However, after LEP1 constraints there remains only a very small parameter range where this decay dominates; unless we are very unlucky, this may dilute the standard signals a bit but will not wash them out. Other decays like  $A \rightarrow \chi_2^0 \chi_2^0 \rightarrow (\ell^+ \ell^- \chi_1^0)(\ell^+ \ell^- \chi_1^0)$  might provide interesting new signals[34].

#### 4.5 Expected MSSM Higgs signals.

For neutral Higgses, the strategy has been first to think about SM-like signals in conventional  $\gamma\gamma$  and 4-lepton channels, and also in  $b\bar{b}$  and  $\tau\bar{\tau}$  channels;  $h$ ,  $H$  and  $A$  can all in principle give such signals. For charged Higgses, the emphasis has been mostly on  $t \rightarrow bH^+ \rightarrow b\tau\nu$  signals.

Four groups have made extensive calculations for LHC and SSC, covering the range  $m_A > 20$  GeV and  $0 < \tan\beta < 50$  [21, 35, 36, 37]. All get broadly similar results, including radiative corrections but mostly ignoring possible SUSY decay modes, and estimate in what regions of parameter space the various MSSM Higgs signals would be detectable. Typical results from Ref.[21] for  $m_t = 150$  GeV are shown in Fig.17. Notice that  $H$  and  $A$  have only small detectability regions for these standard signals, and even the  $h$  regions are restricted, although the MSSM  $\rightarrow$  SM limiting region ( $m_A \rightarrow$  large) is covered as we would expect. In fact, the conventional  $h, H, A \rightarrow \gamma\gamma, ZZ^*, ZZ$  and  $t \rightarrow H^+b$  searches do not cover the whole  $(m_A, \tan\beta)$  parameter plane. Even when we include LEP1 and LEP2 search potential, there is an intermediate region, approximately  $110 < m_A < 160$  GeV and  $\tan\beta > 3$  (depending on your choice of  $m_t$  and authors), where none of the usual signals would be detectable.

There have been various responses to this inaccessible area (IA).

- (a) Additional signals from  $H \rightarrow \tau\tau$  and  $A \rightarrow \tau\tau$  could possibly cover the large- $\tan\beta$  part of the IA[37], but identifying and measuring tau pairs is very difficult.
- (b) Additional signals from  $A \rightarrow Zh \rightarrow \ell\ell\tau\tau$  would not reduce the IA; neither would new  $A \rightarrow \chi_2^0 \chi_2^0 \rightarrow \ell\ell\ell\ell + \text{missing-}p_T$  signals[34].
- (c) SUSY-GUT models have attractive solutions where the top Yukawa coupling  $\lambda_t$  approaches a fixed point (see e.g. Ref.[26]) and gives a constraint  $m_t \simeq (200 \text{ GeV}) \sin\beta$ . With  $m_t \simeq 150 - 170$  GeV, this defines a small- $\tan\beta$  region outside the IA, and incidentally predicts that  $h$  is light enough to be discovered at LEP2 [38]. However, even in this optimistic scenario, not all 5 Higgses can be simultaneously detectable.
- (d) With efficient multiple- $b$ -tagging, the signals from  $t\bar{t}h(H, A) \rightarrow b\bar{b}b\bar{b}WW$  or  $b\bar{b}h(H, A) \rightarrow b\bar{b}b\bar{b}$  could be visible at LHC. For  $\tan\beta \gtrsim 5$ , where the Higgs couplings to  $b$  are enhanced, Ref.[39] argues that it will be possible to detect either  $A$  and  $h$ , or  $A$  and  $H$ , and essentially remove the IA. Fig.18 shows discovery regions at the two-sigma level for luminosity  $100 \text{ fb}^{-1} =$  one LHC year (i.e. the two-sigma level after four years) with  $m_t = 150$  GeV and  $m_{\tilde{t}} = 1$  TeV; the boundary curves marked

$h, i, j, k, l, m$  correspond to  $ttH, tth, ttA, bbH, bbh, bbA$  signals respectively, and the label lies on the detectable side[39].

(e) Alternatively,  $e^+e^-$  colliders with energy above LEP2 (where  $\sqrt{s} \simeq 170 - 190$  GeV at most is planned) would be able to find at least one of the neutral Higgses via  $e^+e^- \rightarrow hZ, hA, HZ, HA$  searches, since there is an upper bound on  $m_h$ . Fig.19 shows the necessary conditions on  $\sqrt{s}$  and luminosity  $\mathcal{L}$  to cover the whole  $(m_A, \tan\beta)$  half-plane with  $\tan\beta > 1$ , using  $Zh \rightarrow \tau\tau jj, \ell\ell jj, \nu\nu jj$  and  $jjjj$  final states with b-tagging [40]. The condition depends on  $m_t$  because of radiative corrections ( $m_t = 1$  TeV is assumed here).

#### 4.6 Summary.

- (a) The five MSSM Higgses have a richer spectrum than the SM, but are in some ways more elusive.
- (b) The lightest scalar mass is bounded much more stringently than in the SM.
- (c) There will be evidence for physics beyond the SM if we find any neutral scalar with non-SM coupling, or more than one neutral scalar, or a charged scalar.
- (d) The principal Higgs-sector parameters are  $m_A$  and  $\tan\beta$ , with radiative corrections controlled mostly by  $m_t$  and  $m_{\tilde{t}}$ . Masses, couplings, production and decay – and hence Higgs signals – vary strongly across the  $(m_A, \tan\beta)$  plane.
- (e) LEP1 plus LEP2 coverage in this plane is limited (approximately to the  $m_h < 90$  GeV region in Fig.15(a).
- (f) LHC coverage (earlier SSC studies are similar) of the remaining parameter space was thought to be incomplete; but recent studies of  $tth(H, A) \rightarrow bbbbWW$  and  $bbh(H, A) \rightarrow bbbb$  signals assuming efficient multiple- $b$ -tagging remove this weakness.
- (g) An  $e^+e^-$  collider with energy just a little way above LEP200 could also guarantee to see at least  $h$ .
- (h) Future useful signals could include  $A \rightarrow Zh \rightarrow \ell\ell\tau\tau$ ,  $A \rightarrow \chi_2^0\chi_2^0 \rightarrow 4\ell + \text{missing-}p_T$ , heavy  $H^\pm \rightarrow tb$ .
- (i) Future theory constraints could come from SUSY-GUT refinements and  $b \rightarrow s\gamma$ .

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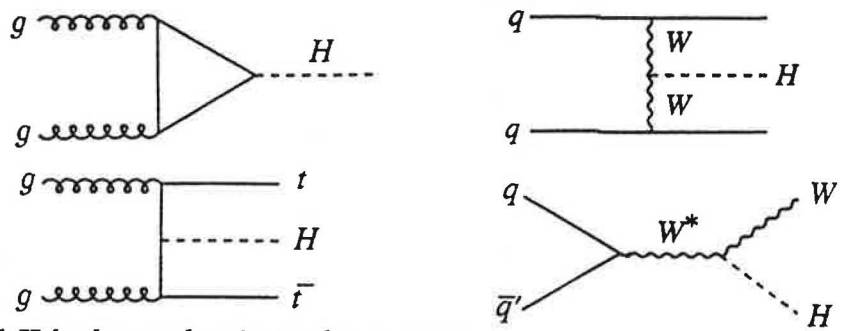


Fig.1. Standard Model H hadroproduction subprocesses.

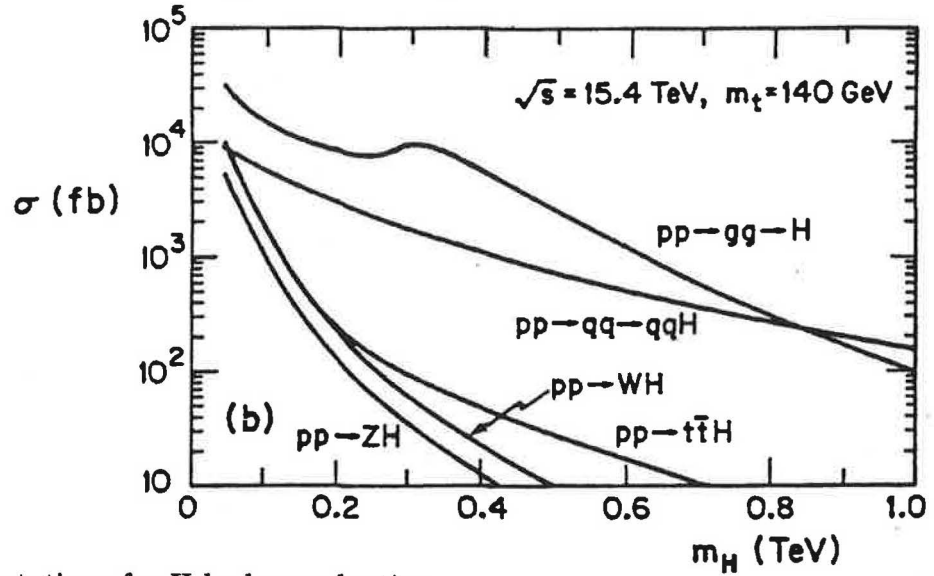


Fig.2. SM expectations for H hadroproduction.

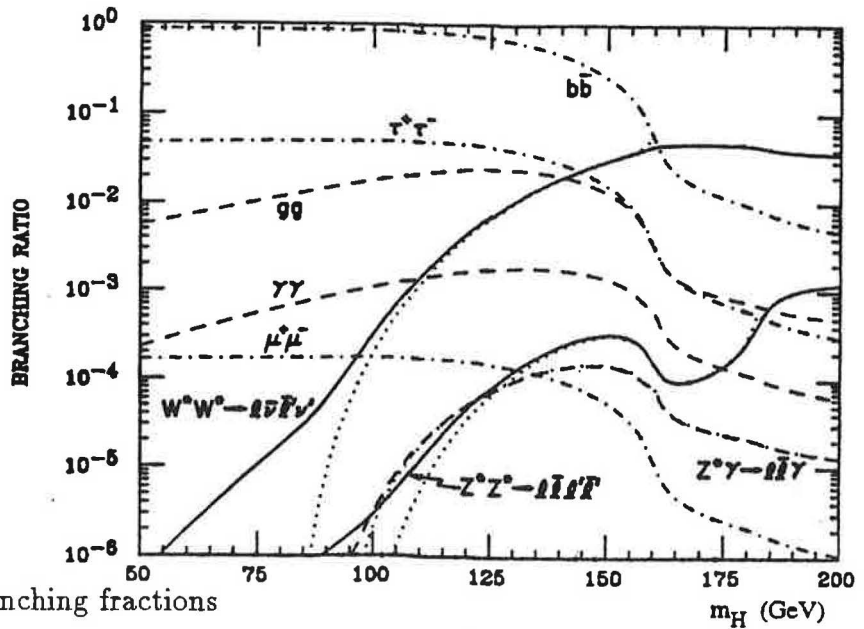


Fig.3. SM Higgs branching fractions



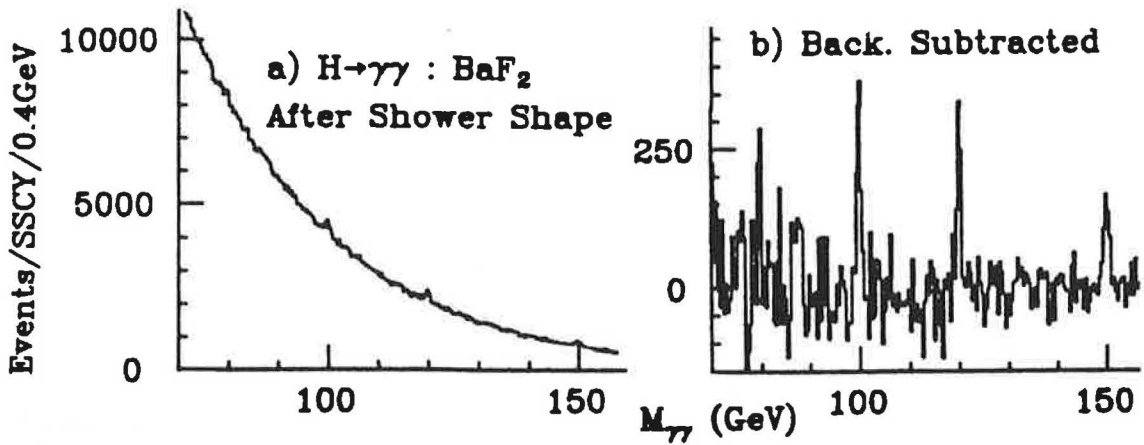


Fig.4.  $H \rightarrow \gamma\gamma$  signals for  $m_H = 80, 100, 120, 150$  GeV [2].

Fig.5. Lepton-tagged  $H \rightarrow \gamma\gamma$  signals for  $m_H = 80, 100, \dots, 160$  GeV [3].

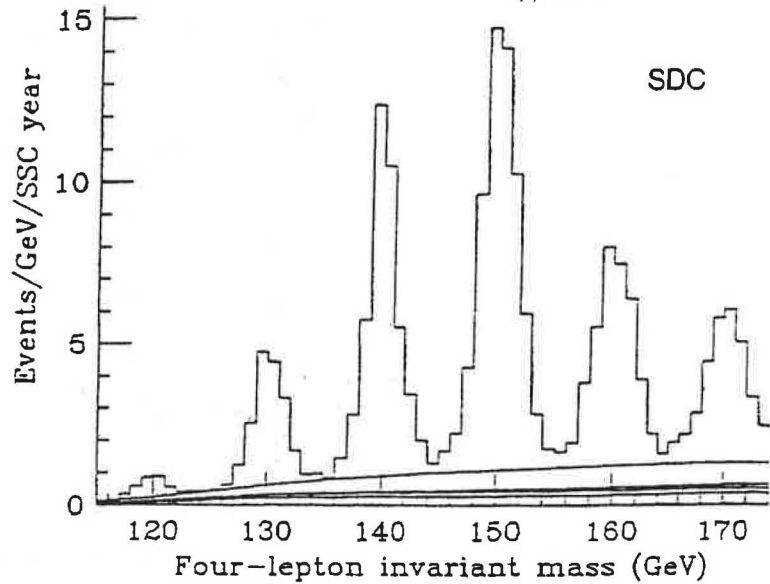
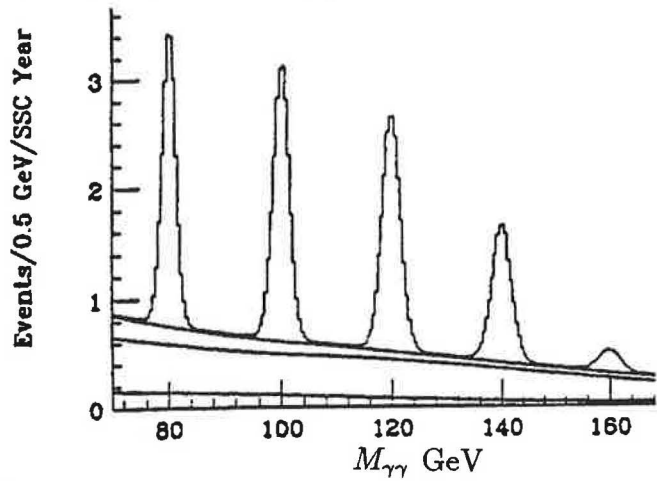


Fig.6.  $H \rightarrow \ell\bar{\ell}\ell'\bar{\ell}'$  signals for  $m_H = 120, 130, \dots, 170$  GeV [3].



Fig.7. Double-lepton tagged  
 $H \rightarrow b\bar{b}$  dijet signal and  
background for  $m_H = 100$  GeV [4].  
 $t\bar{t}H$  and  $t\bar{t}Z$  contributions are shaded

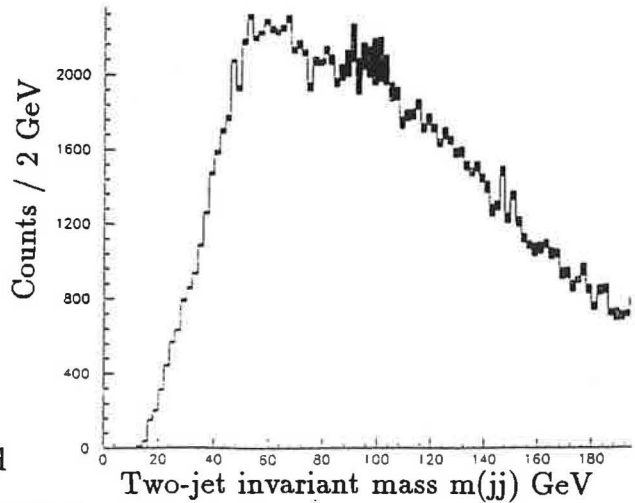


Fig.8.  
 $H \rightarrow b\bar{b}$  dijet signals  
and background with  
3 - b - jet tagging for  
 $m_H = 80, 100, 120, 140$  GeV [5]

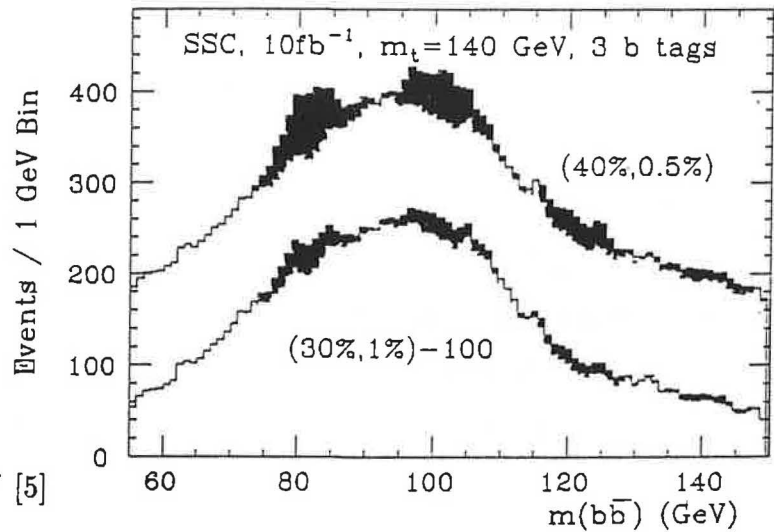


Fig.9  
Cross sections for the  
 $H \rightarrow \ell\bar{\ell}\ell'\bar{\ell}'$  gold-plated  
signals at the SSC and LHC .

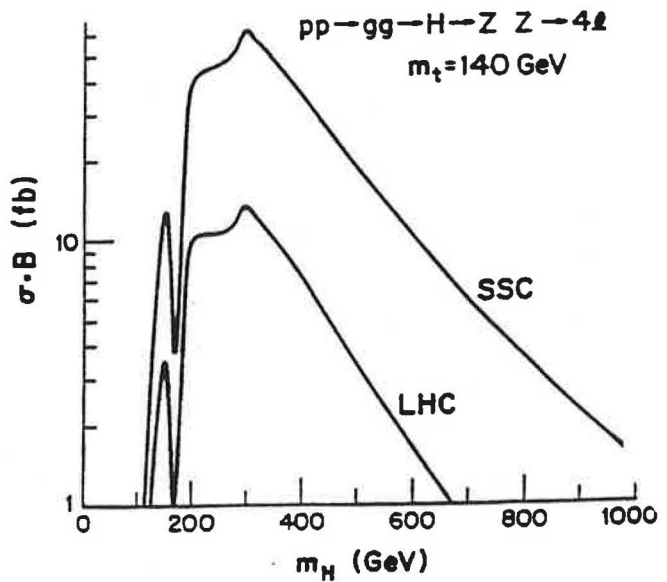


Fig.10  
 Gold-plated  $H \rightarrow ZZ \rightarrow 4\ell$   
 mass peaks and background  
 predicted at the CERN LHC  
 for  $m_H = 600, 800$  GeV [8]

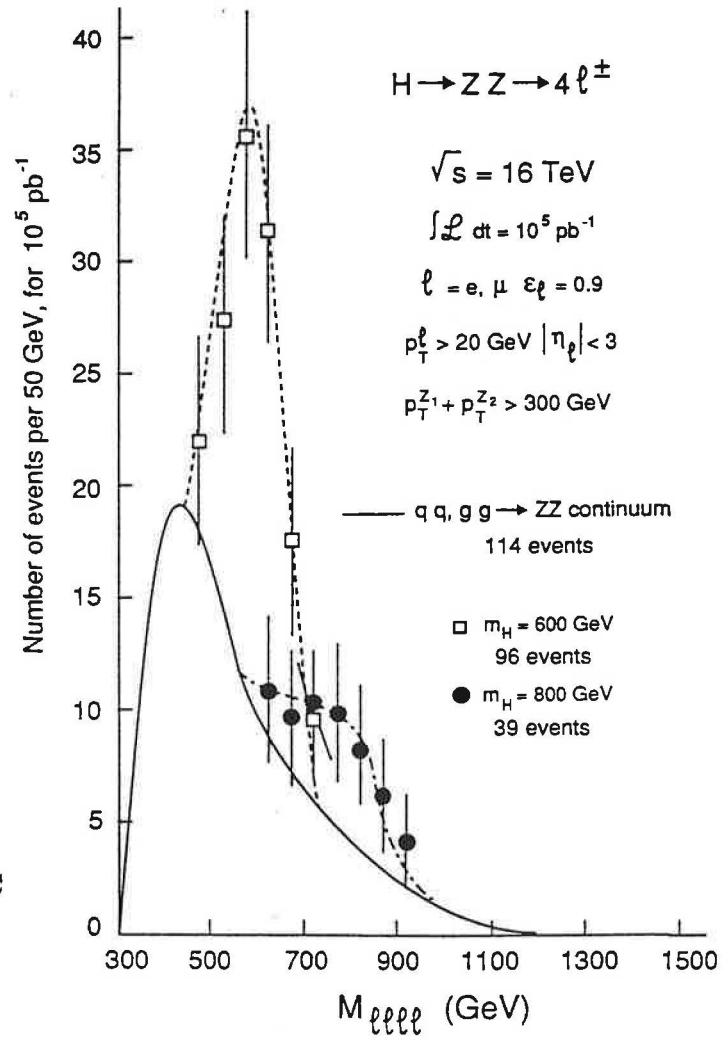


Fig.11.  
 Silver-plated  
 $H \rightarrow ZZ \rightarrow \ell\nu\nu$  signals  
 appearing as shoulders  
 in the missing- $E_T$  plot  
 (an SSC example [3]).

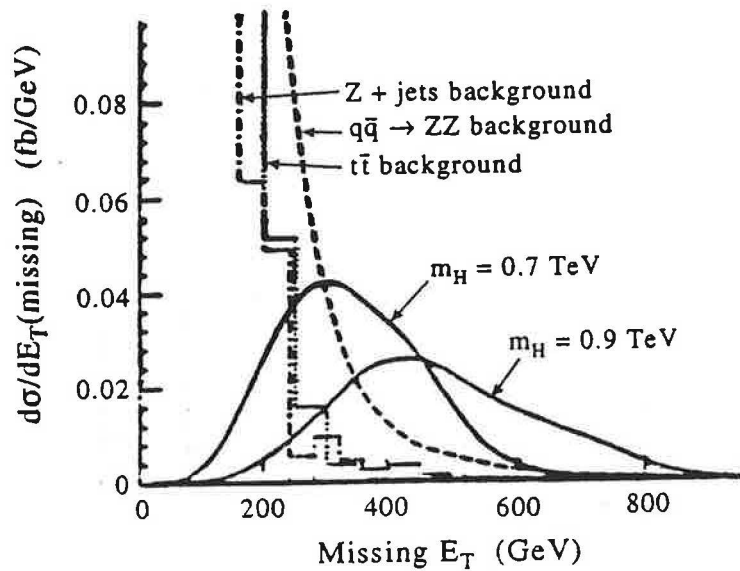


Fig.12.

Longitudinal weak  
boson scattering  
at a  $pp$  collider

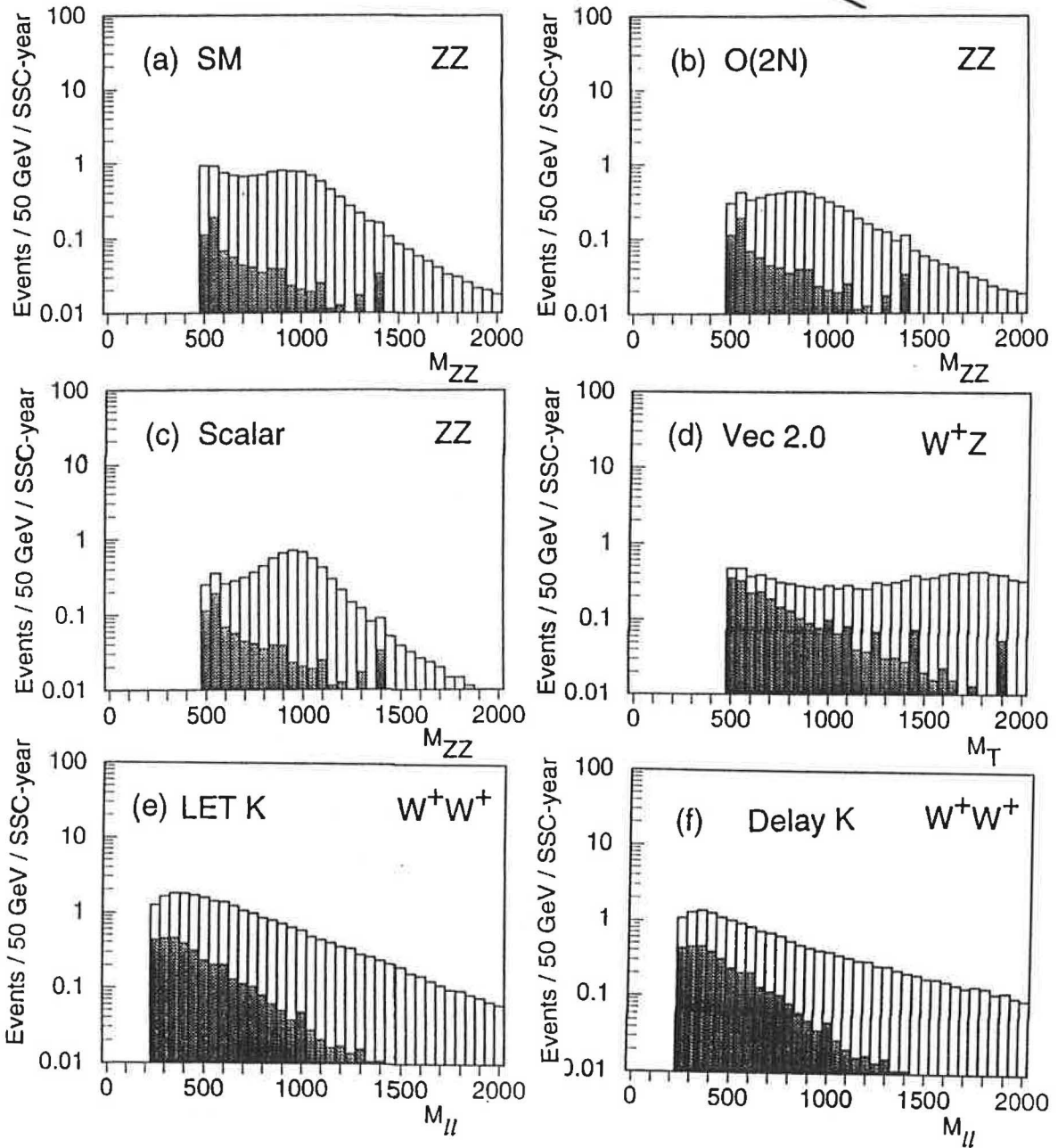
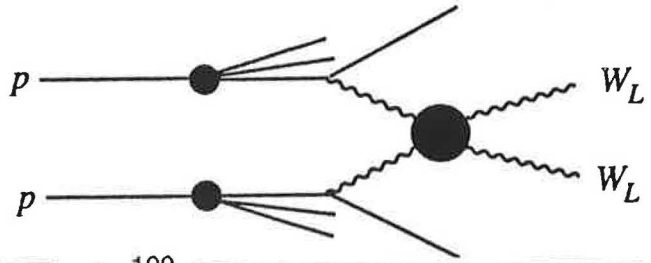


Fig.13. Typical weak-boson scattering signals (unshaded) and backgrounds (shaded)[15].

Fig.14.

Typical  $t$  and  $\bar{t}$   
one-loop graphs.

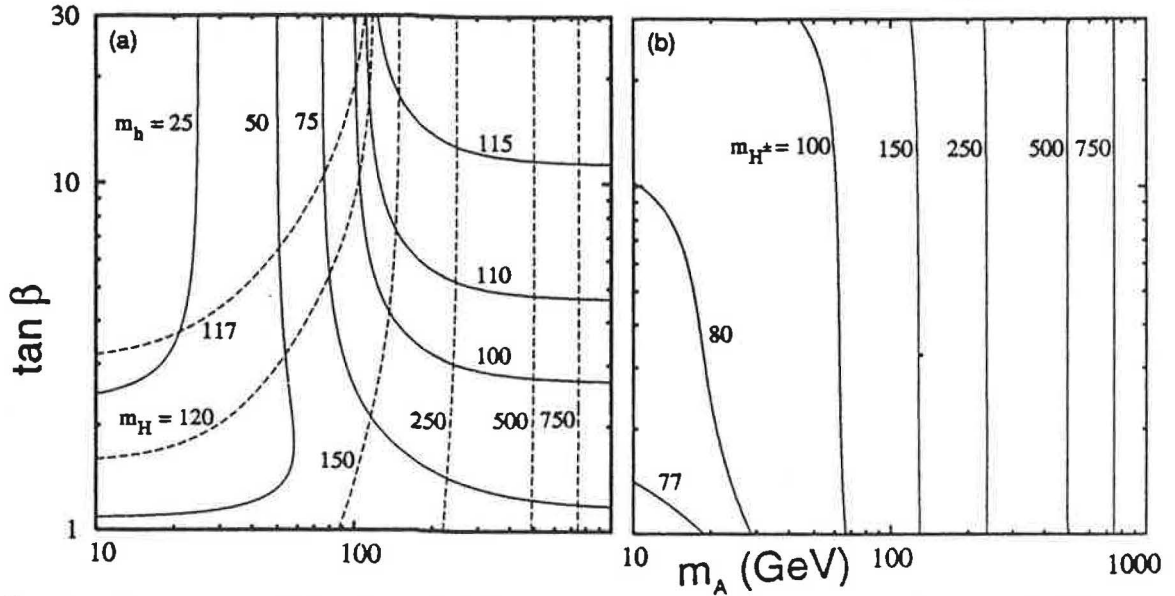


Fig.15. Behaviour of  $h$ ,  $H$  and  $H^\pm$  masses in the  $(m_A, \tan\beta)$  plane including 1-loop radiative corrections [21].

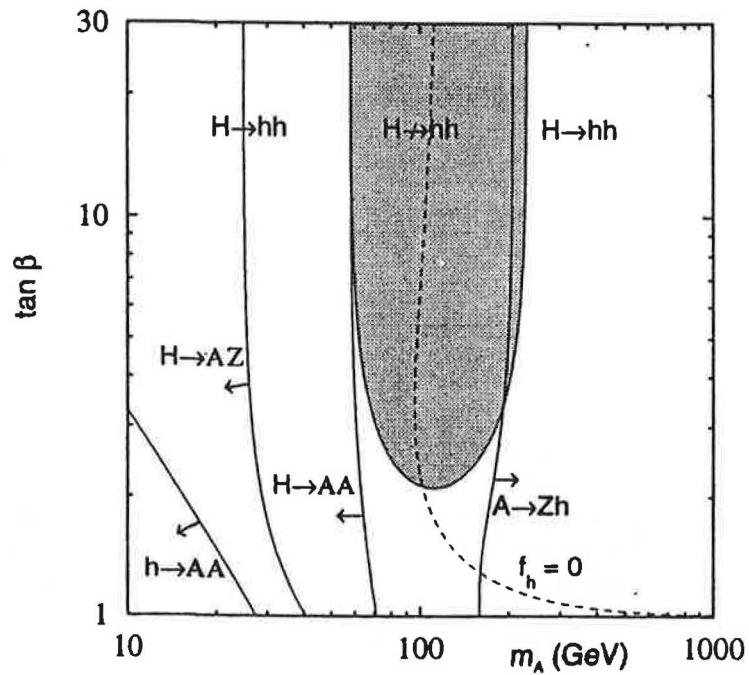


Fig.16. Regions where non-SM neutral Higgs decays compete [21].

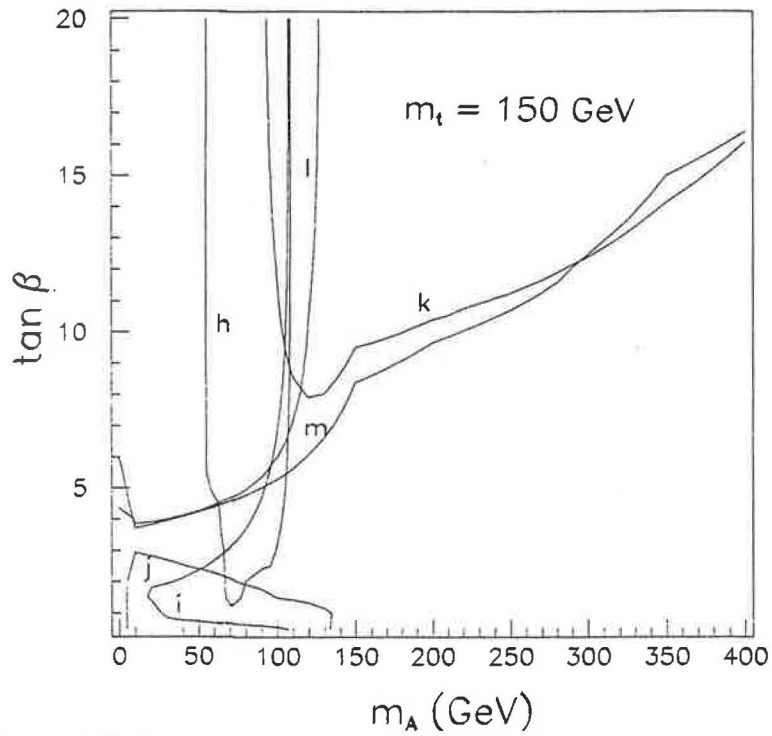


Fig.18. Expected LHC discovery regions for  $tth(H, A)$  and  $bbh(H, A)$  signals [38].

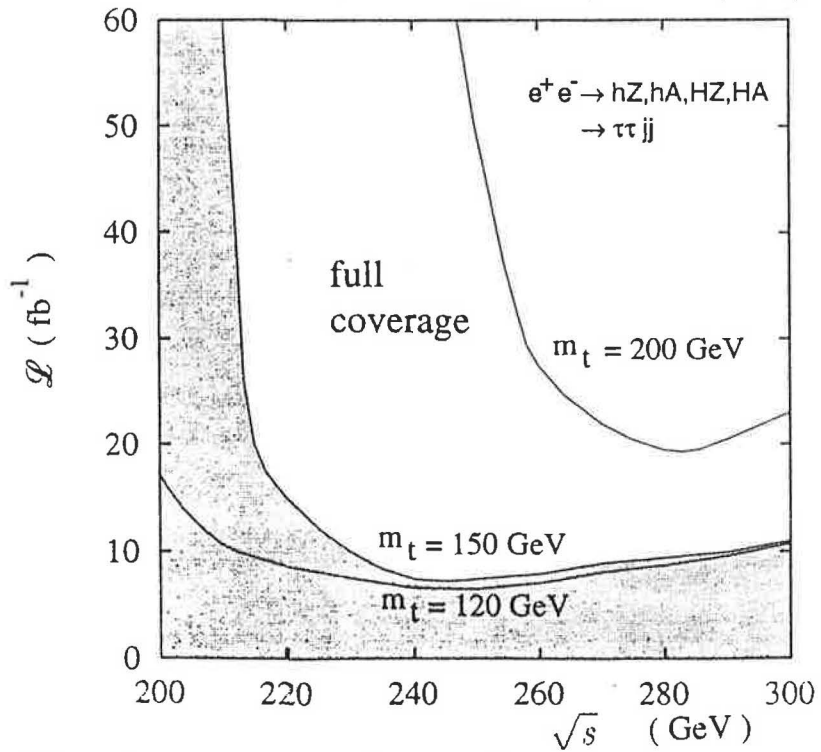


Fig.19. Conditions for covering the  $(m_A, \tan \beta)$  parameter space with an  $e^+e^-$  collider [39].





